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## Composite Load Spectra for Select Space Propulsion Structural Components Final Report

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## CONTENTS

		Page
1.0	Introduction	1-1
	1.1 General	1-1
	1.2 Project Objective	1-2
2.0	Summary	2-1
3.0	SSME Overview	3-1
4.0	Engine Loads and CLS Engine Load Models	4-1
	4.1 Background	4-1
	4.2 SSME Deterministic Engine Model	4-2
	4.3 Probabilistic Load Models	4-10
5.0	Probabilistic Methodology	5-1
	5.1 Introduction	5-1
	5.2 Probabilistic Methods Quick Look Model	5-2
	5.3 Probabilistic Models	5-11
	5.4 Validation Studies	5-21
	5.5 Verification Studies	5-32
6.0	LDEXPT, The Load Expert System	6-1
	6.1 Objective and Approach	6-1
	6.2 Intelligence Database System Design	6-2
	6.3 Knowledge Engineering	6-4
	6.4 The Load Expert System: LDEXPT Version 2.1	6-6
	6.5 The Component Load Models	6-22
Ref	erences	R-1
Арр	endix A. Sample of LDEXPT Load Expert System Consultation Session	A-1
Арр	endix B. Turbine Blade Thermal Load Model	B-1
Арр	endix C. Pressure Fluctuations and Correlation Lengths = Summary and Critique	C-1
Арр	endix D. Periodic Load Model	D-1

## FIGURES

•

		Page
2.1	SSME Powerhead with LOX Posts, Transfer Ducts and Turbine Blades Identified	2-2
2.2	SSME HPOTP Discharge Duct	2-3
2.3	Multi-Level Engine Model	2-4
3.1	Typical SSME Thrust Profile	3-1
3.2	SSME Propellant Flow Schematic	3-2
3.3	SSME Standard Instrumentation Available on Powerhead	3-6
3.4	Data Analysis	3-7
3.5	Time from Engine Start, Secs	3-10
3.6	Thrust Profile	3-10
3.7	Pump Signature Test	3-11
3.8	High Pressure Fuel Pump Speed	3-11
3.9	AMS Fuel Preburner Pc	3-12
3.10	PSD Fuel Preburner Longitudinal Accel	3-13
3.11	Isoplot Fuel Preburner Longitudinal Accel	3-14
3.12	Statos Record	3-15
4.1	SSME Thrust Buildup Limits	4-3
4.2	SSME Engine Shutdown Thrust Decay from FPL (Altitude)	4-3
4.3	SSME Typical Flight Profile	4-4
4.4	SSME Start Timeline	4-9
4.5	Interrelation of SSME Analysis Models	4-9
5.1	Sample Transient Calculation: Five Mission Phase	5-19
5.2	Poisson Transient Model with NFIX = -1	5-20
5.3	ANLOAD Calculation for HPOTP Torque	5-22
5.4	Case Study I: Sum of Three Normally Distributed Variables	5-25
5.5	Case Study I: Upper Tail Values for Normal Sum	5-26
5.6	Case Study II: Product of Three Normally Distributed Variables	5-28
5.7	Case Study I: Upper Tail Value for Normal Product	5-29
5.8	Case Study III: Algebra of Three Normally Distributed Variables	5-30
5.9	Case Study III: Upper Tail Value for Normal Algebra	5-31
5.10	Comparison of ANLOAD Prediction and Data for Fuel Mass Flow	5-37

1

## FIGURES (Continued)

		Page
5.11	Comparison of ANLOAD Prediction and Data for LOX Mass Flow	5-39
5.12	Comparison of ANLOAD Prediction and OPB Discharge Temperature	5-40
5.13	Comparison of ANLOAD and HPOT Discharge Temperature	5-41
5.14	Comparison of ANLOAD and LPOT Turbine Speed	5-42
5.15	Upper Tail Comparison for OPB Discharge Temperature	5-44
5.16	Upper Tail Comparison for HPOT Discharge Temperature	5-45
5.17	Test Data, Flight Data and ANLOAD Comparison for Fuel Flow	5-47
5.18	Flight Data and ANLOAD Comparison for Fuel Flow	5-48
5.19	Test Data, Flight Data and ANLOAD Comparison for LOX Flow	5-49
5.20	Flight Data and ANLOAD Comparison for LOX Flow	5-50
5.21	OPB Discharge Temperature Validation Using Flight/Test Data	5-51
5.22	OPB Discharge Temperature Validation Using Flight Data	5-52
5.23	HPOT Discharge Temperature Validation Using Flight/Test Data	5-53
5.24	HPOT Discharge Temperature Validation Using Flight Data	5-54
5.25	LPOT Turbine Speed Validation Using Flight/Test Data	5-55
5.26	LPOT Turbine Speed Validation Using Flight Data	5-56
6.1	LDEPXT: Load Expert System	6-3
6.2	Load Expert System Load Model Knowledge Base	6-10
6.3	Load Expert System Load Knowledge Base	6-11
6.4	Independent Loads Database	6-12
6.5	LDEP: Dependent Load Database	6-13
6.6	INFC: Influence Coefficient Database for LIDP-ID=2	6-16
6.7	Schematic of PSD Curve from Which Various Constants Need	
	to be Determined	6-29
6.8	Comparison of Prediction and Actual Data at Location XUTDEKT	6-30
6.9	Both Initial and Geometric Factor Predictions are Shown	6-31

## TABLES

		Page
2.1	Composite Load Spectra Scope of the Load Knowledge Base	2-7
3.1	Classification of Data Available for Use in Probabilistic Load Determination	3-8
4.1	SSME Table of Influence Coefficients	4-5
4.2	SSME Engine Influence Coefficient Dependent Parameters for CLS	4-6
4.3	SSME Engine Model Random Variables	4-7
4.4	Engine Influence Model Independent Loads	4-14
4.5	Engine Influence Model Dependent Loads	4-16
5.1	Mean and Variance of Random Variables for Verification Studies	5-23
5.2	Engine Variables Included in the Validation Studies	5-33
5.3	Test Data Used in Verification Studies	5-34
5.4	Flight Data in Verification Studies	5-35
5.5	Independent Engine Variable PDF Parameters	5-42
5.6	Calculated and Predicated Average Values for Engine Analyses	5-43

#### 1.0 INTRODUCTION

#### 1.1 <u>General</u>

Requirements for better performance have pushed engine designs to lighter weight systems, higher pressures, and more severe temperature environments. Temperatures, external and internal fluids flow noise, and mechanical vibration levels have increased markedly and have been shown to limit hardware designs. Advanced engine concepts and designs are enough different so that the loads cannot be simply scaled from other engines.

The use of engine cycles, such as staged combustion on the space shuttle main engine (SSME), result in engine operating pressures in the 3000 to 7000 psi regime. High performance turbomachinery operates in the 30,000 to 100,000 RPM regime. These operational requirements result in complex high energy loading throughout the engine. The difficulty in installation, the burden in cost and the potential for destroying an engine have severely limited required instrumentation and measurements to adequately define loads of key components, such as turbine blades. Also, accurate analytical methodologies for defining internal flow-related loads are just emerging for problems typically found in rocket engines. The difficulty of obtaining measured data and verified analysis methodologies has led to the probabilistic load definition approach of this contract.

Current loads analyses methodologies are driven by their usage in deterministic analysis methods. This includes strength and fatigue analysis as well as mechanical vibration. The deterministic solution typically uses an upper bound approach where maximum loads and minimum properties are used. For critical hardware, a separate sensitivity study is often made to determine nominal operation and which of the loads and their variations govern the hardware design. Quantification of the actual variations and their frequency of occurrence is a crucial weakness.

The Composite Load Spectra (CLS) contract and the associated Probabilistic Structural Analysis Method (PSAM) contract from Lewis Research Center are developing an integrated probabilistic approach to the structural problem. The probabilistic loads approach has the ability to quantify knowledge more technically relative to the loads. The use of mean values and distributions of engine loads, rather than maximum or enveloped loads, can add greatly to the understanding of normal engine operation while furnishing good or better knowledge of maximum conditions.

Present techniques often result in manufacturing of components that, in many cases, greatly exceed design requirements; however, there is no way of assessing this margin for extending the useful life margin. Thus, to formulate more effective designs, it is necessary that loads on components of rocket engines be derived so that they can be applied by probabilistic analysis methods such as PSAM. More effective designs will result in more accurate methods reflecting the true risk. An assessment would be much easier to perform if a probabilistic analysis and associated risk assessment were available.

This project will provide methods to combine technologies of analytical (deterministic) loads and probabilistic modeling. Since these methods will be developed from a generic approach, they will be applicable to current or advanced liquid rocket engine designs.

#### 1.2 Project Objective

The objective of this program is to develop generic load models. Multiple levels of progressive sophistication will simulate the CLS induced in space propulsion system components and will be representative of SSME, such as transfer ducts, turbine blades and liquid oxygen (LOX) posts. These models will be developed using two independent approaches. The first approach consists of describing CLS simulation, using state-of-the-art probabilistic methods to describe the individual loading conditions and combinations of these loading conditions to synthesize the CLS.

The second approach consists of developing coupled models for CLS simulation which combine (deterministic) models for composite load dynamic, acoustic, high-pressure and high rotational speed, etc., load simulation using statistically varying coefficients. These coefficients will then be determined using advanced probabilistic simulation methods with and without strategically selected experimental data. The first approach effort has been completed and work on the second approach started.

The unified theory required to combine various individual load simulation models (hot-gas dynamic, vibrations, instantaneous-position, centrifugal field, etc.) into CLS simulation models will be developed under this program. Results obtained from tests models will be compared with available numerical results with the loads induced by individual load simulation models. Results will also be obtained with available structural analysis results from independent analyses and tests. These theories, developed under both approaches, will be further validated with respect to level of sophistication and relative to predictive reliability and attendant level of confidence.

A computer code incorporating the various individual and CLS models will be developed to construct the specific load model desired. The approach is to develop and deliver the computer code at intervals in the contract. The first version was an initial code for turbine blade loading. Subsequent code versions have added sophistication to the component probabilistic load definition and the decision making processes, as well as installing a new set of loads for an additional component. This allows for ongoing evaluation and usage of the system by Rocketdyne and NASA.

#### 2.0 SUMMARY

The development of the CLS is a 4-year base program and a 2-year option program. Rocketdyne is the prime contractor and is responsible for the overall Battelle Columbus Laboratories (BCL) is the major subcontractor for project. developing the probabilistic methods and related tasks. The effort is divided into three tasks: probabilistic method and load model development, loadexpert system development; and code validation and verification. The CLS base program is essentially complete. Since January 1989, the option program is carrying out. There is no clear-cut separation between the base program and the option program. The option program is really a natural extension of development work from the base program. This final report presents the accomplishments of the CLS efforts during the last 4 years. It summarizes experiences gained during the base program efforts, details the status of the CLS code, and presents some perspectives of the program and its future direction.

The SSME is being used as a baseline model for defining the loads and requirements. The SSME configuration of the four components studied are shown in Figures 2.1 and 2.2. Figure 2.1 is a cross section of the SSME powerhead showing typical LOX posts in the three combustors (two preburners and a main injector), transfer ducts between the turbines, and the main injector and turbine blades. Figure 2.2 shows the HPOTP discharge duct in an overall SSME powerhead view. This duct was chosen as the fourth component because of its history of fluid vibration-related problems.

During the base program, a probabilistic multilevel engine model was developed. The SSME is being used as a baseline model; however, the engine model implemented on the CLS program is generic. The multilevel engine model is composed of the engine system influence model and various component load models as shown in Figure 2.3. The engine system influence model is the foundation of the multilevel engine model which allows various component load models to be built on it. The engine system model evaluates system performance variables and engine subsystem operation loads. Both load types are

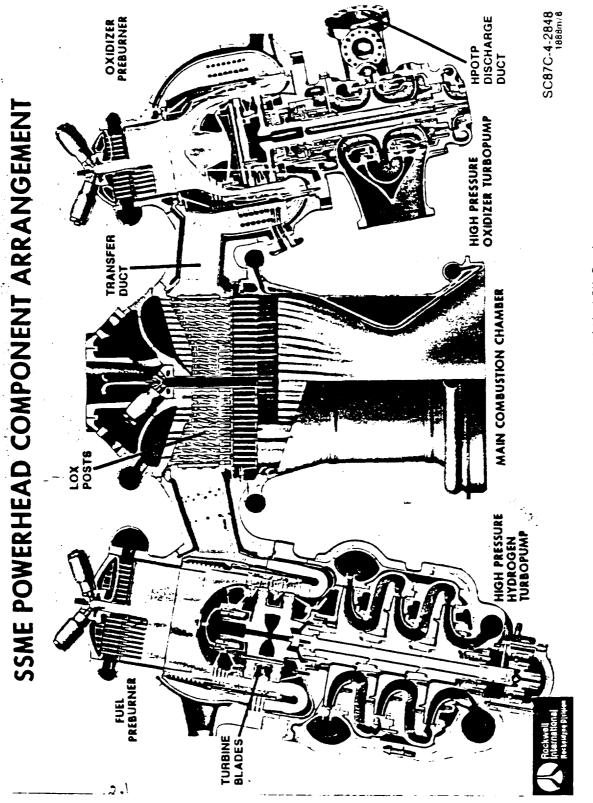


Figure 2.1. SSME Powerhead With LOX Posts, Transfer Ducts and Turbine Blades Identified

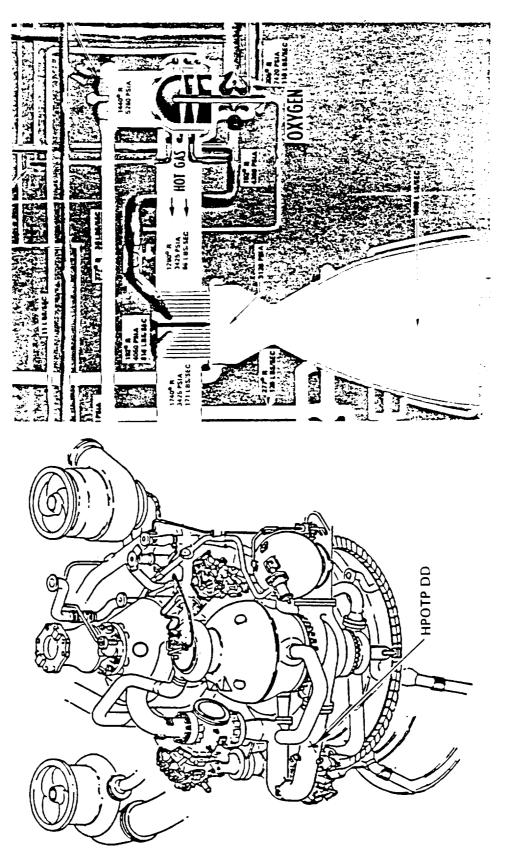


Figure 2.2. SSME HPOTP Discharge Duct

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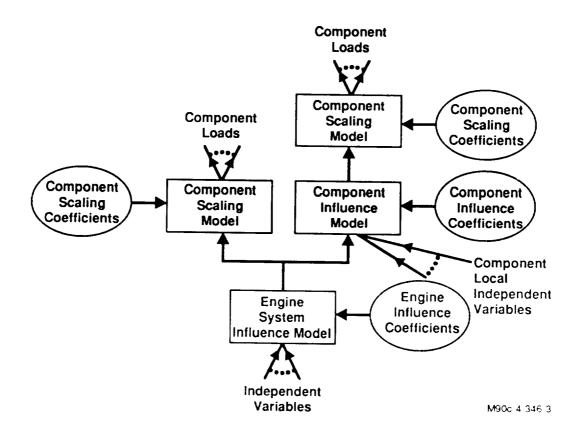


Figure 2.3. Multi-Level Engine Model

classified as system dependent loads from now on as a convenient convention. The evaluation is based on the engine operating power level, engine hardware, and operating parameters. Engine hardware and operating parameters are classified as system-independent loads from now on. The load definitions will be defined in the next section.

