

The BOSS–WiggleZ overlap region – II. Dependence of cosmic growth on galaxy type

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ABSTRACT

The anisotropic galaxy two-point correlation function (2PCF) allows measurement of the growth of large-scale structures from the effect of peculiar velocities on the clustering pattern. We present new measurements of the auto- and cross-correlation function multipoles of 69 180 WiggleZ and 46 380 Baryon Oscillation Spectroscopic Survey CMASS galaxies sharing an overlapping volume of $\sim 0.2 (h^{-1} \text{ Gpc})^3$. Analysing the redshift-space distortions (RSD) of galaxy two-point statistics for these two galaxy tracers, we test for systematic errors in the modelling depending on galaxy type and investigate potential improvements in cosmological constraints. We build a large number of mock galaxy catalogues to examine the limits of different RSD models in terms of fitting scales and galaxy type, and to study the covariance of the measurements when performing joint fits. For the galaxy data, fitting the monopole and quadrupole of the WiggleZ 2PCF on scales $24 < s < 80 h^{-1} \text{ Mpc}$ produces a measurement of the normalized growth rate $f\sigma_8(z = 0.54) = 0.409 \pm 0.055$, whereas for the CMASS galaxies we found a consistent constraint of $f\sigma_8(z = 0.54) = 0.466 \pm 0.069$. When combining the measurements, accounting for the correlation between the two surveys, we obtain $f\sigma_8(z = 0.54) = 0.413 \pm 0.048$, in agreement with the Λ Cold Dark Matter of structure growth and with other survey measurements.

Key words: cosmological parameters – cosmology: observations – large-scale structure of Universe.

1 INTRODUCTION

The evolution of the spatial distribution of galaxies on large scales is deeply influenced by the physics of gravitational attraction, cosmic expansion, and the conditions of the early Universe, and it constitutes an important probe and discriminator of cosmological models. Spectroscopic galaxy surveys map this distribution using the distance–redshift relation, but due to peculiar velocities induced by the gravitational field, these maps also contain ‘redshift-space distortions’ (RSD) of the spatial positions of the galaxies, which modify the true (i.e. real space) pattern of the spatial clustering of galaxies. On large scales the peculiar velocity field \mathbf{v} (in dimensionless units of the Hubble velocity) is related to the matter overdensity δ_m as $\nabla \cdot \mathbf{v} = -f\delta_m$, where the proportionality parameter $f(z)$ is called the linear growth rate of structure. Kaiser (1987)

used this relation to derive the impact of peculiar velocities on the power spectrum measured in redshift space. Modelling the redshift-space clustering, in consequence, allows us to constrain cosmological parameters through estimations of $f(z)$. Using Kaiser’s findings, the pioneering works in the 2dFGRS survey (Peacock et al. 2001; Hawkins et al. 2003) in the local $z \sim 0.1$ Universe, measured the redshift-space two-point clustering of galaxies, which resulted in a confirmation of the concordance Λ cold dark matter (ΛCDM) model at present times. With the advent of galaxy surveys at higher redshifts, we can now trace the history of $f(z)$ and obtain constraints on cosmological models and the nature of dark energy (Linder & Cahn 2007).

However, important challenges must be addressed before we can use this tool effectively. On the observational side, the most important factors limiting the statistical precision of the clustering measurements obtained from different surveys are the limited volume that the surveys can map, due to the *sample variance* from fluctuations in the clustering on different regions of the universe,

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and the discreteness of the galaxy field known as *shot noise* (e.g. Kaiser 1986; White, Song & Percival 2009)

In addition, large-scale structures are subject to a variety of systematic non-linear effects which affect our capacity to model the signal, particularly on small scales. First, galaxies possess non-linear pairwise velocities on small scales, which produces a roughly exponential suppression of the power spectrum on small scales (Peacock 1992; Peacock & Dodds 1994). Secondly, we have non-linear growth of structure (Cole, Fisher & Weinberg 1994), such that even on large scales, the Kaiser relations are insufficient to account for the measured clustering in galaxy data and simulations. A number of authors, in many cases building on the work of Fisher (1995) among others, have improved the basic ‘Kaiser’ model by including various non-linear effects in the matter clustering (Scoccimarro 2004; Taruya, Nishimichi & Saito 2010; Seljak & McDonald 2011; Wang, Reid & White 2014, among others). Finally, there is scale-dependent complexity in how galaxies trace haloes and cross-correlate to matter, known as *galaxy bias*. The latest attempts to use the two-point clustering pattern to model RSD have taken these and other effects into account (e.g. Beutler et al. 2012; Reid et al. 2012; Contreras et al. 2013; de la Torre et al. 2013; Sánchez et al. 2013; Beutler et al. 2014, as recent examples), allowing us to confront predictions from different cosmological models.

Although in linear theory all galaxies respond as test particles to the gravitational field, in detail the non-linear systematics depend on tracers themselves. This is because galaxy formation is affected by many non-linear processes such as small-scale dynamics of halo formation, environment, and complex baryonic processes determining the luminosity and colour at a given time, which are the main observables when selecting galaxies for a large-scale survey. Therefore, the analysis and modelling of two overlapping tracers makes it possible to constrain details of the clustering and formation of the galaxy tracers themselves. Previous work has focused on cross-correlating a tracer with well-known properties with a second tracer we wish to study (e.g. Martínez et al. 1999; Chen 2009; Mountrichas et al. 2009; Font-Ribera et al. 2013). In our current study, we approach this in a cosmological context, in which a comparison of results using different tracers in the same volume tests for systematic errors in modelling of bias and RSD.

In this work, we present measurements and analysis of RSD using galaxies from the WiggleZ Dark Energy Survey (Drinkwater et al. 2010) and the CMASS galaxy sample from the Baryon Oscillation Spectroscopic Survey (BOSS; Dawson et al. 2013). At a redshift of $z \approx 0.6$, the WiggleZ team targeted emission-line galaxies hosted in low-to-intermediate mass haloes, which have low bias ($b_{\text{WiggleZ}} \sim 1$; see Blake et al. 2011a; Contreras et al. 2013; Marín et al. 2013), while the CMASS sample consists of luminous, mostly red galaxies with $b_{\text{CMASS}} \sim 2$ (Reid et al. 2012; Tojeiro et al. 2012; Chuang et al. 2013; Kazin et al. 2013) with similar number density $n \sim 2-3 \times 10^{-4} (h^{-1} \text{ Mpc})^{-3}$. With an overlap volume of approximately $0.2 (h^{-1} \text{ Mpc})^{-3}$, this is, to date, the largest volume overlapping sample between two different galaxy redshift surveys. We measure the redshift-space auto- and cross-correlation functions of these galaxies and explore the constraints on the cosmic growth rate using the two tracers. Our work is supported by a large suite of mock catalogues, which we generated using abbreviated N -body methods (COLA; Tassev, Zaldarriaga & Eisenstein 2013) to model potential systematics coming from observational issues, test different RSD models and their regime of validity, and determine covariances.

A potential advantage of a multitracers analysis was described by McDonald & Seljak (2009), who noted that the correlations in an overlapping volume, if the number density of the tracers is large,

can be used to reduce the sample variance error and improve the measurements of the growth rate. After this initial work, different applications of the multitracers method have been explored by various authors, using different observables such as photometric redshift surveys, weak lensing, gravitational redshifts, signatures of first stars and constraints on primordial non-gaussianity and modified gravity (Seljak 2009; Bernstein & Cai 2011; Gaztañaga et al. 2012; Asorey, Crocce & Gaztanaga 2014; Croft 2013; Lombriser, Yoo & Koyama 2013; Yoo & Seljak 2013). Blake et al. (2013) noted that using the cross two-point correlation function (2PCF) of tracers provides independent validation of the underlying assumption of close correlation between the two tracers and also serves to test the assumption of linear galaxy bias. They applied this multitracers analysis to the GAMA survey power spectra, producing modest gains from the multitracers method, up to 20 per cent in the constraints of f at two different epochs, $z = 0.18$ and $z = 0.38$. Ross et al. (2014) measured the clustering of BOSS galaxies as a function of their colour and did not detect significant differences in distance scale or structure growth measurements. Although the data sets used in our study are too sparse to expect large improvement, we include this effect by computing the full covariance of the measurements using our mock galaxy catalogues.

We present in Section 2 the surveys used in our study. In Section 3, we present the methods and results of the auto- and cross-correlation between tracers. In Section 4, we show models of the RSD and constraints in the model parameters and the growth rate at $z = 0.54$. Finally in Section 5, we summarize our results and conclude. This is the second work of a series of papers analysing clustering in the BOSS–WiggleZ overlap region. Paper I (Beutler et al. 2015) focuses on the analysis of the Baryonic Acoustic Oscillation signal of these two tracers in the common volume.

For clarity we will use the name ‘CMASS-BW’ and ‘WiggleZ-BW’ (BW from BOSS–WiggleZ overlap) for the CMASS and WiggleZ samples limited to the overlap region between the two surveys. We assume a fiducial flat Λ CDM cosmological model as defined in Komatsu et al. (2009), where the matter density is $\Omega_m = 0.273$, baryon density of $\Omega_b = 0.045$, a spectral index of $n_s = 0.963$, an rms of density fluctuations averaged in spheres of radii at $8 h^{-1} \text{ Mpc}$ of $\sigma_8 = 0.81$ and $h = 0.71$. The Hubble rate at redshift $z = 0$ is $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$ is adopted to convert redshifts to distances, which are measured in $h^{-1} \text{ Mpc}$.

2 DATA & MOCK CATALOGUES

2.1 The WiggleZ survey

The WiggleZ Dark Energy Survey (Drinkwater et al. 2010) is a large-scale galaxy redshift survey performed over 276 nights with the AAOmega spectrograph (Sharp et al. 2006) on the 3.9 m Anglo-Australian Telescope. With an area coverage of 816 deg^2 , this survey has mapped 207 000 bright emission-line galaxies over a redshift range $0.1 < z < 1.0$. Target galaxies in six different regions were chosen using UV photometric data from the GALEX survey (Martin et al. 2005) matched with optical photometry from the Sloan Digital Sky Survey (SDSS DR4; Adelman-McCarthy et al. 2006) and from the Red-Sequence Cluster Survey 2 (RCS2; Gilbank et al. 2011). The selection criteria consisted of applying magnitude and colour cuts (Drinkwater et al. 2010) in order to select star-forming galaxies with bright emission lines with a redshift distribution centred around $z \sim 0.6$. The selected galaxies were observed in 1-h exposures using the AAOmega spectrograph, and their redshifts were estimated from

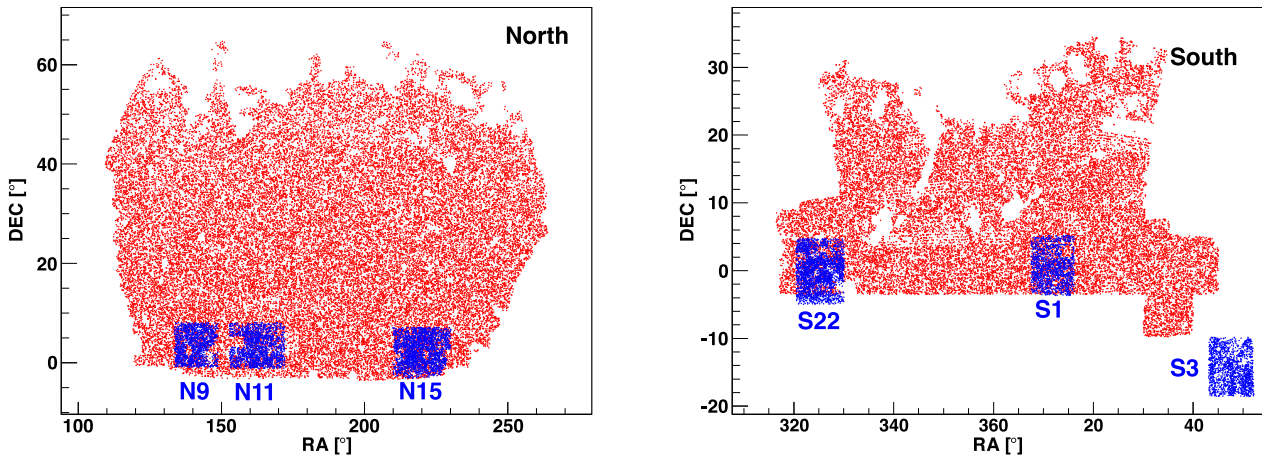


Figure 1. Sky coverage of BOSS-CMASS DR11 (red) and WiggleZ (blue). The left-hand panel shows the northern part of the surveys, while the right-hand panel shows the southern sky coverage. Five of the six WiggleZ regions are covered by CMASS, with a total of 69 180 WiggleZ galaxies and 46 380 CMASS galaxies in the overlap volume.

strong emission lines. The number density of WiggleZ galaxies averages $\sim 3 \times 10^{-4} (h^{-1} \text{ Mpc})^{-3}$ at $z = 0.6$.

2.2 The CMASS sample

The BOSS (Dawson et al. 2013) of the Sloan Digital Sky Survey III (SDSS-III; Eisenstein et al. 2011), which is now complete, was designed to obtain spectra and redshifts for 1.35 million bright galaxies over a footprint $\sim 10\,000 \text{ deg}^2$. These galaxies are selected from the SDSS-III imaging and have been observed together with 160 000 quasars and 100 000 ancillary targets (Gunn et al. 2006; Bolton et al. 2012; Smee et al. 2013). The CMASS sample is composed of luminous, mostly red galaxies selected to probe large-scale structure at intermediate redshifts, achieving a number density of $\sim 3 \times 10^{-4} (h^{-1} \text{ Mpc})^{-3}$. The DR11 catalogue (Alam et al. 2015) includes 1 100 000 spectra out of which the CMASS sample contains $\approx 550\,000$ galaxies in the redshift range $0.43 < z < 0.7$.

2.3 Overlap volumes

We define the overlap regions between CMASS and WiggleZ using the random galaxy catalogues generated for each survey, gridding the sky into 0.1 deg^2 regions and selecting cells containing both CMASS and WiggleZ random points. As seen in Fig. 1, five of the six WiggleZ regions have considerable overlap with CMASS galaxies, totalling 560 deg^2 and a volume of $0.218 (h^{-1} \text{ Gpc})^3$ in the $0.43 < z < 0.7$ range. This results in an overlap sample of 69 180 WiggleZ galaxies and 46 380 CMASS galaxies.