Component load models evaluate loads local to a component (classified as component loads) using system loads as the component boundary loads (subsystem interface operating loads).

The base program engine system influence model, which is implemented into the probabilistic load model, has 23 independent loads and 62 dependent loads. The load selection was developed mainly for the purpose of engine performance

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evaluation. Independent loads do not include most engine hardware parameters. When this model was employed to calculate dependent loads, the load distribution results (mainly the load variation) did not compare well with the 10-second average load database data. Investigation indicates that the engine-to-engine variation was not included in the engine system model. This variation is contributed mainly from engine hardware variations as a result of different manufacturing processes used by different manufacturers and different environmental conditions during the manufacturing process. This pointed out a need for an expanded engine system influence model. As a result of this investigation, an expanded list of independent loads and dependent loads were identified. The lists include 64 independent loads and 99 dependent Joads. A request was made to the engine performance group for a new influence coefficient set for the expanded list of loads. The new influence coefficient set has been generated and is planned to be implemented during the option program of this contract.

The probabilistic methods were surveyed and three methods were selected to be implemented in the CLS code. The three probabilistic methods selected are (1) the Gaussian moment method, (2) the random sampling condensation algorithm (RASCAL) method, and (3) the Monte Carlo method.

The Gaussian moment method assumes all random variables are normally distributed. The variation of a combined load is evaluated, based on Gaussian algebra. This method is best used for a quick evaluation or sensitivity study.

The RASCAL method is a variance of the discrete probability distribution (DPD) method. It is versatile in that it can handle almost all types of distribution, even those without closed forms. It is efficient if very high accuracy is not required.

The Monte Carlo method is the most powerful method because it can be applied to any situation. The conventional wisdom is that the Monte Carlo method is computational-expansive and inefficient; however, with available high speed computers, this is probably not a factor. If high accuracy is required, the Monte Carlo method is probably the best way to solve the problem. The three methods were implemented to the engine system influence model. RASCAL was chosen to be the principal method as most component load models were implemented with the method. Validation of RASCAL has been performed. High accuracy comparable to the Monte Carlo method can be obtained if a large enough bin size is used. But then the efficiency advantage of RASCAL is lost.

Generic probabilistic models were developed and implemented for load calculations using the probabilistic methods discussed above. Each engine mission, either a real flight or a test, has three mission phases: the engine start transient phase, the steady state phase, and the engine cut off transient phase. Power level and engine operating inlet conditions change during a mission. The load calculation module provides the steady-state and quasisteady state calculation procedures with duty-cycle-data option. The quasisteady state procedure is for engine transient phase calculations. In addition, a few generic probabilistic load models were also developed for specific conditions. These include the fixed transient spike model, the poison arrival transient spike model, and the rare event model. These generic probabilistic load models are valuable tools for simulating loads with specific conditions. They were implemented in place. However, more study and development is required to build sufficient knowledge base and database to facilitate general usage. As it stands now, only experts with full knowledge of the loads to be simulated can use these models to synthesize desired loads with the specific conditions.

Four SSME components, turbine blades, transfer ducts, LOX post, and the high pressure oxidizer turbopump (HPOTP) discharge duct were selected for application of the CLS program. The loads for these four components provide a fairly complete picture of loads for the SSME. Loads developed for the four components are listed in Table 2.1. They include static pressure loads and dynamic pressure loads for all four components, centrifugal force for the turbine blade, temperatures or thermal loads for all four components, and structural vibration loads for the ducts and LOX posts (ref. 2.1).

Individual Load	Turbine Load	Transfer Duct	LOX Post	HPOTPDD
Static pressure	X	X	Х	X
Dynamic pressure				
Turbulence				
Sinusoidal (repeated pulse)	x	_	-	-
Random	-	X	X	X
Centrifugal	X	-	-	-
Temperature	X	X	X	X
Structural vibration				
Transient	-	X	X	X
Steady-state	-	X	X	X

#### Table 2.1. Composite Load Spectra Scope of the Load Knowledge Base

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The probabilistic load development has proceeded in parallel with the load definition work. The goal is to address generic engines that may include different mission profiles or incorporate design changes. This will require that a robust and general probabilistic approach be adopted for inclusion in the expert system. Generic component load models were developed to synthesize probabilistic loads of components. In the CLS load expert system, the generic static pressure scaling model, the generic probabilistic thermal load model, and the generic fluctuation pressure (dynamic pressure load for ducts and LOX posts) load model were implemented. With appropriate database, the generic load models will provide the correct loads for each component. The sinusoidal dynamic pressure load for turbine blades is unique and a dedicated turbine-blade dynamic-pressure model was implemented for it. There is a vibration model in place. More development and improvement of the vibration model is required for any real applications.

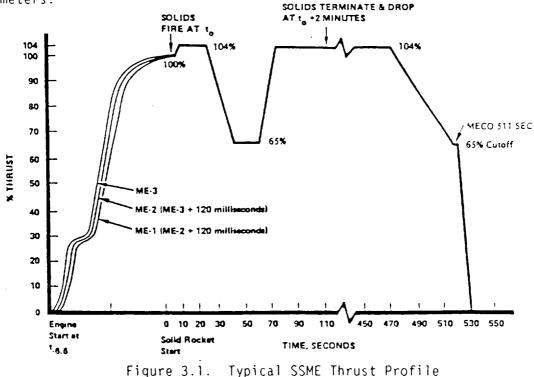
Probabilistic load models were integrated into a load-expert system. The primary function of the load-expert system is to provide a development environment for integrating the load knowledge domain with the probabilistic models. Advantages of an expert system environment for the CLS program are that it facilitates incremental development of the probabilistic load models especially for building generic models, provides a better knowledge representation, avoids data and knowledge redundancy, and provides a friendly user interface for interactive computing.

The intensive computation requirement for load modeling and the nonproprietary requirement dictated that the expert system program be developed in-house and in FORTRAN language so that it could be easily integrated with the FORTRAN routines developed for probabilistic methods and load models. The philosophy is to learn from the experiences gained by artificial intelligence (AI) pioneers and to make the system simple and efficient. As Feigenhaum (ref. 2.2) put it, "knowledge is power." The goal is to put all the knowledge together in a suitable representation which can be utilized efficiently by the load calculation module. Based on this philosophy, the CLS program employs a decision tree inferencing scheme chosen for its simplicity and efficiency coupled with a database system for data management. The engineering data is handled by the database system. The data processing and load modeling were hardwired into decision tree rule modules. The process control and gueries are handled by the expert system. With this simple structure, the expert system achieves its goal of providing a convenient way of retrieving load information to users, performing simple calculations using different load models, and preparing input file for a full-blown load calculation.

#### 3.0 SSME OVERVIEW

The orbiter vehicle main propulsion system includes three SSMEs. An SSME is a reusable, high-performance, liquid-propellant rocket engine with variable thrust. All three SSMEs are ignited on the ground at launch, operating in parallel with solid rocket boosters during the initial ascent phase, and continuing to operate for approximately 550 seconds during total firing duration. Each engine operates at a mixture ratio (liquid oxygen/liquid hydrogen) of 6:1 and a chamber pressure of approximately 3,000 psia to produce a sea level thrust of 375,000 pounds and a vacuum thrust of 470,000 pounds. The engines are throttleable over a thrust range of 65 to 109% of the rated power level. This provides a higher thrust level during lift-off and the initial ascent phase, and allows orbiter acceleration to be limited to 3 g during the final ascent phase.

A typical flight profile is shown in Figure 3.1. This basic profile is characteristic of a majority of the pressure, flow, and pump characteristic parameters.



A brief description of the engine operation and propellant flow schematic is provided in order to furnish an overall perspective of the engine and its loads. Figure 3.2 is a simplified flow schematic where main engine components and flows are shown.

A description of the start sequence follows.

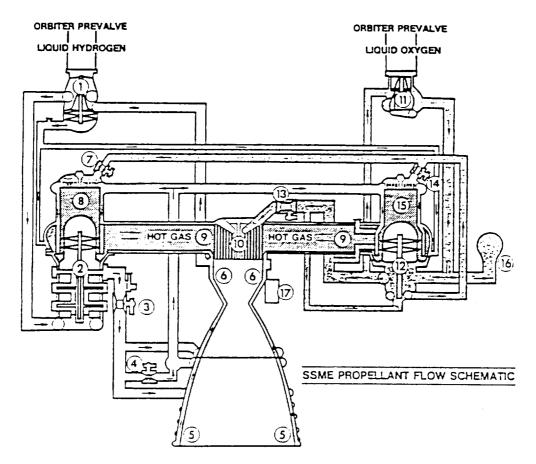


Figure 3.2. SSME Propellant Flow Schematic

#### Components

- 1. Low Pressure Fuel Turbopump
- 2. High Pressure Fuel Turbopump
- 3. Main Fuel Valve
- 4. Chamber Coolant Control Valve
- 5. Nozzle
- 6. Main Combustion Chamber
- 7. Fuel Preburner Oxidizer Valve
- 8. Fuel Preburner (LOX Posts)
- 9. Hot Gas Manifold (& Transfer
  - Tubes

- 10. Main Injector (LOX Posts)
- 11. Low Pressure Oxidizer T/P
- 12. High Pressure Oxidizer T/P
- 13. Main Oxidizer Valve
- 14. Oxid. Preburner Control Valve
- 15. Oxidizer Preburner
- 16. Pogo Suppressor
- 17. Controller

The flow of liquid hydrogen (or fuel) and liquid oxygen (or oxidizer) from the space shuttle external tank is restrained from entering the engine by prevalves (or isolation valves) located in the orbiter above the low pressure turbopumps (1 and 11). Approximately 1 hour prior to firing, the prevalves are opened to allow propellants to flow through the low pressure turbopumps (1 and 11), and through the high pressure turbopumps (2 and 12), and then to the main propellant valves (3 and 13). On the liquid oxygen side, the system also fills two preburner valves (7 and 14). The cryogenic propellants are held in ducts for sufficient time to chill the engine and attain liquid conditions in the respective propellant systems. The chill process is aided by bleedlines to remove gaseous propellants as they are formed.

In the start sequence, hydrogen and oxygen sides operate almost simultaneously. The hydrogen (or fuel) side is explained first.

Upon receipt of the ignition command from the orbiter, the main fuel valve (3) is opened. This permits hydrogen to flow into the coolant loop, through nozzle tubes (5), and through channels in the main combustion chamber (6). Part of this coolant loop flow is diverted by the coolant control valve (4) to the preburners (8 and 15) for combustion and cooling of the preburner walls. Some of the hydrogen used in the coolant loop is warmed in the process to virtually ambient conditions and is tapped off at the main combustion chamber (6) for routing back to the low pressure turbopump (1) to drive the turbine for that pump. This flow passes through the turbine and is returned to the walls of the hot gas manifold (9) and the main injector (10) to provide cooling.

On the oxygen (or oxidizer) side, the ignition command opens the main oxidizer valve (13). The liquid oxygen flows through the two turbopumps (11 and 12) to the main injector (10) and also (through valves at 7 and 14) to the two preburners (8 and 15). Oxygen, tapped off downstream of the high pressure oxidizer turbopump (12), is routed to the low pressure turbopump (11) and to serve as the turbine-drive fluid for that pump. This flow continues through the low pressure oxidizer turbopump (11), thus re-entering the circuit. Spark igniters located in the dome of both preburners (8 and 15) and the main chamber (10) initiate combustion.

After the engine is signaled to start, the initial combustion occurs in the There are two preburners: one provides power to the highpreburners. pressure fuel turbomachinery (8), and the other provides power to high pressure oxidizer turbomachinery (15). Proper sequencing of these two preburners allows the engine to start repeatedly regardless of engine inlet conditions. Each of the two preburners operates at a low mixture ratio of less than one part oxygen to hydrogen to produce hot gas (or hydrogen-rich steam) to provide low-temperature gases for turbomachinery operation. Each temperature can be varied by moving a single valve. The two preburners thus provide a convenient method for controlling engine thrust and mixture ratio. The preburners operate over a broad range of pressure and temperature to achieve a full range of engine operating conditions.

As the fuel-rich gases leave the preburners, they immediately enter highpressure turbomachinery. The gases are expanded in a turbine and the expansion reduces the temperature. After the gases leave the turbomachinery, they enter the hot-gas manifold. This manifold transports and distributes the gases to the main injector. The hot-gas manifold serves multiple functions. It supports the two preburners and two high-pressure turbopumps, and also forms a portion of the thrust chamber structure. The compactness of the hotgas manifold allows the powerhead diameter to be minimized, and its orientation permits access for the removal and inspection of turbomachinery and preburners.

After the gases are routed through the hot-gas manifold, they enter the thrust chamber. The thrust chamber consists of three major parts: the main injector (10), the main combustion chamber (6), and the nozzle (5).

Fuel-rich gases from the hot gas manifold enter the thrust chamber through the injector and are distributed in the injector. Liquid oxygen from the high pressure oxidizer turbopump (2) enters at the top of the injector, is uni-formly distributed within the oxidizer dome. The oxygen then enters the

center tube of each of the injector coaxial elements. The fuel-rich hot gas enters the large annular tube of the coaxial element. The coaxial elements are designed and optimized so that the hot gas, plus the oxygen, is uniformly distributed throughout the combustion chamber. This is achieved by proper matching of gas and oxygen velocities and uniform spacing of elements across the injector face. A portion of the injector elements is extended into the combustion chamber to form acoustic baffles. These elements, quite similar to those used on the injector face, inject hydrogen and oxygen at the same mixture ratio as the elements on the injector face and maintain uniform distribution and high performance.

Propellants injected into the main chamber are combusted rapidly at a mixture ratio of six parts of oxygen to one part hydrogen. The gases are accelerated to sonic velocity and supersonically expanded in the aft portion of the main combustion chamber and the nozzle.

There is a standard set of engine measurements that are taken on each SSME engine ground test that is used for calculating engine performance, measuring critical levels of vibration, temperature, etc. for engine redlines and measuring general engine operation. A subset of the information applicable to the CLS contract (Figure 3.3) includes measured data related to LOX posts, turbine blades and transfer ducts. Most of the measurements are low frequency digital data. The accelerometer data are all high frequency analog measurements.

Figure 3.4 shows the standard flow of engine test data processing on the SSME. For low frequency data, the information is processed through a data reduction code and either plotted as the variable versus time or further processed to obtain steady-state performance calculations that include both measured and calculated flows, temperatures, pressures, torques, speeds, power level, etc. The analog data passes through a high frequency data processing facility and produces a series of standard plots. These data are all reviewed prior to the next test firing of the engine and are also collected in various databases for later use and review. Data tapes are saved from all engine tests and information is recoverable at any time.

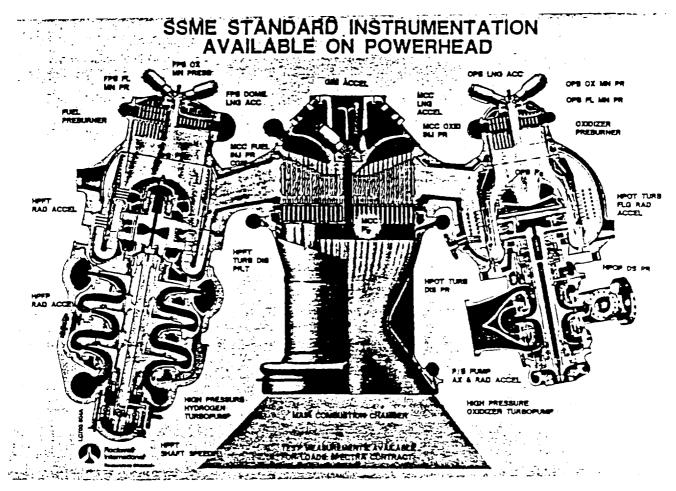


Figure 3.3. SSME Standard Instrumentation Available on Powerhead

The right side of Figure 3.4 depicts the interrelationship of the engine performance model and the engine data analysis. The engine data reduction model and the performance model are essentially the same code. For data analysis, engine measurements are used as input variables. For the performance model, design conditions are used for the input variables. Based on empirical measurements on more than 1000 engine tests, coefficients for these models have been adjusted. The influence conditions or coefficients and nominals are a set of equations with coefficients that are varied as a function of power level to accurately represent the results of the performance model at specific power levels between 65 and 109% power level. Influence coefficients and nominals are a cost effective method of determining engine parameters for a limited set of independent and dependent variables.

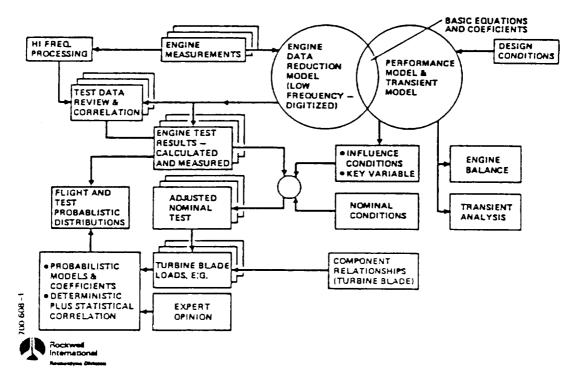


Figure 3.4. Data Analysis

The engine measurements form the best ready database for developing probabilistic loads. Since they are all time-phased, it is a convenient method for obtaining some of the combined load effects. In the development of the individual loads, key variables (e.g., power level, torques, and flow rates) are available to aid in developing correlations in order that generic loads can later be scaled using these parameters.

Table 3.1 summarizes and classifies an overall perspective of where information is obtained for detail analysis of components. The first two items relate to the direct engine measurements and analysis discussed above.

The engine balance and engine transient model have similar simulation codes for modeling engine components. The engine balance model furnishes higher accuracy steady-state quantities, whereas the transient model depicts a full range of engine test conditions. Both models project standard engine or typical engine operating conditions. Engine test results are not directly

# Table 3.1. Classification of Data Available for Use in Probabilistic Load Determination

Data/Analysis	Availability	Examples
<ol> <li>Engine test measurements</li> <li>Low frequency (digital)</li> <li>Hi frequency (FM tape)</li> </ol>	<ul> <li>Every engine test</li> <li>Various types of processed data and records</li> </ul>	<ul> <li>Turbine discharge temp, P<sub>c</sub>,</li> <li>Turbopump or injector accelerometers</li> </ul>
<ul> <li>2) Engine test calculated variables</li> <li>Low freq (digital)</li> <li>Steady state only <ol> <li>sec, 3 sec,</li> <li>sec avg</li> </ol> </li> <li>Major component level</li> </ul>	• Every engine test	• Pump torque, flow rates
<ul> <li>3) Engine transient simulation model</li> <li>Low frequency digital analysis</li> <li>Major component level</li> </ul>	<ul> <li>Specific simulations for understanding start and cutoff</li> <li>Not test specific, but correlated to test results</li> </ul>	<ul> <li>Engine valving and sequencing o overall engine start and cutoff</li> <li>Major component variables</li> </ul>
<ul> <li>Engine balance model</li> <li>Steady state analysis</li> <li>Specific operating conditions</li> <li>Nominals, max, mins</li> </ul>	<ul> <li>Specific engine operation conditions</li> </ul>	<ul> <li>RPL, FPL, 111% and other power levels</li> <li>Various engine configurations</li> <li>Major component variables</li> </ul>
<ul> <li>5 Shock and Vibration environments</li> <li>Design and test environments</li> </ul>	<ul> <li>Specific zones on engine</li> <li>Expected max conditions</li> <li>Different thrust level and engine configurations</li> <li>Historical database for engine</li> </ul>	<ul> <li>Zone A. main combustion champed zone</li> <li>Zone E, fuel preburner</li> </ul>
ó) Special measurements	<ul> <li>Limited database</li> <li>Critical hardware</li> <li>Few measurement</li> <li>Difficult to obtain</li> </ul>	<ul> <li>Instrumented turbooumps</li> <li>Structural and vibration twots</li> <li>Instrumented injector         <ul> <li>SWHGM cold flow</li> <li>Engine 0110 tests</li> </ul> </li> </ul>
<ul> <li>7: Individual component analysis</li> <li>Steady state basis <ul> <li>Engine balance conditions</li> <li>Vibration environ- ment</li> </ul> </li> <li>Transient analysis <ul> <li>Engine transient</li> <li>Shock environment</li> </ul> </li> <li>Expert opinion</li> </ul>	<ul> <li>Some information for all components</li> <li>Level of detail dependent on - criticality of component, accuracy of model and knowledge of loads</li> <li>Steady state primarily</li> <li>Limited duty cycle analysis</li> <li>Limited engine and lab test measurements</li> </ul>	<ul> <li>LOX post</li> <li>Turbine blades</li> <li>Transfer ducts</li> </ul>

used as input, but are used as correlation data to compare with engine testing. In general, the engine balance data, and to a lesser extent engine transient simulation model results, are used for component analysis.

Structural vibration loads are based on shock and vibration environment definitions rather than on individual engine measurements.

Detailed structural analyses are usually based on limited or maximum conditions that occur within the load duty cycle of the component rather than a detailed time-dependent analysis of a mission history profile. Most of the available loads are not readily available in the proper format.

The following figures and discussion are furnished to give a perspective of the form of the available engine data and some of its characteristics. Figure 3.5 is the data processed by Rocketdyne for the fuel preburner chamber pressure (FPB Pc) during a typical test. This trace mirrors the thrust profile trace in Figure 3.6. Since pressure and temperature changes at engine propellant inlets affect engine performance, the thrust profile trace also notates when venting of run tanks occurs in tests.

High frequency sample data processing examples include AMS, PSD, ISOPLOTS, Tracking Filter and STATOS. Figure 3.7 shows the power level profile of a test. This test was chosen since it varies the power level in 1% decrements from 109% to 90%. Each step has a steady-state response of 3 sec. This incremental change is easily noted in the high pressure fuel pump speed profile in Figure 3.8. Figure 3.9 is a typical AMS plot that furnishes a composite level squared time history of the variables noted. These traces show transient effects during start and cutoff, as well as the variation caused by changes in steady-state power level. Figure 3.10 is a power level spectral density (PSD) plot of a selected time interval of the test (14 to 24 seconds from start). The variable is the fuel preburner longitudinal acceleration. This plot shows the HPFTP sinusoidal harmonics at 12N, 18N, 24N and 30N that stand out above the average RMS level of the signal. Also, the HPOTP sinusoidal harmonic at 16N is annotated. The same HPFTP sinusoidal frequencies are easily seen on the ISOPLOT in Figure 3.11. Since they are pump-speed dependent, the ISOPLOT also shows how these harmonics drop off as the power level is decreased from 109%.

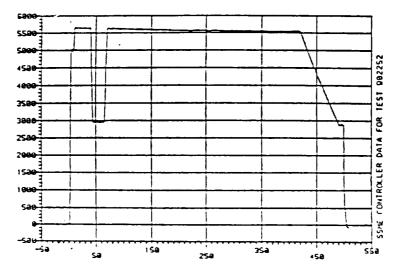


Figure 3.5. Time from Engine Start, Seconds

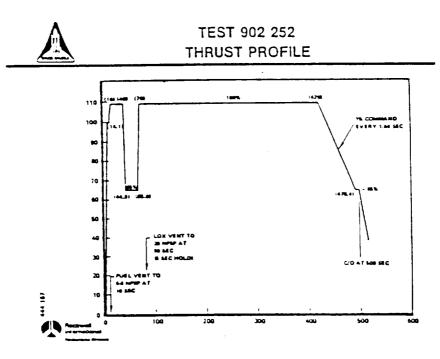


Figure 3.6. Thrust Profile

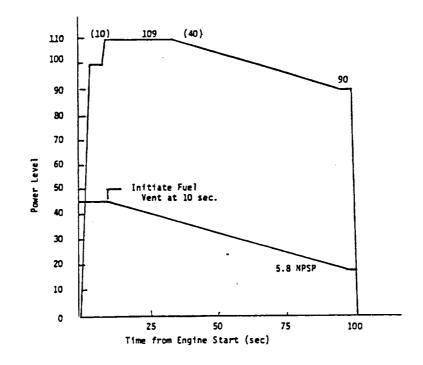


Figure 3.7. Pump Signature Test

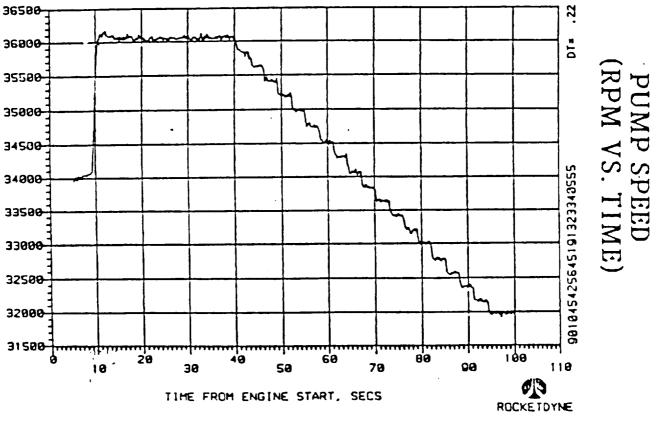


Figure 3.8. High Pressure Fuel Pump Speed

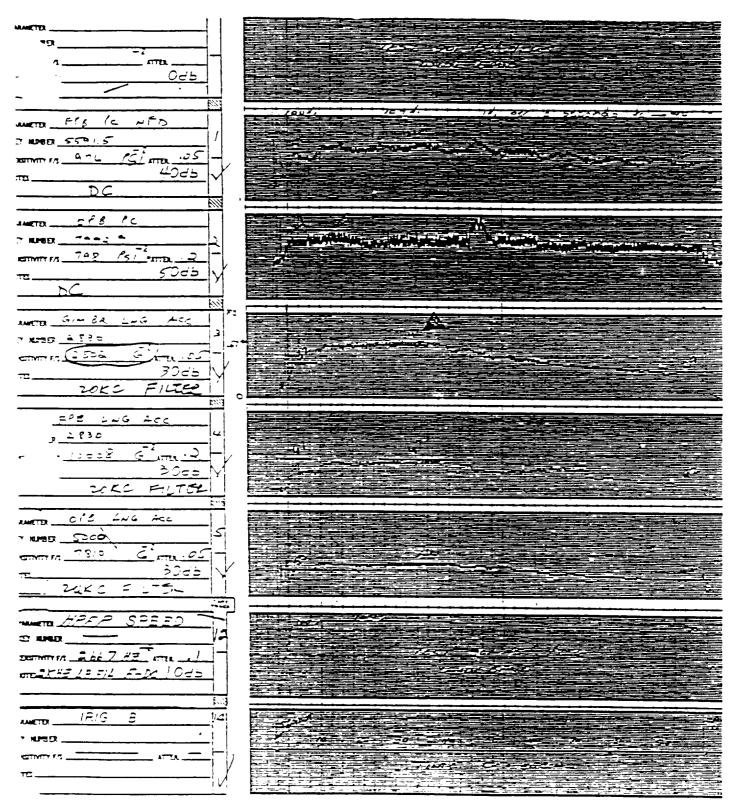
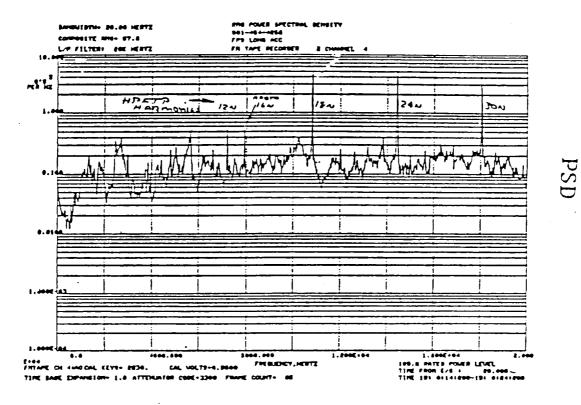


Figure 3.9. AMS Fuel Preburner Pc



FUEL PREBURNER LONGITUDINAL ACCELEROMETER PDS

Figure 3.10. PSD Fuel Preburner Longitudinal Accel.