Fig. 2 shows the redshift distribution of the two samples in the different regions, which is similar in the range $0.5 < z < 0.6$; outside that range the CMASS galaxy counts rapidly decline. To estimate how these differences will affect our results, we calculate the pair-weighted redshift, which consists in taking the average redshift of all pairs at a particular distance range. For the distance range $s = 20\text{--}35 h^{-1} \text{ Mpc}$, where the clustering signal is higher, WiggleZ-BW galaxies have a pair-weighted redshift of $z_{\text{WiggleZ-BW}} = 0.56$ whereas for CMASS-BW galaxies $z_{\text{CMASS-BW}} = 0.53$. For cross-pairs this redshift is $z_{\text{avg},x} = 0.54$. These small differences in redshift will not affect our findings given the measurement errors, therefore we generate cosmological models at $z_{\text{avg},x} = 0.54$ to compare with

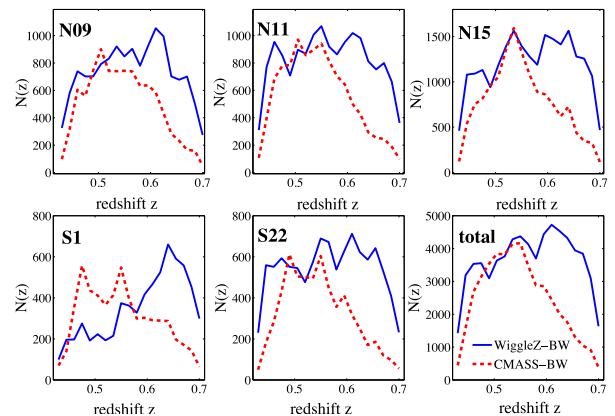


Figure 2. Number of galaxies as a function of redshift for WiggleZ (blue) and CMASS (red) galaxies in the overlap regions, and for the overall overlap volume (bottom-right panel).

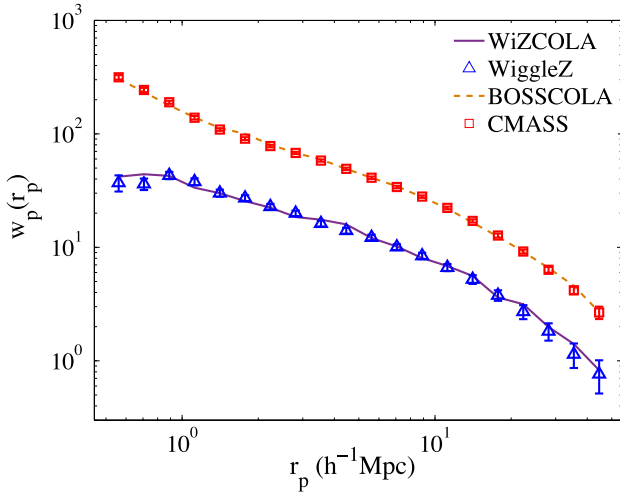
our WiggleZ-CMASS clustering data. Table 1 presents details of the samples used.

2.4 Simulations and mock catalogues

We estimate the covariance of our measurements and test the regime of validity of our RSD models using mock galaxy catalogues built from N -body simulations. The conventional methods to generate N -body simulations do not allow for the generation of a large number of realizations of cosmological volumes at sufficient mass resolution to encompass the low-mass haloes hosting WiggleZ galaxies, which are needed for constructing robust covariance matrices. For this reason we use an approximate, fast method to generate dark matter simulations based on the COmoving Lagrangian Acceleration method (COLA; Tassev et al. 2013). We have developed a parallel version of COLA (Koda et al. 2015; used first in Kazin et al. 2014), wherein each simulation contains 1296^3 particles in a box of side $600 h^{-1} \text{ Mpc}$, which gives a particle mass of $7.5 \times 10^9 h^{-1} M_\odot$, allowing resolution of low bias haloes with masses $10^{12} h^{-1} M_\odot$, found using friends-of-friends algorithm with a linking length of 0.2 times the mean particle separation. Each simulation requires 15 min with 216 computation cores, including halo finding, which

Table 1. Overlapping samples analysed in this study.

Region	WiggleZ-BW N_{gal}	WiggleZ-BW z_{avg}	CMASS-BW N_{gal}	CMASS-BW z_{avg}	Cross-pairs z_{avg}
S01	6620	0.61	5720	0.53	0.57
N09	13940	0.56	9360	0.53	0.54
N11	15560	0.55	10580	0.53	0.54
N15	22740	0.56	14660	0.54	0.54
S22	10320	0.55	6060	0.53	0.54
Total	69180	0.56	46380	0.53	0.54


Figure 3. Projected correlation function $w_p(r_p)$ for WiggleZ and CMASS galaxies in the overlap regions (symbols). Lines are the mean values of $w_p(r_p)$ for the COLA mock catalogues.

is much faster than a classical N -body simulation, but with similar precision on the relevant scales ($k < 1 \, h \, \text{Mpc}^{-1}$).

We generate a total of 2400 realizations (480 for each WiggleZ region) of a flat Λ CDM universe with *WMAP5* cosmological parameters (Komatsu et al. 2009), which defines our fiducial cosmology. Using the output at $z = 0.6$ we create WiggleZ-based (WiZcola) and CMASS-based (BOSScola) mock galaxy catalogues, from Halo Occupation Distribution models (HOD; Berlind & Weinberg 2002), such that the resulting projected correlation functions $w_p(r_p)$ match those of the observations, as seen in Fig. 3.

For details on how the mock catalogues were constructed please refer to Koda et al. (2015). In summary, for the emission-line galaxies in the WiggleZ we use a lognormal HOD (Zehavi et al. 2005), since we do not expect to see these galaxies in very large mass haloes. We assume that the probability that a dark matter halo of mass M (measured in $h^{-1} M_\odot$) hosts one WiggleZ galaxy is

$$P_{\text{WiggleZ}}(M) = \exp \left[-\frac{(\log_{10} M - \log_{10} M_0)^2}{2\sigma_{\log M}^2} \right], \quad (1)$$

where $\log_{10} M_0 = 12.275$, fixing $\sigma_{\log M} = 0.1$. These values fit $w_p(r_p)$, and to obtain the WiggleZ expected density we randomly subsample each realization to match the smooth number density.

For CMASS galaxies, we adopt the model used by Blake, Collister & Lahav (2008), using the error function for the central galaxies, where the probability of populating one central galaxy in a dark matter halo of mass M is

$$P_{\text{CMASS}}(M) = \frac{1}{2} \left[1 + \text{erf} \left(\frac{\log_{10} M - \log_{10} M_{\min}}{\sigma_{\log M}} \right) \right] \quad (2)$$

and, if there is a central galaxy in the halo, the number of satellite galaxies is obtained from a Poisson distribution with mean

$$\langle N_{\text{sat}} \rangle = (M_{200,m}/M_0)^\beta. \quad (3)$$

We find $\log_{10} M_{\min} = 12.92$, $\sigma_{\log M} = 0.37$, $\log_{10} M_0 = 14.00$, and $\beta = 1.45$ for the CMASS HOD. We then apply the relevant selection functions to the mock galaxies to match the survey geometry. Our simulations encode the joint covariance in the overlapping survey regions.

3 MEASUREMENTS

3.1 Measuring correlation functions

We estimate the redshift-space two-point correlation function $\xi(s, \mu)$ (2PCF) as a function of comoving separation s and the cosine of the angle of the distance vector with respect to the line of sight (LOS) $\mu = \cos(\theta)$. We use the Landy & Szalay (1993) estimator, counting pairs of objects in data and random catalogues:

$$\xi_{\text{auto}}(s, \mu) = \frac{DD(s, \mu) - 2DR(s, \mu) + RR(s, \mu)}{RR(s, \mu)}, \quad (4)$$

where DD , DR , and RR are, respectively, the weight-normalized data–data, data–random, and random–random pairs with separation s and μ (with a given resolution Δs , $\Delta \mu$). For both the random and data catalogues, we use the optimal (inverse-density) FKP weighting (Feldman, Kaiser & Peacock 1994):

$$w_i(\mathbf{x}) = \frac{1}{1 + n(\mathbf{x})P_0}, \quad (5)$$

where $P_0 = 5000 (h^{-1} \text{Mpc})^3$ for WiggleZ-BW and $P_0 = 20000 (h^{-1} \text{Mpc})^3$ for CMASS-BW galaxies. For WiggleZ galaxies, angular incompleteness and radial selection are introduced in the random catalogues (Blake et al. 2010). A small fraction of galaxies contain errors in the redshift assignment, but this effect is absorbed into the fitted galaxy bias factor. CMASS galaxies, have additional weights applied to account for the angular incompleteness, fibre collisions, redshift failure, and correlation between density of targets and density of stars (Ross et al. 2012).