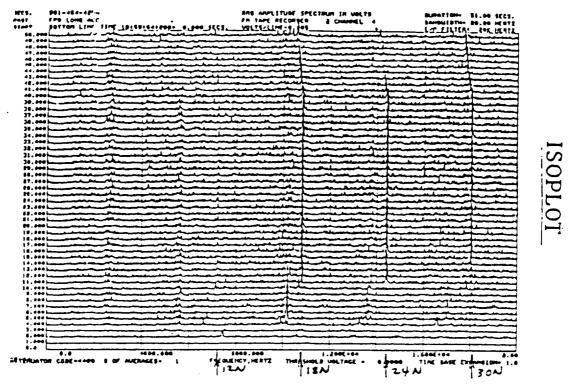


Figure 3.11. Isoplot Fuel Preburner Longitudinal Accel.

The PSD shown demonstrates that high frequency inputs from both pumps are carried through the powerhead and drive the fuel preburner accels. Similar responses are found in the main injector accelerometers.

The STATOS record (Figure 3.12) is included to show that the accelerometer response is such a wide spectrum that the special (standard) processing shown in the previous figures is required to gain intelligent information from the data.

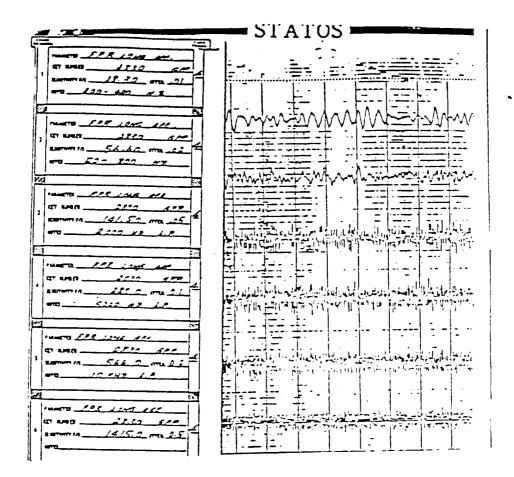


Figure 3.12. Statos Record

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#### 4.0 ENGINE LOADS AND CLS ENGINE LOAD MODELS

#### 4.1 <u>Background</u>

Individual loads applicable to the four components in this project are summarized in Table 2.1. Those loads cover a major portion of the loading throughout a rocket engine and are an excellent representative set to develop into an engine loads expert system. Where applicable, individual loads are modeled for the entire duty cycle.

The loads are essentially self-generated or self-induced loads except for steady-state g-forces and gimbaling requirements during flight. This allows the engines to be readily separated from the vehicle loads analysis as a subsystem with specific requirements.

The vehicle design can be divided into conceptual, preliminary, detail, and design verification phases. This is followed by flight support and possible uprating and problem resolutions. During the conceptual and preliminary design phases of a vehicle, major decisions are reached that spawn requirements for engine design. Vehicle requirements often are related to load alleviation or preventative measures and performance requirements to optimize vehicle design with engine design. Examples include: (1) controlled thrust rise rate, (2) in-flight load alleviation, (3) cutoff impulse requirements, (4) engine inlet operating pressures and temperatures, and engine gimbal angle and rate requirements. A description of the approach to deriving the loads design criteria for the space shuttle and its payload is given in Reference 4.1. The vehicle system requirements reduce to a set of engine loads and system requirements (ref. 4.2) that define limits and engine duty cycles that end up defining a part of the engine individual and composite loads. (Note: most examples in the discussion presented herein are related to the SSME, but they are also appropriate for generic rocket engines.)

The basic engine duty cycle is controlled by engine thrust buildup limits (Figure 4.1) engine thrust decay limits (Figure 4.2) and overall flight requirements such as maximum operational power, throttling during maximum dynamic loads, and throttling near the end of flight to maintain a maximum g-load limit (Figure 4.3). These and other engine requirements are used to develop engine configurations and design.

#### 4.2 <u>SSME Deterministic Engine Model</u>

Deterministic models of varying complexity are used in all analysis efforts to evaluate engine performance, engine operating conditions, and component operating loads. The steady-state engine simulation model, i.e., the engine performance model relates engine operating parameters and inlet conditions to engine system performance parameters and engine subsystem operation conditions. The engine performance model is a fairly complex system. Trend charts for engine parameters and pump curves as functions of power level are used in the model to anchor experimental and test data. Engine hardware parameters are calibrated for each engine so that the model evaluation of measured loads agrees with measurements. This, in turn, produces accurate performance evaluation and other unmeasured subsystem operating loads.

To facilitate the engine performance evaluation and prediction, a production influence coefficient model has been developed by the Engine Performance Analysis group at Rocketdyne. The model uses some 20 independent operating parameters and inlet conditions to calculate system-dependent variables used to assess engine performance. Engine operating parameters and inlet conditions are classified as engine-direct variables. The 23 engine-direct variables, listed in Table 4.1, include propellant inlet temperatures and pressures, line resistance changes due to gimbaling, and tank repressurization flow settings. Engine system performance parameters and engine subsystem operating conditions are classified as the system-dependent loads listed in Table 4.2. Based on the evaluation of the engine performance model, the influence coefficients were obtained. To account for an as-built engine condition, tag values are used for engine subsystem operating conditions as the

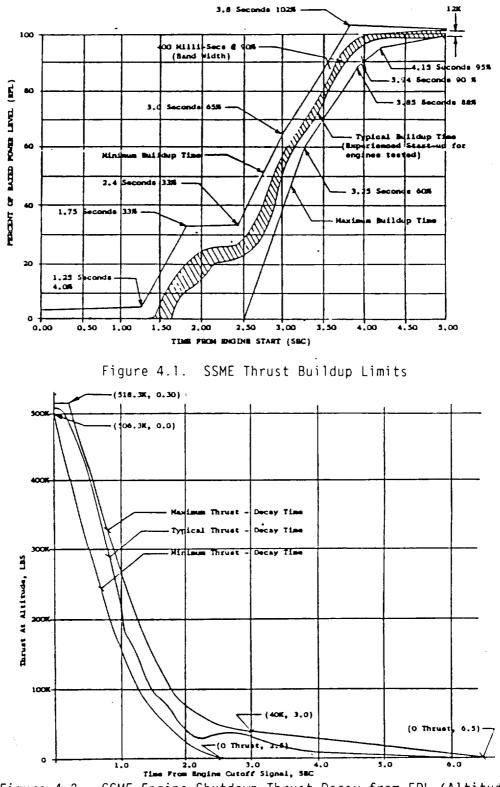


Figure 4.2. SSME Engine Shutdown Thrust Decay from FPL (Altitude)

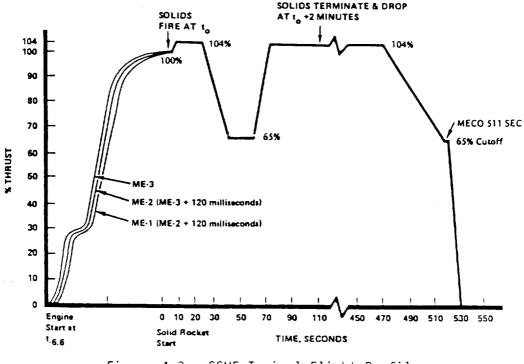


Figure 4.3. SSME Typical Flight Profile

nominal values of the engine. Tag values are obtained by adjusting 41 random variables relating to engine hardware parameters in the engine performance model such that measured variables match measurements from the acceptance tests of the engine. The deterministic adjustment removes the engine-to-engine variation and allows the engine influence coefficient model to accurately predict the engine performance.

It is known that engine-to-engine variations, due to manufacturing and other environmental conditions, are significant. A list of 46 random variables listed in Table 4.3 was developed to account for variations in hardware. The variations were based on consultations with component experts to define how much each item was expected to vary from a manufacturing, performance, or test-to-test basis. The performance unit then combined these variations with design requirements and knowledge of past engine performance to develop a set of variances for the random variables. The combined effect of these variables

Table 4.1.	SSME	Table	of	Influence	Coefficients
------------	------	-------	----	-----------	--------------

	Independent Parameter	Nominal Value
1	Commanded mixture ratio	6.0000
2	Fuel inlet total pressure (psia)	30.0000
3	Oxidizer inlet total pressure (psia)	100.0000
4	Fuel inlet temperature (R)	37.0000
5	Oxidizer inlet temperature (R)	164.0000
6	HPFTP turbine efficiency multiplier	1.0090
7	HPFTP turbine flow multiplier	1.0125
8	HPOTP turbine efficiency multiplier	1.0152
9	HPOTP turbine flow multiplier	0.9741
10	T/C characteristic velocity multiplier (C*)	1.0004
11	Main fuel valve resistance	0.0138
12	Main oxidizer valve resistance	0.0107
13	Coolant control valve resistance	-1.942890E-16
		1.000000E+00
		0.00000E+00
14		0.00000E+00
14	FPB fuel injector resistance	0.1550
15	OPB fuel injector resistance	0.6850
16	LPFTP turbine inlet orifice resistance	0.7160
17	LPFTP turbine nozzle area (in <sup>2</sup> )	0.9500
18	Oxidizer pressurant flowrate (lb/sec)	3.666887E+01
		-9.966946E+01
		9.016788E+01
10		-2.711157E+01
19	Fuel pressurant flowrate (lb/sec)	1.676685E-01
		1.764161E+00
		-3.111869E-01
20		0.00000E+00
20	LPOTP Pump cavitation correction	1.0000
21	LPOTP Pump cavitation correction	1.0000
22 23	LPOTP Pump cavitation correction	1.0000
23	LPOTP Pump cavitation correction	1.0000
Rem	arks: A one percent increase in the independen will cause the percentage change in the parameter as given by the curve-fit coef listed below.	dependent

1, HPOTP TURBINE SPEED (RPM)	35. OXIDIZER PRESSURANT TEMPERATURE (R)
2. HPFTP TURBINE SPEED (RPM)	35. OXIDIZER PRESSURANT TEMPERATURE (R) 36. FUEL PRESSURANT TEMPERATURE (R)
3. HPOTP PUMP DISCHARGE PRESS.(PSIA)	37. LPOTP PUMP SUCTION SPECIFIC SPEED
4. HPFTP PUNP DISCHARGE PRESS.(PSIA)	38. LPFTP PUMP SULITUM SPELIFIC SPEED
5. OPB CHAMBER PRESSURE (PSIA)	39. HPOTP PUMP SUCTION SPECIFIC SPEED
6. FPB CHAMBER PRESSURE (PSIA)	40. NPFTP PUMP SUCTION SPECIFIC SPEED
7. ENGINE OXIDIZER FLOWRATE (LB/SEC)	41. MCC COOLANT DISCHARGE PRESSURE (PSIA)
8. ENGINE FUEL FLOWRATE (LB/SEC)	42. NCC COOLANT DISCHARGE TEMPERATURE (R)
9. ENGINE THRUST (LB)	43. LPOTP TURBINE TORQUE (FT-LB)
10. OX101ZER PRESS. FLOWRATE (LB/SEC)	
11. FUEL PRESSURANT FLOWRATE (LB/SEC)	45. HPOTP TURBINE TORQUE (FT-LB)
12. OPB OXIDIZER VALVE POSITION	46. HPFTP TURBINE TORQUE (FT-LB)
13. FPB OXIDIZER VALVE POSITION	47. LPOTP TURBINE FLOWRATE, LBM/S
14. NCC OXIDIZER INJECTOR PRESS (PSIA)	
15. HCC OXIDIZER INJECTOR TEMP (R)	49. HPOTP TURBINE FLOWRATE LAM/S
16. HOT GAS INJECTOR PRESSURE (PSIA)	50 HPETP TURBINE FLOWRATE LBM/S
17 NCE INJECTOR END PRESSURE (PSIA)	51. LPOTP TURBINE INLET PRESSURE, PSIA
	52. LPFTP TURBINE INLET PRESSURE, PSIA
	53. HPOTP TURBINE INLET PRESSURE, PSIA
20. PU PUMP DISCHARGE PRESSURE (PSIA)	
21. HPOTP PUMP INLET TEMPERATURE (R)	55. LPOTP TURBINE INLET TEMPERATURE, (R)
	56. LPFTP TURBINE INLET TEMPERATURE, (R)
	57. HPOTP TURBINE INLET TEMPERATURE, (R)
24. MFV DISCHARGE TEMPERATURE (R)	58. HPFTP TURBINE INLET TEMPERATURE, (R)
25. PB PUMP DISCHARGE TEMP. (R)	59. LPOTP TURBINE DISCHARGE PRESS., PSIA
26. HPFTP PUMP INLET TEMPERATURE(R)	60. LPFTP TURBINE DISCHARGE PRESS., PSIA
27. LPOTP TURBINE SPEED (RPM)	61. HPOTP TURBINE DISCHARGE PRESS., PSIA
28. LPFTP TURBINE SPEED (RPN)	59. LPOTP TURBINE DISCHARGE PRESS., PSIA 60. LPTP TURBINE DISCHARGE PRESS., PSIA 61. HPOTP TURBINE DISCHARGE PRESS., PSIA 62. HPFTP TURBINE DISCHARGE PRESS., PSIA
29. HPOT DISCHARGE TEMP (R)	•
30. HPFT DISCHARGE TEMP (R)	
31. OPB OXIDIZER VALVE RESISTANCE	
J2. FPB OXIDIZER VALVE RESISTANCE	
33. OXIOIZER PRESSURANT PRESSURE (PSIA)	
34. FUEL PRESSURANT TEMPERATURE(R)	
34. FUEL PRESSURAMI IEMPERATURE(X)	

۰.

are used in the definition of max/min conditions used for the engine balance limits. These max/min conditions, together with the design limits of the engine inlet conditions, are used for design purpose as boundaries to check that the engine operation will satisfactorily continue into another test or flight.

The engine dynamic (transient) simulation model is also formulated using generic engine process descriptions, constitutive equations, and detailed tabulation of propellant physical properties. The description of the basic processes of the system simulation involves all applicable static and dynamic formulations considered important in accurately representing the overall behavior of the engine during start, mainstage control, and cutoff. The validity and veracity of these process descriptions, in terms of their ability to describe the overall system behavior, have been proven by correlation of simulation results with engine test results from previously developed rocket engines.