It is possible to model the 2PCF using the full information from $\xi(s, \mu)$, but that requires a large covariance matrix with the associated problems with its inversion. For this reason it is standard to compress this information in multipoles

$$\xi_l(s) = \frac{2l+1}{2} \int_{-1}^1 \xi(s, \mu) L_l(\mu) d\mu, \quad (6)$$

where L_l is the Legendre polynomial of order l . In practice we approximate equation (6) by a discrete sum over the binned $\xi(s, \mu)$,

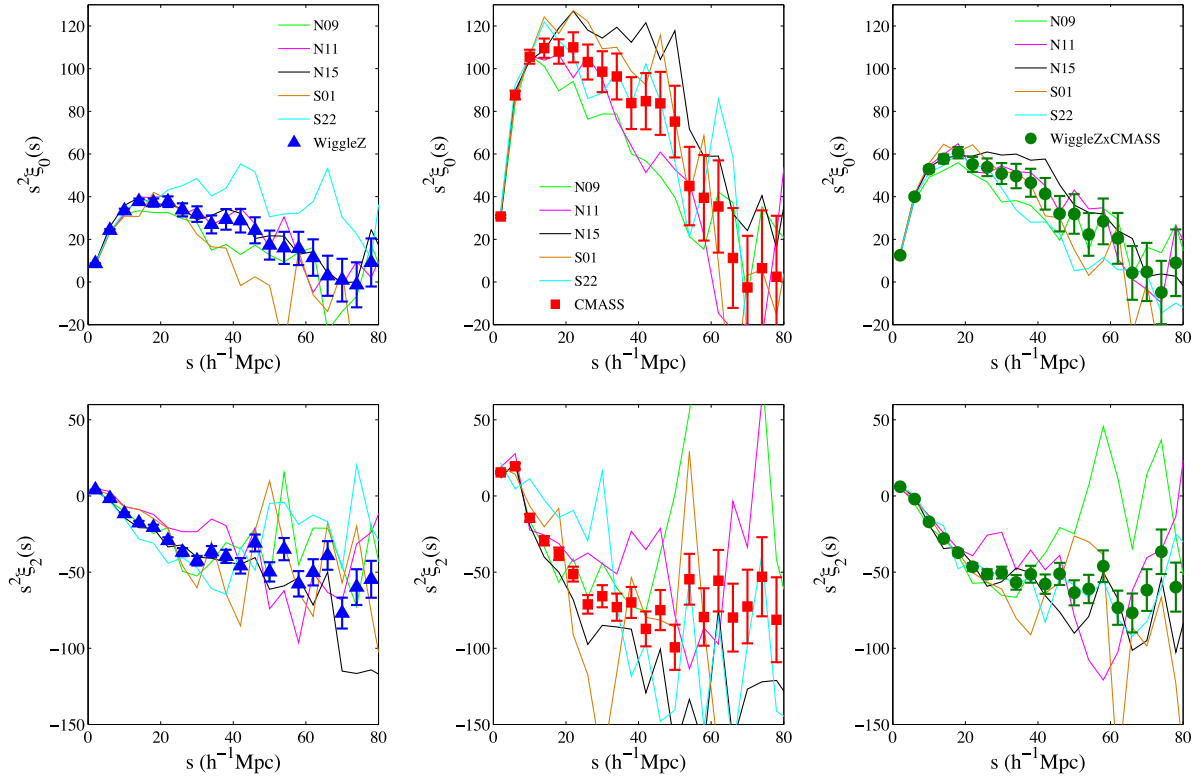


Figure 4. Combined monopole (top row) and quadrupole (bottom row) of $\xi(s, \mu)$ for the WiggleZ and CMASS autocorrelation function (left-hand and middle columns) and the cross-correlation function (right-hand column). Lines are measurements of individual regions, symbols display the combined measurements. Results are plotted as $s^2\xi_l(s)$ as a function of separation s .

where we use $\Delta s = 4 h^{-1}$ Mpc and $\Delta\mu = 0.01$ for every WiggleZ-BW and CMASS-BW region. We use the monopole ($l = 0$) and quadrupole ($l = 2$) of the two-point functions, to analyse the RSD, for separations $s < 80 h^{-1}$ Mpc. Our results are unchanged if larger separations are used, whilst the increase in variance due to the finite number of mocks becomes significant.

The covariance of each region is estimated from the mock WiZola and BOSScola catalogues (see Section 3.3). After calculating the covariances of the measurements in each overlap region from the COLA mock catalogues, we use inverse-variance weighting to obtain the ‘optimally combined’ measurements. For the statistic $\xi_{l,\text{comb}}(s)$, the optimally combined function is calculated as

$$\xi_{l,\text{comb}}(s) = C_{\text{comb}} \sum_{i=1}^{N_{\text{reg}}} C_i^{-1} \xi_{l,i}(s), \quad (7)$$

where C_{comb} is the overall covariance matrix, calculated from the estimations of the covariance matrices of individual regions C_i (see Section 3.3) and where $N_{\text{reg}} = 5$ is the total number of regions. Results for the auto-2PCFs are shown in Fig. 4, for individual regions (as lines) and for the combined measurements (as symbols). The different amplitude of clustering of the WiggleZ-BW and CMASS-BW galaxies reflects the difference in the type of haloes these galaxies inhabit. Due to the limited volume where the correlations are measured, we correct our correlation function values by the ‘integral constraint’ (Peebles 1980; Beutler et al. 2012). The corrections to the WiggleZ and BOSS correlations differ in each region and have values of the order of 8×10^{-4} and 1×10^{-3} , respectively, for the smaller regions (where the integral constraint is higher), and do not significantly affect the RSD model constraints.

3.2 Cross-correlations between WiggleZ-BW and CMASS-BW clustering

In addition to the autocorrelations, we also measured the cross-correlation between the two sets for tracers using the estimator

$$\xi_{\text{cross}}(s, \mu) = \frac{D_W D_C - D_W R_C - R_W D_C + R_W R_C}{R_W R_C}, \quad (8)$$

where the W and C subscripts represent the quantities in the WiggleZ and CMASS galaxies, respectively. The cross-correlation function measurement provides an independent validation of the assumption that both galaxy types trace the same large structures on a range of scales, and also serves to test our linear and local galaxy bias model.

To test the strength of the correlation between the tracers, we also constrain the cross-correlation coefficient, r_{\times} , which is produced from the relation

$$\xi_{\text{WiggleZ} \times \text{CMASS}}^{l=0}(s) = r_{\times}^2(s) \xi_{\text{WiggleZ}}^{l=0}(s) \xi_{\text{CMASS}}^{l=0}(s), \quad (9)$$

with $|r_{\times}| \leq 1$. On large scales in redshift-space, and assuming linear, deterministic bias, this quantity should tend to the value (Mountrichas et al. 2009):

$$r_{\times, \text{Kaiser}} = \frac{1 + \frac{1}{3}(\beta_W + \beta_C) + \frac{1}{3}\beta_W\beta_C}{\sqrt{(1 + \frac{2}{3}\beta_W + \frac{1}{3}\beta_W^2)(1 + \frac{2}{3}\beta_C + \frac{1}{3}\beta_C^2)}}. \quad (10)$$

Assuming $b_W = 1$ and $b_C = 2$ (Reid et al. 2012; Contreras et al. 2013), and a growth rate $f(z) = 0.54$ (0.75), when estimating $\beta = f/b$, it is expected that $r_{\times, \text{Kaiser}} = 0.997 \sim 1$.