Table 4.3.	SSME	Model	Random	Variables
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	YARIABLE NAME	2 @ VARIATIO 	N POWER	LPFTP	LPOTP	HPFTP	HPQTP	NOZZLE	HEAT EXCHANGER
۱.	Main Chamber Throat Area	0.2	X	x	X	X	x	x	x
2.	Efficiency C <sub>r</sub>	0.2	x	X	X	X	X	x	X
	(thrust coefficient)								
3.	Efficiency C*	0.25	x	X	x	X	X	x	X
	(characteristic velocity)								
4.	Chamber Coolant Resistance	8.0	x	x		x		r	
5.	Main Oxidizer Injector Resistance	5.0	x		x	X	X		x
6.	Main Hot Gas Injector Resistance	5.0	x			X	X	L	x
7.	FPB Fuel Injector Resistance	2.0	x			x	X	x	x
₿.	OPB Fuel Injector Resistance	2.0	x			X	X	X	I
9.	Fuel Hot Gas Manifold Resistance	10.0	x	X		X	X	X	X
0.	LDX Hot Gas Manifold Resistance	10.0	x	x		X	X	x	X
۱.	Main LOX Dome Resistance	4.0	X		X	x	X		x
2.	OP2 Discharge Duct Resistance	4.0	x		x	x	x		ž
·	(HPOT discharge press.)	••	-		<b>·</b>	~	~		~
3.	LPFT Nozzle Area	2.0	x	x		X	X	x	
4.	LPOP Efficiency	1.0	-	ч	x	~	x	~	
5.	LPOT Efficiency	4.0			x		x		
6.	LPOT Nozzie Area	2.0			x		x x		
1.	HPFP Efficiency	1.6	X	x	x	X	x	X	
8.	HPFT Efficiency	2.0	ĩ	x	, x	x	x	x	I I
9.	HPFT Nozzle Area	2.0	ĩ	x	x	x	x	X	
5.	HPOP Efficiency	0.8	x	x	x	x	x	x	X
1.	HPOT Efficiency	2.0	ĩ	x	x	ž	x		x
2.	HPOP Head Coefficient	0.8	•	^	^	•		X	X
).	HPFP Head Coefficient	1.6				x	X		
	HPOT Nozzle Area	2.0	x			x	X	X	
5.	Preburner Pump Efficiency	0.8	~			^	x	^	
	Preburner Pump Head Coefficient	0.8					î		
	Chamber Coolant Valve Resistance	17.6		X		X	^	X	
).	Hain LOX Valve Resistance	12.7		^	X	•	x		
).	Hain Fuel Valve Resistance	12.7		x	•		*		
).	Primary Faceplate Resistance	15.0	x	x		x x		,	
	Secondary Faceplace Resistance	15.0	x	x		x		X X	
2.	MCC Baffles Resistance	6.6	x	x		x		X	
	Heat Exchanger Bypass Resistance		~	~		•		•	
		2.63* 8.5*							X
		a.s- 1.3	x						X
5. 5.			X	I T	X	X	X	X	X
		1.0	*	X	1	X	X	X	X
/. ].		100.0*	-					_	X
).		100.0*	x	_				X	
		5.0	X	X	X	X	X	X	X
	LPOP Head Coefficient	2.0			X				
1. •		2.0		X					
•		8.0	X	X		X	X	X	X
	LPFT In Duct Res	4.0		X		X			
	LPOT Area	2.0			X		X		
	Nozzle AT	5.0	X	x		X		X	X
<b>.</b>	MCC Coolant af	8.0	X	X		X		X	X

The transient phase of the load definition is based on a combination of vehicle requirements, engine simulation models and engine test results. Typical vehicle requirements were discussed earlier: start and cutoff transient envelopes specified to minimize vehicle loads. Additional requirements, like rates of power level changes during throttling and associated up-thrusts, are additional requirements that size-control some of the nominal loads on components during transient operation. Thrust control drives pump speeds, torques, and system pressures and temperatures. Generally, the dynamic simulation models are used for transient conditions below 65% power level. Various transient models are employed for surveying system characteristics, tradeoff and optimization of the control system, and evaluating system design changes simulating nonlinear operating conditions.

The dynamic simulation models and steady-state performance models describe the same processes; however, the performance models stress accuracy of steady-state operation parameters, but the dynamic simulation models have to consider the overall system behavior throughout the duty cycle. Figure 4.1 shows how the SSME thrust buildup is contractually controlled. The shape of the thrust buildup, as well as the shape of the transient duty cycle loads, are governed by the event sequences defined for startup and shutdown transients.

The SSME start transient event sequence is shown in Figure 4.4. These events are control system parameters, e.g., either valve opening conditions or analysis events known to occur in the transient operation, such as injector dome priming, fuel side oscillation. They can be related to surges, large thermal transients, chugging, pops, and sideloads.

The dynamic simulation model is essentially a nominal operation description of engine startup and shutdown operations.

The engine performance model and the dynamic simulation model furnish the system's operating load conditions: pressures, temperatures, vibration levels for inlet and outlet conditions of transfer ducts, preburners, injectors, and turbopumps (Figure 4.5). These interface loads are used with deterministic models to evaluate loads on individual components like turbine blades,

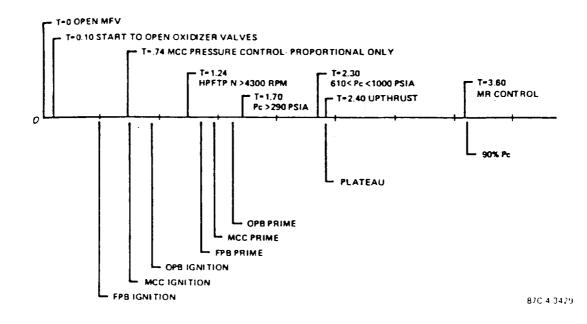


Figure 4.4. SSME Start Timeline

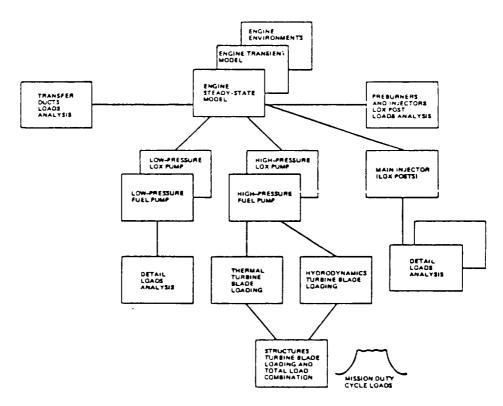


Figure 4.5. Interrelation of SSME Analysis Models

transfer ducts, LOX posts, etc. For instance, the steady-state loads are used by the hydrodynamics specialists to determine loads across each turbine stage or blade. The heat transfer specialists use information from the same model results to determine blade temperatures. The dynamics experts use the model results to determine turbine blade dynamics. The structural and analysis experts use model information and input loads from other experts to develop the total load and structural analysis.

## 4.3 Probabilistic Load Models

The engine performance model, dynamic simulation model, and other deterministic models are too complex to be used as basic tools to synthesize engine loads. The CLS approach to probabilistic load development is to synthesize loads with information extracted from engine data and detail analysis results of the deterministic engine load models. The CLS probabilistic load models treat the engine operation as a stochastic process. The engine hardware parameters, operating inlet condition variables, and all engine loads are assumed to be random variables. Scaling models are utilized whenever possible.

The influence model developed for engine performance evaluation is ideal for CLS. It is a numerical abstract of the engine model. It can evaluate engine loads for different power levels. With the random variable assumption, probabilistic methods can be applied to the influence model to obtain load distributions. This probabilistic influence model thus becomes the CLS system-level engine model. It provides all of the system's operating loads subsequently used by component load models to generate component loads.

The probabilistic influence model utilizes influence coefficients to correlate changes in engine operating parameters and inlet condition variables (classified as system-independent loads) to changes in system operating conditions and performance variables classified as system-dependent loads. The influence equation is:

$$\frac{del Y_i}{Y_{io}} = \sum_{j}^{\Sigma} (IC)_{ij} \frac{del X_j}{X_{jo}}$$
(4.1)

where,  $X_{j0}$  is the nominal value of the jth engine independent load del  $X_{j}$  is the change in the jth independent load  $Y_{i0}$  is the nominal value of the ith dependent load del  $Y_{i}$  is the change in the ith dependent load (IC)<sub>ij</sub> is the influence coefficient correlating the jth independent load to the ith dependent load

With few exceptions, the nominal values for the independent loads are not varied with the command power level. The nominal values for dependent loads and influence coefficients are functions of power level. Their variations are fitted into a polynomial function of the commanded power level as below:

 $Y_{jo} = a_{o} + a_{1}^{*}T + a_{2}^{*}T^{*}T + a_{3}^{*}T^{*}T^{*}T$   $(IC)_{ij} = c_{o} + c_{1}^{*}T + c_{2}^{*}T^{*}T + c_{3}^{*}T^{*}T^{*}T$ where,  $a_{i}$ 's and  $c_{i}$ 's are constant coefficients, T is the commanded power level in fraction of the rated power.

The probabilistic influence model implemented on the load-expert system has 23 system-independent loads as listed in Table 4.1 and 62 system-dependent loads as listed in Table 4.2. The distribution information of independent loads is obtained based on a 10-sec average database of the SSME flight and test data. These load parameters are stored in the load-expert system knowledge base in database format. They can be conveniently retrieved and updated.

The deterministic influence model is valid for the power range from 65% to 110% power levels. In CLS, the power range of the probabilistic influence model is extended down to zero. The complete duty cycle of the engine operation is therefore modeled by the same influence model. During the transient phase of the duty cycle, a quasi-steady state is assumed, i.e., the loads behave as steady-state loads within each time step. Discussion on the duty cycle load calculation and transient model is deferred to next section. Verification of the probabilistic influence model was performed by comparing load calculations with the SSME 10-sec average database. The general finding is that variations of the system loads, as calculated with the probabilistic influence model, do not cover the corresponding variations of the SSME 10-sec average database. Initially, the load calculations were thought to be related to instrumentation measurement errors as the HPFTP discharge temperature calculation was under investigation. However, the same thing happened when the pump speed calculation was evaluated. The pump speed measurement has about the best measurement accuracy. This pointed out the inadequacy of the probabilistic model.

The SSME 10-sec average database includes data from flights and tests. The database includes data from numerous engines. Variations in the database consist of engine-to-engine variations and test-to-test variations. Engine-to-engine variations account for the changes in engine hardware, whereas test-to-test variations account for variations from different tests of an engine. In the deterministic modeling, tag values are used to account for engine-to-engine variations due to the use of different engines as well as changing components. Tag values are calculated by the engine performance model. The tag value method does not quite fit into the probabilistic influence model because tag values have to come from outside of the model.

It is known that engine-to-engine variations are related to engine hardware. Different manufacturing processes, different manufacturers, and different assembling procedures, etc. all contribute to hardware variations. A set of random variables related to engine hardware, as listed in Table 4.3, has been determined to have significant effect on components of interest in this project. As shown in Table 4.3, the letter X in each column indicates significant effects of the hardware random variable to the hardware identified at the top of the column. These random variables fit naturally into the probabilistic influence model as system-independent hardware parameter variables. Therefore, an expanded list of engine system-independent loads and dependent loads were developed for the next version of the CLS engine load model. The new list of system-independent loads with their means and coefficients of

variation is shown in Table 4.4. System-dependent loads are shown in Table 4.5. A new influence coefficient set is required for the expanded list of engine system loads. The probabilistic influence model with the expanded set of influence coefficients will be implemented on the CLS load-expert system during the option phase of the project. To reiterate, this is an excellent solution to meet contract requirements for modeling a generic engine, not necessarily of the SSME type.

With the probabilistic influence model as the overall engine system model synthesizing system interface loads or system-dependent loads, various compo ent load models can be built on the next level (ref. Figure 2.3). The component load models use system-dependent loads as input loads and generate component loads local to the components. In modeling component loads, generic scaling technique and influence method are employed. The goal is to build generic models which can be utilized across different components and for different engines. This goal has been satisfied. The CLS now has a generic static pressure scaling model, a generic probabilistic thermal load model, and a generic fluctuation pressure load. These models will be described in the CLS load implementation section.

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	Table 4.4.	Engine	Influence	Model	Independent	Loads
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ID	INDEPENDENT LOAD	NOMINAL VALUE	<u>c.o.v.</u>
1	Commanded mixture ratio	6.0	$\frac{0.001}{0.002}$
2	Fuel inlet pressure (psia)	30.0	0.259
3	Oxidizer inlet pressure (psia)		0.327
4	Fuel inlet temperature (R)	37 0	0.016
5	Oxidizer inlet temperature (R)	164.0	0.011
6	Fuel pressurant flowrate (lbm/sec	:) 0.7	0.0065
7	Oxidizer pressurant flowrate (1bm	/sec) 1.5968	0.015
8	HPFP cavitation (%)	1.0	0.001
9	LPFP cavitation (%)	1.0	0.001
10	LPOP cavitation (%)	1.0	0.001
11	Nozzle, mixer delta P (%)	1.1455	
12	MCC throat diameter (in)	10.293	0.001
13	Nozzle exit diameter (in)	90.324	
14	LPFT nozzle area (in <sup>2</sup> )	0.95	0.1
15	LPOT nozzle area (in <sup>2</sup> )	1.386	0.1
16	LPFP efficiency (%) HPFP efficiency (%)	1.11	0.0017
17	HPFP efficiency (%)	1.00	0.008
18	LPFT efficiency (%)	1.025	0.0027
19	HPFT EIICIENCY (%)	1.0355	0.01
20	LPOP efficiency (%)	1.14	0.005
21	HPOP efficiency (%)	1.02	0.004
22	PBP efficiency (%)	1.022	0.0016
23	LPOT efficiency (%)	1.022	0.02
	HPOT efficiency (%)	1.0152	0.01
	HPOP cavitation (%)	1.0	0.001
	LPFP head coefficient (%)	0.99	0.007
	HPFP head coefficient (%)	1.0237	0.008
	LPOP head coefficient (%)	1.0	0.013
29	PBP head coefficient (%)	1.155	0.004
30	MCC OX dome resistance	0.0384	0.02
31	HGM OX side resistance	0.0032	0.05
32	HGM fuel side resistance	0.0275	0.05
33	MCC Hot Gas injector resistance	0.0031	0.025
34	HGM coolant OX side resistance		
35	LPOP disch duct resistance	0.0021	
	Primary faceplate resistance	15.0	0.075
37	Secondary faceplate resistance	11.17	0.075
38	LPFT seal resistance	7283.0	
39	HPOT coolant circuit resistance	2066.0	
40	HPFP disch duct resistance	0.0123	
41	Main fuel valve resistance	0.0138	0.064
42	Main oxidizer valve resistance	0.0107	0.064
43	MCC OX injector resistance	0.0602	0.025
44	MCC cooling jacket delta pressure	1.031	

Table 4.4. Engine Influence Model Independent Loads (Continued)

, *,* 

<u>ID</u> 45 46	OPB fuel injector resistance FPB fuel injector resistance	NOMINAL VALUE 0.685 0.155	
48	LPFT disch duct resistance LPFT inlet duct & F-7 resistance PBP inlet duct resistance	0.104 0.5689 0.134	0.01
50 51 52	Coolant control valve resistance Baffle flow coefficient PB fuel supply duct resistance	0.05568 0.95	0.088
54	Nozzle delta P (%) HPOTP turb-end bearing coolant res		0.001
56	MCC combustion efficiency (MCC C*) Nozzle heat load (%) MCC chamber heat load (%)	0.884 0.7932	0.001
60	HPOT flow coefficient Preburner combustion efficiency (%	•	
	Mixer delta P (%) LOX flow constant (c2) MCC pc measurement error (%) Engine fuel flowmeter error (%)	1.0 2.8952 1.0 1.0	

ID	INDEPENDENT LOAD	NOMINAL VALUE	<u>c.o.v.</u>
1	Engine altitude thrust (lbf)	471067.522	0.005
2	HPOTP speed (rpm)	27239.145	0.004
3	HPFTP speed (rpm)	34517.69	0.008
4	HPOP disch pressure (psia)	1595.403	0.0089
5	PB pump disch pressure (psia)	7185.46	0.0098
6	HPFP disch pressure (psia)	6161.829	0.009
7	OPB chamber pressure (psia)	5039.427	0.0129
8	FPB chamber pressure (psia)	4876.04	0.0137
9	Engine oxidizer flowrate (lbm/sec)		0.0062
10	Engine fuel flowrate (lbm/sec)	149.06	0.0069
11	Oxidizer pressurant flowrate(lbm/s	sec) 1.5968	0.015
12	Fuel pressure flowrate (lbm/sec)	0.6996	0.0065
13	OPB oxidizer valve position (%)	0.6495	0.0147
14	FPB oxidizer valve position (%)	0.7652	0.0135
15	MCC oxidizer injector pressure(psi	ia) 3540.82	0.0086
16	MCC Hot Gas injector pressure (psi		0.0064
17	MCC injector end pressure (psia)	3006.0	0.0058
18	HPOP inlet pressure (psia)	380.07	0.0228
19	HPFP inlet pressure (psia)	226.084	0.0263
20	HPOP disch temperature (R)	190 <b>.19</b> 5	0.002
21	HPFP disch temperature (R)	94.904	0.0114
22	MFV disch temperature (R)	95.491	0.0114
23	PB pump disch temperature (R)	203.377	0.0025
24	HPOP inlet temperature (R)	169.425	0.006
25	HPFP inlet temperature (R)	42.472	0.0019
26	LPOTP speed (rpm)	5042.8	0.008
27	LPFTP speed (rpm)	15850.64	0.0087
28	HPOT disch temperature (R)	1352.533	0.0274
29	HPFT T/D disch temperature (R)	1625.723	0.0193
30	OPB oxidizer valve resistance	130.79	0.098
31	FPB oxidizer valve resistance	13.18	0.15
32	Oxidizer pressurant pressure (psia	a) 3439.598	0.0092
33	Fuel pressurant pressure (psia)	3348.296	0.0079
34	Oxidizer pressurant temperature (H	R) 838.0	0.0245
35	LPFT disch temperature (R)	472.95	0.0125
36	LPOP suction specific speed (NSS)	8054.341	0.02
37	LPFP suction specific speed (NSS)	19738.26	0.02
38	HPOP suction specific speed (NSS)	11295.08	0.0185
39	HPFP suction specific speed (NSS)	6017.04	0.024
40	MCC coolant disch pressure (psia)	4840.48	0.0108
41	LPOT torque (ft-lbf)	1565.124	0.0159
42	LPFT torque (ft-1bf)	996.605	0.0182
43	HPOT torque (ft-1bf)	4436.78	0.0108
44	HPFT torque (ft-lbf)	9452.388	0.0142

# Table 4.5. Engine Influence Model Dependent Loads

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Table 4.5.	Engine	Influence	Mode1	Dependent	Loads	(Continued)

TD		IONTNAL VALUE	
<u>ID</u> 45		NOMINAL VALUE 176.17	<u>C.O.V.</u> 0.01
	LPOT flowrate (lbm/s)	26.46	0.0175
46	LPFT flowrate (lbm/s)	28.40	0.01
47	HPOT flowrate (lbm/s)		
48	HPFT lfowrate (lbm/s)	158.92	0.0107
49	LPOT inlet pressure (psia)	3947.348	0.0895
50	LPFT inlet pressure (psia)	4508.63	0.0105
51	HPOT inlet pressure (psia)	5019.85	0.00875
52	HPFT inlet pressure (psia)	4857.17	0.0095
53	LPOT inlet temperature (R)	190.195	0.002
54	LPFT inlet temperature (R)	489.121	0.0122
55	HPOT inlet temperature (R)	1501.062	0.0266
56	HPFT inlet temperature (R)	1812.757	0.0186
57	LPOT disch pressure (psia)	414.28	0.0208
58	LPFT disch pressure (psia)	3403.035	0.0076
59	HPOT disch pressure (psia)	3318.146	0.0066
60	HPFT disch pressure (psia)	3439.885	0.0067
61	LPOT power (bhp)	1502.269	0.024
62	LPFT power (bhp)	3013.01	0.027
63	HPOT power (bhp)	23012.439	0.0155
64	HPFT power (bhp)	62192.2	0.0175
65	HGM inlet pressure, fuel (psia)	3356.87	0.0075
66	HGM inlet pressure, OX (psia)	3302.345	0.0075
67	Oxidizer T/D dynamic pressure (psia	a) 16.6	0.01
68	Oxidizer T/D flow velocity (ft/s)	454.81	0.01
69	Fuel T/D dynamic pressure (psia)	25.72	0.01
70	Fuel T/D flow velocity (ft/s)	578.4	0.01
71	HPOT mixture ratio (0/F)	0.7323	0.034
72	HPFT mixture ratio (O/F)	0.9267	0.0227
73	OPB power (bhp)	168661.0	0.02
74	FPB power (bhp)	544895.0	0.02
75	MCC power (bhp)	1.2473E+07	0.005
76	OPB OX in manifold pressure (psia)		0.013
77	OPB fuel in manifold pressure (psia		0.0085
78	FPB OX in manifold pressure (psia)	6088.94	0.0137
79	FPB fuel in manifold pressure (psia		0.0088
80	PBP disch, PB OX supply temp (R)	203.377	0.0025
81	Mixer disch, PB fuel supply temp (I		0.0045
82	Fuel HGM velocity (ft/s)	1322.532	0.01
83	Fuel HGM dynamic pressure (psia)	132.983	0.01
84	LOX HGM velocity (ft/s)	214.13	0.01
85	LOX HGM Verocity (10/3) LOX HGM dynamic pressure (psia)	3.737	0.01
86	OPB fuel dynamic pressure (psia)	0.1978	0.01
87	OPB fuel flow velocity (ft/s)	367.214	0.01
87 88	FPB fuel dynamic pressure (psia)	44.647	0.01
00	tro fuer dynamic pressure (bata)	44.04/	0 • 0 T

Table 4.5. Engine Influence Model Dependent Loads (Continued)

ID	INDEPENDENT LOAD	NOMINAL VALUE	<u>c.o.v.</u>
89	FPB fuel flow velocity (ft/s)	411.96	0.01
90	HPOP disch dynamic pressure (psia)	230.658	0.01
91	HPOP disch velocity (ft/s)	174.213	0.0052
92	HPOP head rise (ft)	7545.048	0.0095
93	HPFP disch dynamic pressure (psia)	123.277	0.01
94	HPFP disch velocity (ft/s)	469.11	0.0055
<b>9</b> 5	HPFP head rise (ft)	174050.04	0.0085
96	PBP disch dynamic pressure (psia)	32.48	0.01
97	PBP disch velocity (ft/s)	65.14	0.0052
98	HGM coolant inlet pressure (psia)	3346.037	0.0074
99	Engine nozzle exit velocity (ft/s)	14562.83	0.01
		`	•

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# 5.0 PROBABILISTIC METHODOLOGY

## 5.1 <u>Introduction</u>

This section reports on the progress and development of the probabilistic load model for generic space propulsion engines. This effort is part of the program being conducted by Rocketdyne and Battelle Columbus Division for NASA Lewis Research Center to develop an expert system to predict composite loads in a generic space propulsion engine. The ultimate goal of the program is to address generic engines that may include different mission profiles or incorporate design changes. The program requires that a robust and general probabilistic approach be adopted for inclusion in the expert system model. During the first year of the program, a survey was conducted to select these models and the initial programming, debugging, and shake-down analyses were performed. The second year of the program was oriented towards building the probabilistic methodology. A database was developed that could be used by both the probabilistic methodology and the expert system. The database included different functional forms for the load description, model verification and validation, and the generalization of the computer program system. The third year of the program focused primarily on the refinement of current methodology, improvement of the transient load model, incorporation of the periodic load model, verification of the probabilistic methodology, and documentation.

The probabilistic model includes three probabilistic methods: (1) a Gaussian moment propagation method which assumes that all load variables and engine parameters are normally distributed, (2) a discrete probability method (RASCAL), and (3) Monte Carlo. The Gaussian moment propagation method, referred to as the Quick Look Model (QLM) provides a fast, efficient method for determining the composite load distribution, providing that basic variable distributions are not severely skewed. RASCAL is a discrete method capable of handling standard distributional forms (e.g., normal, lognormal, Weibull, etc.), and nonstandard forms such as bi-modal. RASCAL also provides a range

of levels for accuracy. RASCAL also performs important sampling used to examine regions of concern for the composite load although such values would be unexpected during nominal engine operation. Finally, Monte Carlo analysis is available so that classical confidence limits can be obtained to assess the accuracy of the composite load prediction.

All phases of the mission history profile are addressable by the probabilistic load model. Currently, each mission profile is divided into phases defined as transient, quasi-steady, or steady-state phases. The transient phase is characterized by rapid changes in the amplitude of individual loads and engine parameters. Rapid changes allow the program to ignore small oscillations about the much larger nominal load fluctuations. Uncertainty in the load is caused by variability in the peak load value and its time of occurrence. The quasi-steady phase is that portion of the mission where the nominal value of the load is slowly changing and can thus be approximated by staircase type quasi-steady state steps. The steady-state region is where the nominal values of all of the individual and composite loads are approximately constant. Unlike the transient phase, both the quasi-steady and steady-state phase do have fluctuations superimposed upon the nominal behavior. Additionally, each of these phases can have spike values superimposed which represent the occurrence of rare events.

## 5.2 Probabilistic Methods Quick Look Model

In some analysis, only an approximation to the variability of the load is needed. In such a case, the relatively long running time of RASCAL or Monte Carlo simulation models is not justified. To provide a program which quickly calculates such an approximation, the QLM was developed.

The basic assumption made in the QLM model is that all of the individual loads and engine parameters used to predict individual and composite loads are normally distributed. In this case, the influence function tables can be used

directly to calculate the mean and variance of the output. If there are dependencies among variables, then some modification to the current program is needed. However, if the correlation coefficient is provided or calculated, then exact solutions are still available. The basic formulas used to perform these calculations are given by the algebra of normal distributions presented below. In these formulas,  $\mu$  represents the mean or expected value of the random variable, and  $\sigma$  is the standard deviation, i.e., the square root of the variance.

These formulas are used in conjunction the influence equations to provide mean and variance estimates of load variables. Since influence functions currently in the probabilistic load model do not involve any divisions, all of the formulations are exact (assuming independence), if the probability density functions are all Gaussian.

Statistics Of The Sum: Z = X + Y

$$E[Z] = \mu_{\chi} + \mu_{y}$$

$$VAR[Z] = \sigma_{\chi}^{2} + \sigma_{y}^{2} + 2\rho\sigma_{\chi}\sigma_{\chi}$$
(3)

Statistics Of The Difference: Z = X - Y

$$E[Z] = \mu_{x} - \mu_{y}$$

$$VAR[Z] = \sigma_{x}^{2} + \sigma_{y}^{2} - 2\rho\sigma_{x}\sigma_{y}$$
(4)

Statistics Of The Product: Z = X \* Y

$$E[Z] = \mu_{X} \star \mu_{y} + \rho \sigma_{X} \sigma_{y}$$

$$VAR[Z] = \mu_{y}^{2} \sigma_{x}^{2} + \mu_{y}^{2} \sigma_{x}^{2} + \sigma_{x}^{2} \sigma_{y}^{2} 2\rho \mu_{x} \mu_{y} \sigma_{x} \sigma_{y} + \rho^{2} \sigma_{x}^{2} \sigma_{y}^{2} \qquad (5)$$

<u>Statistics Of The Quotient: Z = Y / X</u>

$$E[Z] \approx \frac{\mu_{y}}{\mu_{\chi}} \left[ 1 + \frac{\sigma_{\chi}}{\mu_{\chi}} \left( \frac{\sigma_{\chi}}{\mu_{\chi}} - \rho \frac{\sigma_{y}}{\mu_{y}} \right) \left( 1 + 3 \frac{\sigma_{\chi}^{2}}{\mu_{\chi}^{2}} + \dots \right) \right]$$

$$VAR[Z] \approx \frac{\mu_{y}^{2}}{\mu_{\chi}^{2}} \left[ \frac{\sigma_{\chi}^{2}}{\mu_{\chi}^{2}} + \frac{\sigma_{y}^{2}}{\mu_{y}^{2}} - 2\rho \frac{\sigma_{\chi}\sigma_{y}}{\mu_{\chi}\mu_{y}} + 8 \frac{\sigma_{\chi}^{4}}{\mu_{\chi}^{4}} \right]$$
(6)

Two options exist in the computer code for using the QLM model. If the user requests that the QLM model be used and all of the input distributions are not normal, then the corresponding mean and variance are calculated by the appropriate moment transformation. On the other hand, if the user does not request the QLM model, yet all input distributions are gaussian, then the QLM model is substituted. The QLM substitution is made since there is no reason to run a simulation to approximate an answer which can be obtained exactly with the QLM model.