We measure the value of r_{\times} from our data, assuming it is a constant on all scales (an assumption we do not expect to hold on scales smaller than $15\text{--}20 h^{-1}$ Mpc). Using the RSD model described in Section 4.1, and the COLA mocks to build our covariance matrix,

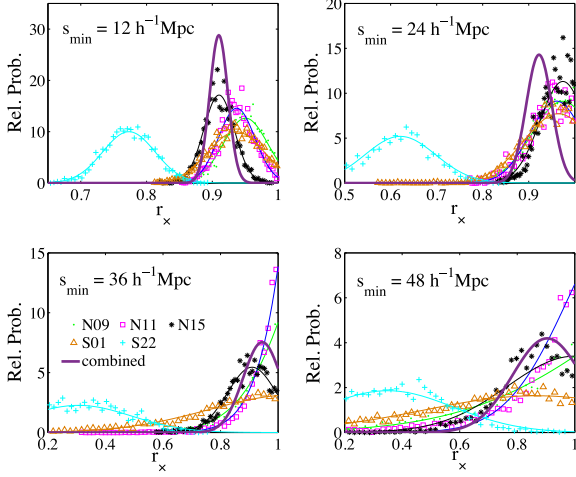


Figure 5. The cross-correlation coefficient r_x for the WiggleZ-CMASS-BW correlations for each overlap region, and when combining all regions, as a function of the smallest scale s_{\min} (in h^{-1} Mpc) of the fit.

we use the correlation monopoles to fit for the bias parameters of the WiggleZ-BW and CMASS-BW galaxies and r_x for each overlap region and the joint likelihood (see Section 4.3 for details of the fitting procedure).

Fig. 5 presents the posterior probability distribution of r_x , as a function of the minimum scale of fit s_{\min} . Focusing on the fits to the combined regions, we can see that they are not consistent with $r_x = 1$ at the 2σ level on scales $s_{\min} \sim 20 h^{-1}$ Mpc. This behaviour may be explained by a number of factors such as non-linear pairwise velocities, non-linear bias and stochasticity. CMASS galaxies tend to be hosted in the centres of large haloes and in high-density regions, precisely the regions that are avoided by WiggleZ galaxies. We expect that on large scales both galaxies trace similar structures, and this is confirmed in the measurements of r_x being consistent with 1 when fitting on large scales.

Examining individual regions it can be noticed that it is region S22 which reduces the overall fit to r_x . Its lower value of r_x is driven by a high autocorrelation function in the WiggleZ-BW S22 region, although the measured values are reasonably within the scatter of the mock catalogues. The best fits to the growth rate do not significantly change when the S22 region is excluded, and in the final fits we include all regions.

3.3 Covariance estimation

We estimate the correlations between the multipoles of the auto- and cross-2PCF by calculating the covariance matrix in each region n from COLA mocks. A deviation from the mean of a quantity X , in separation bin i , for the mock k can be written as

$$\Delta_{i,n}^k = X_i^k - \langle X_i \rangle, \quad (11)$$

where, in our case, X corresponds to the monopole or quadrupole of the auto- or cross-2PCF in each bin. The covariance matrix of each region n is determined as

$$C_{n,ij} = \frac{1}{N_{\text{mocks}}} \sum_{k=1}^{N_{\text{mocks}}} \Delta_{i,n}^k \Delta_{j,n}^k. \quad (12)$$

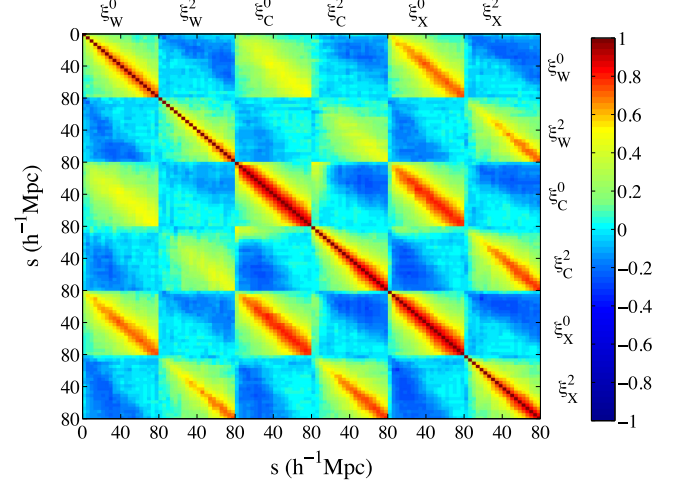


Figure 6. Correlation matrix (normalized covariance matrix) of the WiggleZ-CMASS multipoles based on COLA mocks. The matrix is divided in the contributions from the monopole and quadrupole of WiggleZ-BW (W), CMASS-BW (C), and cross 2PCF (X), and each pixel represents a separation s (in h^{-1} Mpc).

After calculating C_n for all regions, we can determine the combined covariance matrix (Blake et al. 2011b)

$$C_{\text{comb}}^{-1} = \sum_{n=1}^{N_{\text{comb}}} C_n^{-1}. \quad (13)$$

Fig. 6 shows the correlation matrix (normalized covariance matrix) for all our measurements, showing the strong correlation between the measurements of the two tracers.

Since we used a large, but finite number of mock catalogues for the covariance estimation (used later in the likelihood tests) and the standard deviation of the samples, there are biases when we wish to use this covariance matrix for model fitting. Following the work of Hartlap, Simon & Schneider (2007), we rescale the inverse of the covariance matrix by

$$C_{\text{comb,H}}^{-1} = \frac{N_{\text{mocks}} - N_{\text{bins}} - 2}{N_{\text{mocks}} - 1} C_{\text{comb}}^{-1}, \quad (14)$$

where $N_{\text{mocks}} = 480$ is the number of the realizations of the mock galaxy catalogues and N_{bins} denotes the number of bins used. Percival et al. (2014) introduces additional corrections to obtain an unbiased estimation of the variance of the model parameters estimated from the likelihood distribution. When using the mock catalogues to estimate our covariance matrix and the observed data (i.e the CMASS-WiggleZ galaxy correlations), the variance estimated from the likelihood distribution should be multiplied by

$$m_\sigma = \frac{1 + B(N_{\text{bins}} - N_p)}{1 + 2A + N(N_p + 1)}, \quad (15)$$

where N_{bins} is the number of bins entering the fits, N_p is the number of free parameters, and

$$A^{-1} = (N_{\text{mocks}} - N_{\text{bins}} - 1)(N_{\text{mocks}} - N_{\text{bins}} - 4), \quad (16)$$

$$B = A(N_{\text{mocks}} - N_{\text{bins}} - 2). \quad (17)$$

In case we use the mocks as data to build the likelihood function, used for instance in the case where we want to validate our models as in Section 4.2, this variance should be further multiplied by

$$m_v = m_\sigma \frac{N_{\text{mocks}} - 1}{N_{\text{mocks}} - N_{\text{bins}} - 2}. \quad (18)$$

We perform measurements in separation bins up to $s = 80 h^{-1}$ Mpc. From constraining models using one-tracer autocorrelation function multipoles to simultaneous fits using both auto- and cross-correlations, the m_σ factor lies in the range $m_\sigma = 1.05\text{--}1.2$.