## Discrete Probability Distribution Method

Discrete probability distributions (DPDs) are tools in risk analysis to simplify the computations necessary to determine failure probabilities. DPDs may be used to investigate probabilistic functions: (1) functions whose exact form is uncertain, and (2) calculation of quantities where there is significant uncertainty numerical quantities that should be replaced by probability distributions. Mathematical operations between these quantities should be replaced by analogous operations between probability distributions.

Suppose the initial values of loads are discretized into M values. Each value of each variable is then assigned a probability of occurrence. If these

discrete values are paired with their probabilities, the following vectors of ordered pairs result for two loads, X and Y:

$$X = (X_1, p_1), (X_2, p_2), \dots, (X_m, p_m))$$
  

$$Y = (Y_1, q_1), (Y_1, q_2), \dots, (Y_m, q_m)).$$

The number of discrete points in each of these vectors has been chosen to be the same, although it is not necessary to do so. The addition of two discrete vectors is defined by

$$Z = Y + X$$

$$Z = (Y_i, p_i) + (X_j, q_j), \text{ and}$$

$$Z = (X_j + Y_i, p_iq_j) \text{ for all i and j.}$$

Therefore, the addition of two vectors containing m-ordered pairs results in each vector having  $m^2$ -ordered pairs. The multiplication of DPDs is similarly defined:

$$Z = X * Y$$

$$Z = [X_j * Y_i, p_i * q_j)] \text{ for all } i \text{ and } j$$

For the combination of a large number of loads, the amount of computer storage increases very quickly. If there are k loads, each described by M discrete points, then the vector will contain  $M^k$ -ordered pairs. Since, even for relatively small values of M and K (on the order of 20), the computer storage capability will quickly be exceeded, it is necessary to examine some procedure for reducing this vector's size. This leads to the introduction of a condensation or aggregation procedure.

The condensation operation must preserve the total probability and mean within each vector while ensuring that the residual error afterwards is as small as possible. A new procedure for handling such problems was developed by Kurth (ref. 5.2) and has been denoted RASCAL. This algorithm is covered in detail in reference 5.2 but its basis is the DPD algorithm, even though, strictly speaking, it is not a DPD process. The RASCAL algorithm is the primary analysis method used throughout this program.

RASCAL can be summarized as follows. The input variables are discretized into DPDs denoted:

 $X_{i} = [X_{i,j}, P_{i,j})]$ 

where

i = 1, 2, . . ., n
j = 1, 2, . . ., ND
n = number of variables
ND = number of discrete points
X<sub>i,j</sub> = conditional mean of variable i in discrete interval j
P<sub>i,j</sub> = probability of X<sub>i,j</sub>
X<sub>i</sub> = input variable i.

The input variables are related to a response, R, by some function, denoted f. Thus,

 $R = f(X_1, X_2, \ldots, X_n)$ .

At this point, it is decided how many points one wishes to use to characterize the conditional mean of each interval in R after condensation (this number is denoted by M). If

 $ND \cdot M > ND^{n}$ 

then the standard DPD algorithm is used. This is done to minimize the calculational time since, in this case, duplicate values will be produced. If (ND-M) is less than  $ND^{n}$ , then n random integers between 1 and ND are generated:

A response,  $R_1$ , is calculated by

$$R_1 = f(X_{1,k_1}, X_{2,k_2}, \dots, X_{n,k_n})$$

and the associated probability is given by  ${\ensuremath{^\dagger}}$ 

$$q_{1} = \prod_{i=1}^{n} P_{i,k_{i}}$$

The process is repeated (ND•M) times to give an array of ordered pairs of the responses:

$$V = [R_1, q_1), (R_2, q_2), \dots, (R_L, q_L)]$$
  
L = ND•M

Condense V to  $V_p$ , to produce the desired distribution:

$$V_{R} = [(R_{1}, P_{1}), (R_{2}, P_{2}), \dots, (R_{ND}, P_{ND})]$$

<sup>&</sup>lt;sup>†</sup>This calculation assumes that the input variables are independent.

The RASCAL method provides accuracy close to the Monte Carlo method in less computational time. In addition, if a given region of the input variable's range needs to be examined more accurately, RASCAL provides a means for doing so by input rather than by requiring coding changes. The RASCAL method does not provide any way to estimate the confidence level of the result available with the Monte Carlo analysis. However, the true result can be approached asymptomatically by increasing the number of data points used in individual DPDs. Later chapters in this report discuss validation of the RASCAL methodology.

## Monte Carlo

The Monte Carlo technique is a method for solving problems by constructing a random process for each problem. This random process is so devised that parameters and quantities of interest may be calculated from random samples from a given distribution. In effect, it is simply a method for adding a probabilistic structure to a deterministic model.

As an example, consider a specific piece of equipment in a space propulsion engine. Suppose the composite load, denoted by  $L_c(t)$ , is related to the individual load  $L_i(t)$ , by a general function

$$L_{c}(t) = f(L_{1}(t), L_{2}(t), ..., L_{n}(t))$$

For instance, consider  $L_{c}(t)$  for the turbine blades where the  $L_{i}(t)$  are loads due to the effects of temperature, pressure, vibrational modes, and so forth. If each individual load has been characterized by a probability distribution function (PDF), then the following procedure is used during a Monte Carlo simulation:

- 1. The cumulative distribution function (CDF) of each individual load is generated by integrating the PDF.
- 2. Invert the CDF.

- 3. Generate a random number,  $r_1$ , between the values of 0 and 1.
- 4. Let  $F(L_j(t_1))$  represent cumulative probability of realizing a load  $L_j(t_1)$  at time step  $t_1$ . From the inverted CDF, the value of  $L_i(t_1)$  is uniquely determined, where  $F(L_i(t)) = r_1$ .
- 5. Let N be the total number of individual loads. Let M be the total number of time steps, ti. Repeat Steps 3 and 4 for each  $L_j(t_i)$ :  $1 \le j \le N$ , for a given  $t_i$ . A value of  $L_c(t_i)$ , where

$$L_{c}(t_{i}) = f(L_{1}(t_{i}), L_{2}(t_{i}), \dots, L_{N}(t_{i}))$$

is calculated. The entire process is repeated until the number of time steps exceeds M (or insufficient computer time terminates execution.

The result is an M-dimensional vector of composite loads:  $(L_c(t), L_c(2), \ldots, L_c(M))$ . This vector is used to construct a histogram of the composite load. This histogram can now be analyzed statistically to obtain estimates of the mean, kurtosis, probability of the load being exceeded, and so on. By the law of large numbers, the vector described above approaches the continuous distribution in the limit as M tends to infinity. In order to achieve accurate results, however, the value of M must be so large that alternate sampling schemes must be utilized.

The Monte Carlo technique has been included in the probabilistic methods for the load model construction because of the accuracy which can be obtained from the model. Classical statistical estimates of the confidence level can be obtained. If the N responses calculated by the Monte Carlo simulation method are ordered from smallest to largest, then the (100  $_{\star}$   $_{\alpha}$ )th percentile of the load can be bounded by

$$L_{U} = INT[N\alpha + \Phi(0.5(1+\beta))(N\alpha(1-\alpha))^{1/2}] + 1$$
$$L_{I} = INT[N\alpha - \Phi(0.5(1+\beta))(N\alpha(1-\alpha))^{1/2}] + 1$$

where  $\alpha$  is in fractional form,  $\Phi$  is the cumulative distribution function of the standard normal variable, INT[...] is the truncated integer part of a real number and ß is the desired confidence level. For example, if ß is equal to 95% then

$$L_{U} = INT[N\alpha + 0.83525(N\alpha(1-\alpha))^{1/2}] + 1$$
$$L_{L} = INT[N\alpha - 0.83525(N\alpha(1-\alpha))_{1/2}] + 1$$

The major disadvantage to the Monte Carlo method is the cost. Because it is a 'brute force' method, the number of simulations which must be performed to estimate low probability loads grows very quickly. While there are methods available for estimating with greater confidence low probability events for relatively low values of N (for example, importance or stratified sampling methods), the accuracy must necessarily decrease elsewhere. Thus, if the entire range of loads must be determined, then importance sampling methods are not very useful.

#### Summary and Recommendations

The three methods described above are those which have been used in the probabilistic load model development. There is a variety of other investigations which deal with the combination of random and randomly occurring loads. However, most of the other methods are very mathematical in nature and either require or use many assumptions about load types or distributions. In the development of a generic probabilistic load model, it is necessary to limit the number of assumptions so that the widest possible spectrum of load types can be handled by the model. The following probabilistic methods were recommended for use in the probabilistic load model development:

- 1. Gaussian Algebra
- 2. RASCAL
- 3. Monte Carlo

The literature of available probabilistic methods for developing a probabilistic load model for generic space propulsion engines has been reviewed. An assessment of the ability of each method to perform the task required for such a complex environment has been made. There are four important considerations in the development of this model: (1) the ability of the model to handle nonstandard distributional forms, (2) the treatment of nonstationary processes, (3) the handling of physical dependencies in the model, and (4) the ability of the method to operate efficiently so that it will be included in an expert system computer code.

## 5.3 Probabilistic Models

#### Introduction

The construction of a probabilistic load model requires that the physical processes occurring during engine start-up, operation, and cut-off be modeled by techniques that can handle the unique characteristics of the associated processes. For example, during steady-state operation it seems reasonable to assume that the variability in the various individual engine loads will, in most cases, be independent.\* This is a much less valid assumption during such

<sup>\*</sup>This is not meant to imply that the magnitude of the pressures and temperatures, for example, suddenly become independent of each other, but rather that the statistical variability can be treated as independent in the probabilistic model. This assumption of independence will not be made in the coupled engine model to be developed later.

transient operations as engine start, when large changes in loads are coupled by the demand to reach a specified power level. To deal with such nonstationary behavior, the mission history profile is divided into mission history phases. The phases are so defined that either the process can be assumed to be stationary over the phase (quasi-steady) or it has specified models for dealing with nonstationary behavior, i.e., the transient model.

Mission history phases are defined by relating each time period to an event timeline. The event timeline defines the controller-demanded power level of the engine and the associated relative times from engine start when the power is changed. It is also possible to define near instantaneous load changes on the event timeline. This allows such processes as spike transients or rare event loads (i.e., debris loading), to be incorporated into overall probabilistics analysis.

## Steady-State Operation

In all discussions of the different mission history phases, emphasis will be on their relationship to the statistical and probabilistic modeling since it is assumed that such relatively basic concepts are already familiar to most users of this program.

As the name implies, the steady-state mission phase is used when the demanded engine power level is at a constant value for a period of time. During this time there will be nominal engine loads which are the design loads. About these nominal levels there will be fluctuations due to the stochastic behavior of the processes. For a steady-state mission phase, the probabilistic model assumes that the ratio of the variance of the engine load or parameter to its nominal value is constant. This is reasonable from a physical standpoint since we do not design engines so that their nominal operation leads to an unstable growth in the variability of a load about its mean value. Therefore, once the PDF for the steady-state power level has been calculated, it is not necessary to perform any time-dependent calculations because all probabilistic information is contained in this PDF. Subsequent calculations determining stresses induced by such loads would require a sample path obtained from this information; this is easily done using the PDF.

## Quasi-Steady Approximation

During the quasi-steady state mission phase, the assumption is made that individual and composite loads can be modeled as steady-state loads over a sufficiently small time step. Assume that the current time is given as  $t_{\phi}$ . Then between  $t_{\phi}$  and  $(t_{\phi} + \Delta t)$ , the mean and variance is assumed to be constant. After  $(t_{\phi} + \Delta t)$ , the variance and the mean must be adjusted to account for new nominal conditions. In the absence of any other information, it is assumed that this ratio, which is the coefficient of variation, remains constant. After mean values and variances have been updated, the process is repeated from  $t_{\phi} + \Delta t$  to  $t_{\phi} + 2\Delta t$ . The entire process keeps repeating until the end of the quasi-steady phase is reached.

#### Transient Load Model

The transient load model is provided to predict individual and composite load results during the physical transient portion of the engine mission history profile. Usually during these phases, significant departures from nominal behavior occur due to the nonequilibrium operation of the engine. During the engine ignition, for example, the temperature in the transfer ducts, turbines, and LOX posts will change rapidly in what are referred to in this document as spike-type events. A generic methodology has been developed to handle the spike-type events.

The transient model is identified as mission phase 4 or 5 in the computer code input. Mission phase 4 implies that the number of randomly occurring spikes

obey a Poisson arrival rate model. Mission phase 5 implies that the random spikes occur uniformly during the mission phase. The reason both models are available in a Poisson model is that if the mean arrival rate is N events during the mission phase, then during the simulation there will be instances in which many more than N events occur. In many cases, this is physically unrealistic. Therefore, a uniform model is also provided since the user can then be insured that there is an upper bound for the number of spike-type events which occur.

Due to the physics of the engine, the second problem encountered in developing a transient load model is that there are some events which must always occur while subsequent events are randomly occurring. For example, there is always a temperature spike which occurs due to the engine ignition, but, subsequently, there are one or two spikes which can occur. Therefore, a third type of model is available which always requires that fixed spikes occur.

While the number of spikes which occur may be random, there may still be a time dependency, i.e., given that the spike does occur, it is always within a specified time range. This capability is also included in the model.

The following paragraphs provide a more detailed explanation of the transient model operation. After this discussion, an example calculation is presented and discussed.

# Transient Model: Determination of Number of Spike Events

For the purpose of the following discussions, it will be assumed that the current mission phase, denoted as IMP for load variable IR, has already been determined to be of type 4 (Poisson model) or type 5 (Uniform model). These parameters are input as MP(IR,IMP) and are discussed in the users manual input description in more detail. The operation of the model for the quasi-steady and steady-state type of mission phases is unaffected by these new changes.

The first step in the load model calculation is the determination of the number of spike values seen during the mission phase. To calculate this number, three options are available to the user: (1) a Poisson arrival rate model, (2) a uniform arrival rate model, and (3) a fixed time-of-arrival model. The Poisson arrival rate model is obtained by inputting MP (IR, IMP) equal to 4, while the uniform model is obtained with MP (IR, IMP) equal to 5. The definition of the subsequent inputs changes, depending upon the value of the MP(IR, IMP).

The parameter needed as input for the Poisson arrival model is the mean arrival rate, called RAMDA(IR,IMP) in the program. This is equal to the mean number of spike events per mission phase time period. Thus, if there are 3 spike events, the average for mission phase IMP, and the phase is 5 sec long, then RAMDA(IR,IMP) is equal to 0.6 (3 events/5 sec).