4 CONSTRAINTS ON COSMIC GROWTH

4.1 Modelling the RSD

RSD modify the two-point clustering of galaxies on both large and small scales, which we will summarize here. Due to its peculiar velocity \mathbf{v} , a galaxy at a position in real space \mathbf{r} gets mapped to \mathbf{s} in redshift space:

$$\mathbf{s} = \mathbf{r} + \frac{(1+z)\mathbf{v} \cdot \hat{\mathbf{r}}}{H(z)} \hat{\mathbf{r}}, \quad (19)$$

where $\hat{\mathbf{r}}$ is the galaxy unit vector along the LOS direction, $v_r \equiv \mathbf{v} \cdot \hat{\mathbf{r}}$ is the LOS component of its velocity, and $H(z)$ is the Hubble parameter at a redshift z .

On large scales, as described by Kaiser (1987), hereafter **K87** (also see Hamilton 1998 for derivations in configuration space), matter overdensities δ_m grow coherently as $\nabla \cdot \mathbf{v} \propto -f\delta_m$ where $f \equiv d \ln G(a)/d \ln a$ is the linear growth rate of fluctuations. The evolution of the growth rate in certain models can be approximated by the evolution of the matter density in the universe $f(z) = \Omega_m(z)^\gamma$, where $\gamma = 0.55$ in the case that the large-scale gravity obeys General Relativity; for alternative theories of gravity, γ can take on different values (Linder & Cahn 2007). **K87** assumes that the difference in clustering between dark matter and galaxies can be described by a linear bias model where $\delta_g = b\delta_m$. In redshift space, the clustering has a directional dependence, parametrized by μ , the cosine of the angle of the distance vector with respect to the LOS. In Fourier space, thus, the galaxy overdensity takes the form

$$\delta_g(\mathbf{k}) = (b + f\mu^2)\delta_m(\mathbf{k}), \quad (20)$$

creating in configuration space the so-called squashing effect on large scales.

On smaller scales in redshift space, structures appear elongated along the LOS, creating the observed ‘Fingers of God’. In Fourier space this effect can be modelled by introducing a Gaussian or a Lorentzian pairwise velocity distribution (i.e. a convolution of a Gaussian or exponential profile in configuration space) multiplying the large-scale RSD of the power spectrum. The simplest model for the redshift space galaxy power spectrum, using Gaussian damping for the galaxy power spectrum in redshift space, is predicted to be

$$P^s(k, \mu) = (b + f\mu^2)^2 P_m(k) e^{-(k\mu\sigma_v/H)^2}. \quad (21)$$

In this model, $P_m(k)$ represents the non-linear real-space power spectrum and σ_v the linear pairwise velocity dispersion, predicted to be

$$\sigma_v^2(z) = \frac{f^2(z)H^2(z)}{6\pi^2(1+z)^2} \int P_{\theta\theta}(k) dk, \quad (22)$$

where, in the **K87** formalism, $P_{\theta\theta} = P_m$.

However, this simple model has been shown in simulations to be insufficiently accurate on large scales, because there is not a perfect correlation between density and the velocity (divergence) field (e.g. Okumura & Jing 2011; de la Torre & Guzzo 2012; Kwan, Lewis & Linder 2012; White et al. 2015). Scoccimarro (2004), hereafter **S04**, suggested a modification of the simple Kaiser formalism by including the velocity field terms. In the case of one tracer, the

RSD in the galaxy autopower spectrum reads

$$P_a^s(k, \mu) = [b^2 P_{\delta\delta}(k) + 2\mu^2 f b P_{\delta\theta}(k) + \mu^4 f^2 P_{\theta\theta}(k)] e^{-(k\mu\sigma_v/H)^2}, \quad (23)$$

where $P_{\delta\delta}$, $P_{\delta\theta}$, and $P_{\theta\theta}$ are the non-linear matter density–density, density–velocity, and velocity–velocity power spectra, respectively. In our analysis, these terms are obtained from fitting formulae derived by Jennings (2012), from a suite of N -body simulations.

Using this correction, our fiducial model (based on *WMAP5* results, see Section 1) predicts (via equation 22) the large-scale velocity dispersion σ_v to be $\sigma_v(z=0.6) \sim 220 \text{ km s}^{-1}$. We will also make the approximation that on the scales we study all galaxies respond as equal tracer particles to the gravitational potential (i.e. there is no linear velocity bias), making σ_v independent of the galaxy tracer. However, we choose to leave σ_v as a free parameter to account for any additional non-linearities on smaller scales. This particular formalism has been successfully used in a number of studies (e.g. Blake et al. 2011a, 2013; de la Torre et al. 2013), and, as we will see below, reproduces the expected constraints on the growth rate from the COLA mock catalogues and provides a good description of the galaxy anisotropic clustering at the current statistical level (see Taruya et al. 2010; Reid & White 2011; Seljak & McDonald 2011; Wang et al. 2014, for additional improvements on RSD modelling).

In the case of the redshift-space cross-power spectrum, assuming that both tracers are described by the same dispersion parameter σ_v , we can write the large-scale terms as

$$P_x^s(k, \mu) = [b_1 b_2 P_{\delta\delta}(k) + \mu^2 f (b_1 + b_2) P_{\delta\theta}(k) + \mu^4 f^2 P_{\theta\theta}(k)] \times e^{-(k\mu\sigma_v/H(z))^2}, \quad (24)$$

where b_1 and b_2 are the biases of the different tracers. Since we are measuring the multipoles of the 2PCF, we calculate first the power spectrum multipoles as

$$P_l^s(k) = \frac{2l+1}{2} \int_{-1}^1 P^s(k, \mu) L_l(\mu) d\mu, \quad (25)$$

where l is the multipole order and L_l is the Legendre polynomial of order l . Then for the 2PCF in configuration space we have

$$\xi_l^s(s) = \frac{i^l}{2\pi^2} \int P_l^s(k) j_l(ks) k^2 dk, \quad (26)$$

where j_l is the spherical Bessel function of order l .

4.2 Tests using COLA mocks

We tested the validity of these models using our COLA mock catalogues. In summary, we compared the **K87** and **S04** models for the large-scale distortions to $P(k)$ (calculated using our fiducial cosmological parameters), using a Gaussian function for the small-scale damping (we also tried fits using the Lorentzian profile without significant differences), constraining the growth rate f at the simulation output redshift $z = 0.6$, marginalizing over the bias of each tracer and the common velocity dispersion σ_v . We performed these fits for every COLA mock on scales $s < 80 h^{-1}$ Mpc, although changes when using larger scales were not significant.

Fig. 7 shows the mean and standard deviation of the best-fitting values of $f(z = 0.6)$ across the mocks. For the WiZcola mocks the **K87**+Gaussian model tends to underpredict the value of the growth rate whereas the **S04**+Gaussian model agrees well for scales $s_{\min} > 20 h^{-1}$ Mpc. For the BOSScola mocks the differences are less pronounced, but the input growth rate is recovered with a systematic error less than the statistical error. In both cases the goodness of fit

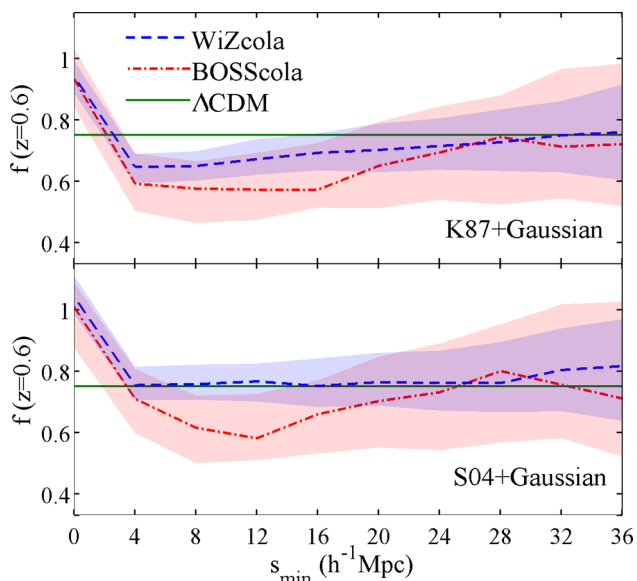


Figure 7. Constraints on the linear growth rate $f(z = 0.6)$ using COLA mock galaxies with the same angular and redshift selection functions as the galaxy survey data. Fits to the growth rate $f(z = 0.6)$ ($=0.76$, for the *WMAP5* cosmology, green solid line) are performed for the models as a function of s_{\min} , with $s_{\max} = 80 h^{-1}$ Mpc. Coloured shades cover the 1σ (68 per cent) confidence interval for f , defined using the dispersion in the best-fitting values across the 480 mocks.

is similar with $\chi^2/\text{d.o.f.} \sim 1$ for both WiggleZ and BOSS COLA mocks on larger scales $s_{\min} > 20 h^{-1}$ Mpc, worsening considerably on scales $s_{\min} < 10 h^{-1}$ Mpc. In what follows we will use the **S04+Gaussian** model for our parameter fits.

There are, however, specific differences in the scale of validity of the models depending on which tracer is used. It can be seen that for low-bias galaxies represented by the WiZcola mocks, the agreement between the model fits and the input value of $f(z = 0.6)$ extends to lower scales than in the case of galaxies residing in more massive haloes. Although the Kaiser effect is stronger for lower bias galaxies, the higher non-linearities arising from the formation and high-clustering of high-mass haloes lead to a model break-down on larger scales. For the particular case of the WiggleZ–BOSS overlap, $s_{\min} = 24 h^{-1}$ Mpc is the minimum scale where both models recover adequately the fiducial growth rate with negligible systematic error.

Multitracer approach

Having chosen the model to analyse redshift-space clustering, we examined the consequences of using multiple tracers when recovering model parameters. For each realization of the COLA mocks we fit the **S04+Gaussian** RSD model first using the autocorrelations independently, then analysing both autocorrelations but considering the common covariance matrix, and lastly adding the cross-correlations using the monopole and quadrupole of $\xi(s, \mu)$ in the range $24 < s < 80 h^{-1}$ Mpc. Results are shown in Fig. 8, which displays the 1σ contours enclosing the best-fitting values of $f(z = 0.6)$ and σ_v . The expected values for these parameters are consistent with our COLA constraints, and the approximation that σ_v is the same for both tracers is valid for this range of scales. The constraints for the parameters are correlated between the two surveys, with a cross-correlation coefficient $\rho_{WC}^f = \sigma_{WC}^f / \sigma_W^f \sigma_C^f = 0.4$ for the growth rate between both surveys.

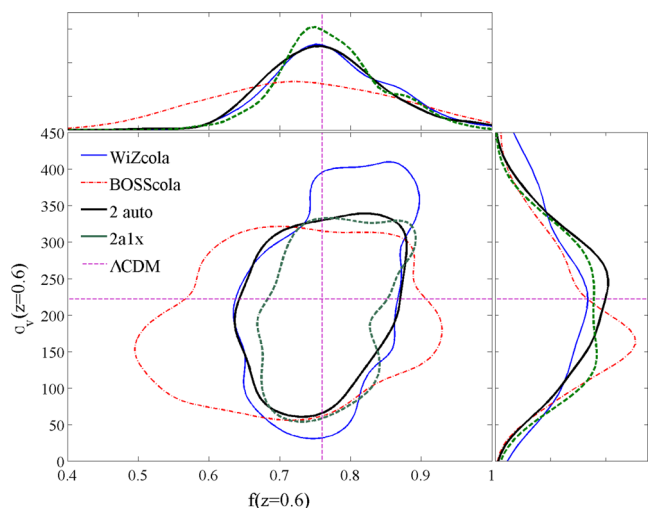


Figure 8. Constraints for RSD parameters in the **S04** model for fits to COLA mocks in the range $24 < s < 80 h^{-1}$ Mpc using 2PCF multipoles. Results for the full fit and for individual subsamples, with the contours enclosing 68 per cent of the best-fitting parameters are shown. The four cases considered are WiZcola mocks alone (blue solid line), BOSScola mocks alone (red dashed line), joint analysis of the autocorrelations (black solid line), and an analysis further adding the cross-correlation function (green dashed line).

When analysing the 2PCFs of the two tracers simultaneously, taking into account the common covariance, an improvement in the measurement of f is obtained, of the order of 30 per cent compared to using the BOSScola mocks alone (which because of a higher bias, have a lower value of β and hence a lower signal) but only 5 per cent compared to using WiZcola mocks alone. Adding the cross-2PCF produces an improvement of 20 per cent compared to the WiZcola-only constraints, mostly due to an increased signal in the shot-noise dominated regime. Analysing individual mocks shows that the improvement also varies in each realization. As predicted by McDonald & Seljak (2009), Gil-Marín et al. (2010), and Blake et al. (2013), although our tracers have big differences in their biasing, due to the sparsity of our sampling we are in the regime where shot noise dominates and improvement via the cancellation of cosmic variance is small.

4.3 Data fitting procedure

In our analysis, we fixed the cosmological parameters of the matter power spectra to the best-fitting *WMAP5* model (Komatsu et al. 2009), the fiducial cosmology of our COLA mocks, and constrain the parameters ($b_W, b_C, f(z = 0.54), \sigma_v$). Due to the degeneracy of the first three parameters with $\sigma_8(z)$, the rms of the matter density field in $8 h^{-1}$ Mpc spheres, we are effectively constraining ($b_W \sigma_8, b_C \sigma_8, f \sigma_8, \sigma_v$). When we also include the WiggleZ–CMASS cross-correlation in the analysis, we additionally fit for the parameter r_{\times} . We compare the constraints from the single-tracer model for each galaxy type to each other, and then include the common covariance and the cross-correlations in the cosmological fits.

We use the monopole and quadrupole of the tracers, and present results as a function of the minimum-scale fitted s_{\min} , with $s_{\max} = 80 h^{-1}$ Mpc. We execute a Maximum Likelihood parameter estimation test, where we minimize the quantity

$$\chi^2 = \sum_i \sum_j (X_{i,\text{model}} - X_{i,\text{data}}) \mathcal{C}_{\text{comb},ij}^{-1} (X_{j,\text{model}} - X_{j,\text{data}}), \quad (27)$$

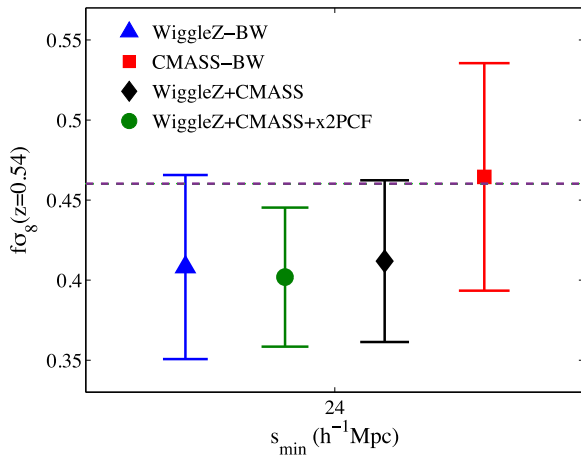


Figure 9. Fits to the RSD model parameters using correlation multipoles with $24 < s < 80 h^{-1}$ Mpc. We show results when analysing individual surveys and joint constraints. The purple line shows the prediction from *WMAP5* cosmology.

where X is one of the elements of the vector formed by the multipoles of $\xi(s, \mu)$ of WiggleZ-BW, CMASS-BW, and/or WiggleZ-CMASS-BW correlations. We explore the parameter space using a Monte Carlo Markov Chain method imposing the prior that all parameter values must be bigger than zero.

4.4 Fits for the growth rate

Fig. 9 presents the parameter fits of $f\sigma_8(z = 0.54)$ fitting the monopole and quadrupole of the WiggleZ and CMASS auto- and cross-correlation on scales between $s_{\min} = 24 h^{-1}$ Mpc, and $s_{\max} = 80 h^{-1}$ Mpc. As shown in the previous section, $s_{\min} = 24 h^{-1}$ Mpc is the minimum scale where there are not important systematic deviations in the parameters from the study with the COLA mocks, and our fits to the observed data follow this trend. Table 2 lists the results for the parameter fits.

Comparing the single-tracer fits for WiggleZ-BW and CMASS-BW galaxies, there is agreement at the 1σ level for the values of $f\sigma_8(z = 0.54)$, meaning that when fitting to these scales there is evidence of no systematics depending on the type of galaxy used. Our constraints on the growth rate are consistent with our fiducial cosmology $f\sigma_8(z = 0.54)_{\text{WMAP5}} = 0.46$ at the 1σ level, and with a slightly larger deviation, to the Planck cosmology result $f\sigma_8(z = 0.54)_{\text{Planck}} = 0.48$ (Planck Collaboration XVI 2014).

Consistent with previous work, we recover that the bias of the WiggleZ-BW galaxies, $b_W \sim 1$, is smaller than that of the CMASS-BW galaxies, $b_C \sim 2$. The value of the best-fitting chi-squared statistic indicates that the model provides a reasonable fit to the data in all cases. For the pairwise dispersion, values for the different tracers are consistent with the predicted value from theory (Section 4.1).

Combining the two tracers including their cross-covariance yields slightly better constraints for $f\sigma_8(z = 0.54)$ at the level of 10 per cent (compared to WiggleZ constraints alone). This result indicates that for these tracers, in a low-density regime (where the common cosmic variance cancellation does not improve the constraints; see Blake et al. 2013), even in the presence of a slightly larger Hartlap–Percival correction, the improvement is due to reduced shot noise. When including the cross-correlations the improvement is of the order of 20 per cent (again, compared with WiggleZ constraints alone). In the case when we include the cross-correlations, we obtain our poorest value for $\chi^2/\text{d.o.f.}$, implying that our simple constant r_\times model may not describe all of the complexities of the cross-correlation. Given this result, we quote as result of our paper for the growth rate constraint the one obtained when we combine only the autocorrelations, yielding $f\sigma_8(z = 0.54) = 0.413 \pm 0.048$.

5 SUMMARY AND CONCLUSIONS

In this work, we have presented the first cosmological RSD analysis using data from two overlapping surveys, WiggleZ and CMASS. After defining the overlap volumes, we measured two-point auto- and cross-correlations functions of these tracers; after obtaining their multipoles and calculating their cross-covariance using N -body mock catalogues, we compared them with RSD models in order to measure the growth rate of structure $f\sigma_8$ at an effective redshift $z = 0.54$. Our main findings are as follows.

- (i) The cross-correlation coefficient r_\times between the WiggleZ-BW and CMASS-BW galaxies agrees with the expectation that on large scales, the two classes trace similarly the large-scale structure with $r_\times \sim 1$. On smaller scales $s \lesssim 20 h^{-1}$ Mpc, $r_\times < 1$, likely produced by a combination of a number of factors such as non-linear pairwise velocities, non-linear bias and stochasticity.
- (ii) We tested RSD models in realistic mock catalogues simulating WiggleZ and CMASS galaxies. When fitting galaxy correlation functions on scales $s > 24 h^{-1}$ Mpc, a single velocity dispersion provides an adequate description for the distortions from different tracers, recovering our fiducial cosmological parameters in all cases.
- (iii) Using these mock catalogues, we confirmed a lack of a significant improvement when using the multitracers technique, given the sparsity of the sampling for these tracers.
- (iv) The fits to $f\sigma_8(z)$ from all tracers are consistent with each other, showing no evidence for strong modelling systematic errors as a function of galaxy type.
- (v) The combined fits to $f\sigma_8(z)$ are consistent with the predictions from *WMAP5* cosmology, and, with a slightly larger deviation, to the Planck cosmology results at the 1σ level.

As shown in Fig. 10, our combined fit for the growth rate $f\sigma_8(z = 0.54) = 0.413 \pm 0.048$ is in excellent agreement with estimates from different surveys. Although more sophisticated models for the RSD can be employed, the motivation for our work was to show consistency in the cosmological fits when using different tracers. This agreement provides further evidence for the robustness in

Table 2. Fits to the RSD model parameters when using multipoles with $24 < s < 80 h^{-1}$ Mpc assuming *WMAP5* $\sigma_8(z = 0) = 0.812$.

Tracers	$b_W\sigma_8(z = 0.54)$	$b_C\sigma_8(z = 0.54)$	$f\sigma_8(z = 0.54)$	σ_v (kms $^{-1}$)	r_\times	$\chi^2/\text{d.o.f.}$	d.o.f.
WiggleZ-BW only	0.651 ± 0.043	–	0.409 ± 0.055	205 ± 135	–	1.11	28 – 4
CMASS-BW only	–	1.204 ± 0.058	0.466 ± 0.069	130 ± 109	–	1.43	28 – 4
WiggleZ+CMASS	0.646 ± 0.038	1.233 ± 0.048	0.413 ± 0.048	117 ± 100	–	1.28	56 – 5
WiggleZ+CMASS+x2PCF	0.648 ± 0.031	1.242 ± 0.035	0.403 ± 0.040	88 ± 86	0.93 ± 0.024	1.57	84 – 6

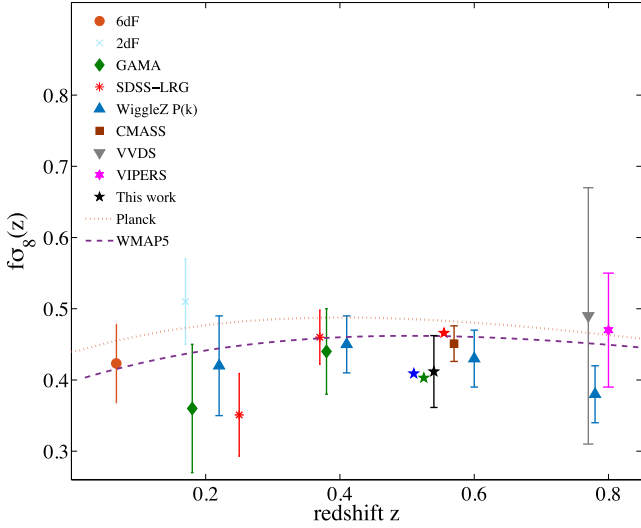


Figure 10. Fits to the growth rate $f\sigma_8(z)$ from different galaxy surveys: 6dF (Beutler et al. 2012), 2dFGRS (Hawkins et al. 2003), GAMA (Blake et al. 2013), WiggleZ (Blake et al. 2011a), SDSS LRGs (Samushia, Percival & Raccanelli 2012), CMASS-DR9 (Reid et al. 2012), VVDS (Guzzo et al. 2008), and VIPERS (de la Torre et al. 2013). For our work, the colours and order of the starred points match those of Fig. 9 and that the error bar has been put only on the WiggleZ+CMASS point for clarity.

the growth rate measurements at the current level of observational precision, which are important for answering the outstanding questions on the nature of dark energy and large-scale gravity.

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of Utah, Vanderbilt University, University of Virginia, University of Washington, and Yale University.

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