The Poisson model does not have an upper bound on the number of events which can occur. For example, the values given in the previous paragraph where the mean arrival rate is 3, there is approximately a 3.4% probability that there will be seven or more events occurring in the 5-sec interval. Since this can lead to physically unrealistic scenarios and mission profiles, an option for a two-sided distribution was believed to be necessary. For some load variables, there will never be more that N events during the mission phase, and zero will always be a lower bound\*, a uniform distribution is included to provide both an upper and a lower bound to the calculations. When MP(IR,IMP) is equal to 5 the uniform distribution is chosen. For this case RAMDA(IR,IMP) is equal to N+1, i.e., the maximum number of events which can occur plus one.

Finally, there should be a method for handling spike events which always occur but have some variability about either the nominal spike amplitude or the time of occurrence. This is input as NFIX(IR,IMP) greater than zero.

<sup>\*</sup>Although, it may not be the maximum lower bound.

These are the only parameters which are needed to determine the number of spike events which occur during the transient mission phase. The next step is to determine when the event occurs.

## Transient Model: Determination of Timing of Spike Events

The timing of the spike events must rely on some basic information about the mission phase definition. The previous transient model assumed that the spike event began and ended with the beginning and ending of the mission phase definition. This implies that the spike width is equivalent to the mission phase length. The new model allows for multiple peaks within the transient mission phase. However, this implies that the information about the spike width is lost. There are several options for dealing with the replacement of this information, but the one chosen for this model development is to input the nominal spike width and leave it fixed throughout the current mission phase. If the spike width changes dramatically from peak to peak, then two approaches may be considered. The simplest approach is to divide the current mission transient phase into multiple mission phases in which the spike width can be considered constant. The second option is to make the spike width a random variable. This option requires information more detailed than the approximate nature of the model warrants. Therefore, the second option is not contained in the current version of ANLOAD. It can be added later if new data or information indicates that this is the better method.

The information on the spike width is input in the array denoted WIDTH(IR,IMP). The width of the spike is then constant for this mission phase time period, defined by the start time STIME(IR,IMP) and the end time ETIME(IR,IMP).

The start of the spike transient event is obtained in two different ways, depending on the type of model used for the transient load modeling. For the uniform model, the spike transient can occur with equal probability in the mission phase time interval defined by ETIME(IR,IMP)-STIME(IR,IMP). For the

Poisson model, the arrival of the spike transient is given by a Poisson distribution with the mean time of occurrence equal to (1/mean arrival rate). This model will more likely cause the spike values to occur earlier in the mission phase than later in the mission phase. This is intuitively correct since one expects less of a departure from the nominal engine conditions as the mission phase is leaving the transient regime and approaching a quasi-steady or steady-state operating condition.

The previous description relates to how the initial spike transient peak is placed in the mission phase time interval. Because there is some probability that more than one peak can occur, one must decide if the peaks can overlap or if there is some time delay before the next spike transient value can occur. This is done by inputting the number of spike widths that must pass before the next peak can occur, denoted IDLAY in the ANLOAD program. If IDLAY is zero, then peaks can overlap. This will cause a masking of peaks so that multiple peaks may actually appear as single peaks. This can lead to a reduction in the calculated variance.

The amplitude of peak values is calculated after the timing of the peak occurs. This is done to reduce the array storage requirements in the program. Since peak amplitudes are calculated at each time interval, there is no need to store their values. The calculations proceed by calculating the first four moments of the load amplitudes. These moments are then sent to the distribution fitting subroutine and the best fit distribution is used to summarize the results on the output file.

# Transient Load Model Sample Calculation

A sample problem which uses all of the available options was run. This was not meant to be a physically realistic run, but rather was used to demonstrate the options. All mission phases were constructed to be 5 sec in duration. The Poisson arrival rate in each case where this model is used was 0.6, i.e., a mean arrival rate of three events per 5-sec interval. The spike width for all cases was given as 0.25 sec and a delay time of two spike widths (0.5 sec) was used. Subsequently, five mission phases were defined. The first phase used the Poisson model with no fixed spikes. The second phase used the Poisson model, but the spikes were forced to occur in a Gaussian distribution of about 12.5 sec with a standard deviation of 0.25 (this is the NFIX less than zero option). The fourth phase was the final transient phase and used the uniform model with the maximum number of peaks equal to 3. The final phase was a quasi-steady state phase which went from 65% to 104% power levels. The fifth phase was included to check that there was a correct time phasing between the models. Figure 5.1 shows the results of mission phases.

As Figure 5.1 indicates, the transient model appears to be working well. The Poisson Model shows peaks occurrence in the expected manner. The second mission phase, between 5 and 10 sec, shows the variance getting smaller near 7.5 and 8 sec. This is expected because there are two fixed peaks at those times when mean time of occurrence is equal to these values. The uniform model, used between 15 and 20 sec, also behaves as one would expect, since the time of a peak occurrence is likely to occur equally anywhere in this phase.

The third phase is where the number of peaks behaves similarly to a Poisson arrival rate model, except that the timing is within a specified distribution, is expanded and shown in Figure 5.2. In this figure, one can more clearly see the load prediction follows the base curve with no variation until 11.75 sec. At this time, the load shows a sharp increase and associated variability. This ends at 14.0 sec. This is precisely the expected result. Since 11.75 sec is three standard deviations away from the mean time occurrence, it would not be likely to see any spike values occurring until after that time. The peak at 12.5 sec is exactly where it should be and the smaller peaks at 13.0 and 13.5 sec are also seen. Therefore it is concluded that the model is working as planned.

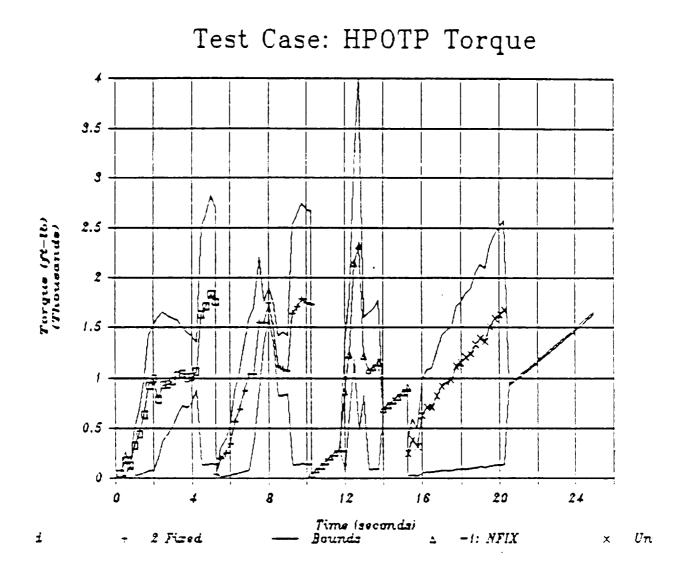


Figure 5.1. Sample Transient Calculation: Five Mission Phases

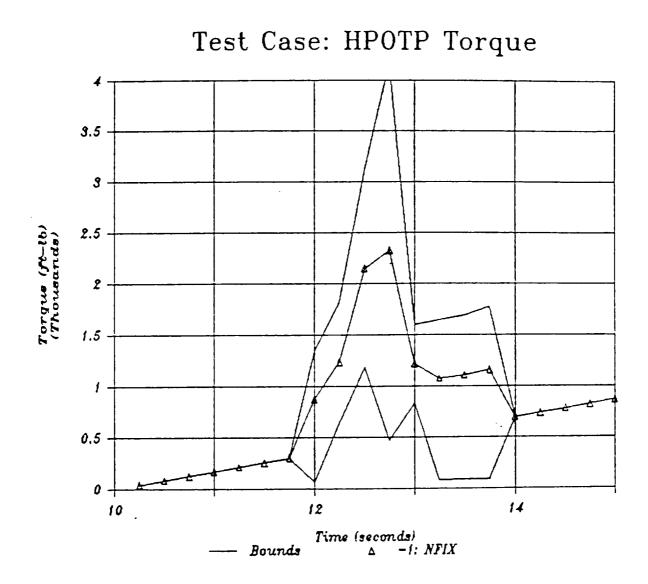


Figure 5.2. Poisson Transient Model With NFIX = -1

As a final test case, the entire probabilistic load model was run using the Poisson transient model with no fixed spikes from 0 to 2.5 sec, and a quasisteady state calculation from 65% to 104% power from 2.5 sec to 10 sec. These results are shown in Figure 5.3. Again, the model behaves as expected.

### 5.4 Validation Studies

#### Introduction

The latest version of the probabilistic load model must have validation studies performed on the code to insure that the methodology is performing as intended. The verification of probabilistic methodologies can only take place under limited testing conditions. The limitations on verification conditions arise because there are very few distribution types which can have an analytical solution derived for a specified combination of distributions. Additionally, dependent variables, nonlinearities, etc., all provide conditions for which only bounding types of solutions are available.

There are two probabilistic methods which must be validated: RASCAL and Monte Carlo. The validation analyses, which has been performed, involve only normal distributions. It is believed that if the probabilistic model can produce accurate results in comparison to the theoretically calculated values for normal distributions, then it will also produce accurate results for nonnormal distribution types. This is clearly the case for lognormal distribution since it is a simple transformation of the normal algebra. For most other distribution types, it would be necessary to run Monte Carlo analyses to check the RASCAL results. This does not seem to be valid use of the available resources: if RASCAL compares well with Monte Carlo for normal distributions then it will also compare well with Monte Carlo when non-normal distributions are used. This is because, in limitations where the number of intervals used for RASCAL approaches infinity, RASCAL methodology becomes the Monte Carlo method. Therefore, only normal distributions are used in validation studies for probabilistic methods.

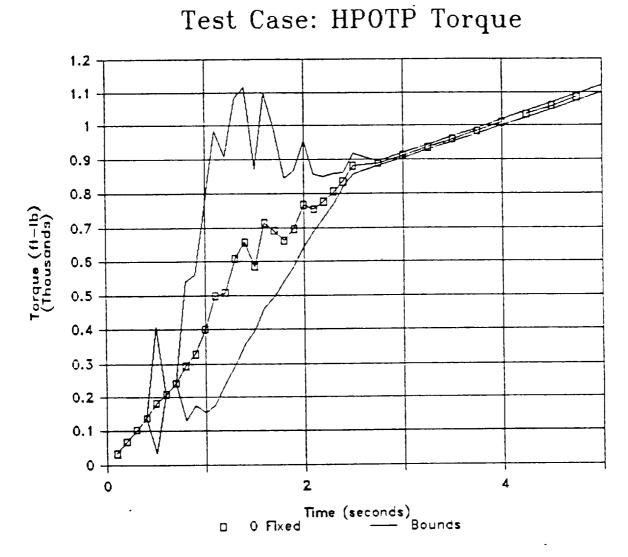


Figure 5.3. ANLOAD Calculation For HPOTP Torque

There are three case studies which were employed. These are:

Case Study I. Sum Of Three Normal Distributions: Y = A + B + CCase Study II. Product Of Three Normal Distributions: Y = ABCCase Study III. Sum And Product Normal Distributions: Y = A + BC

In all three studies, the mean and variance of random variables A, B, and C are those given in Table 5.1. Using the algebra of normal distributions, it is straightforward to calculate the mean and variance of combinations in these distributions. These results are also shown in Table 5.1. These are the theoretical values of the mean and variance which both the Monte Carlo and RASCAL methods should reproduce accurately. In addition, if the distribution for Y is also normal then it is possible to compare the CDF, which one obtains from the computer analyses, to the theoretical distribution. These comparisons are made in the following discussions.

TABLE 5.1. MEAN AND VARIANCE OF RANDOM VARIABLES FOR VERIFICATION STUDIES

<u>Variable</u>	Mean	<u>Varianc</u> e			
А	10.0	1.0			
В	10.0	4.0			
С	10.0	9.0			
Y=A+B+C	30.0	14.0			
Y = ABC	1000	380.705			
Y=A + BC	110.	36.5650			

#### <u>Case Study I. Sum Of Three Normal Distributions: Y = A + B + C</u>

The sum of three normal distributions with parameters given in Table 5.1 results in a normal distribution in which the mean value is equal to the sum

of the three means and the variance is the sum of the variances. Therefore, it is possible to exactly calculate the resulting distribution. This is a normal distribution with a mean of 30.0 and a variance equal to 14.0. The results of RASCAL calculations are shown in Figure 5.4. In this figure, the squares represent RASCAL results when equal probability intervals are used. The plus signs represent the results when an equal space interval (between the first and 99th percentile values) option is used. As the figure readily demonstrates, RASCAL calculation is very close to the theoretically correct result.

Figure 5.5 demonstrates the key difference between RASCAL calculations and the Monte Carlo Method. In Figure 5.4 the Monte Carlo results were not shown because they are also as close to the theoretical line as the RASCAL results were over the entire CDF scale. However, in the expanded view shown in Figure 5.5, one can see that the Monte Carlo result does not perform as well in the upper tail region as the equal space RASCAL result. For these calculations, the Monte Carlo analysis used the same number of sample points as did the RASCAL analysis (1000). The error bars on the Monte Carlo result (ref. Figure 5.5) represent the 95% confidence intervals. Thus, in the Monte Carlo analysis, there are three points shown above the eighty percentile value that will not encompass the theoretically correct line 95% of the time. This is an important point to makein the calculation of confidence limits with the Monte Carlo method. The confidence limits calculated with Monte Carlo do not imply that 95% of the time the confidence limit will encompass the true result: rather they imply that if the Monte Carlo analysis is repeated, that 95% of the time the Monte Carlo result will lie within the error band. While RASCAL does not currently have an analogous calculation for confidence limits, the ability to sample more frequently in the tail region will insure that the prediction will be closer to the true result than a standard Monte Carlo analysis.

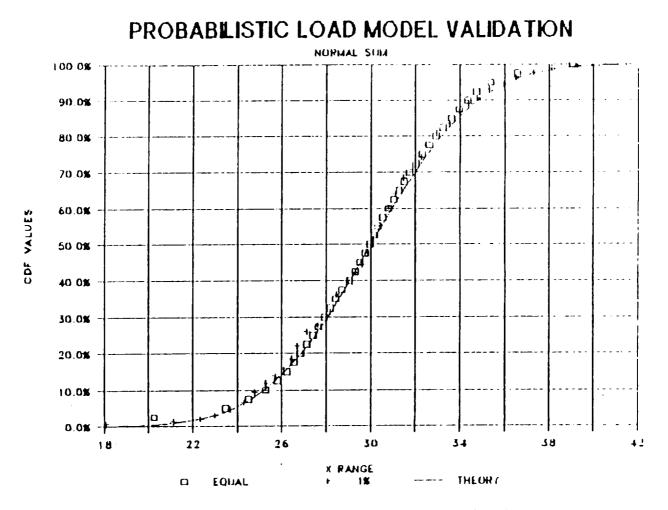
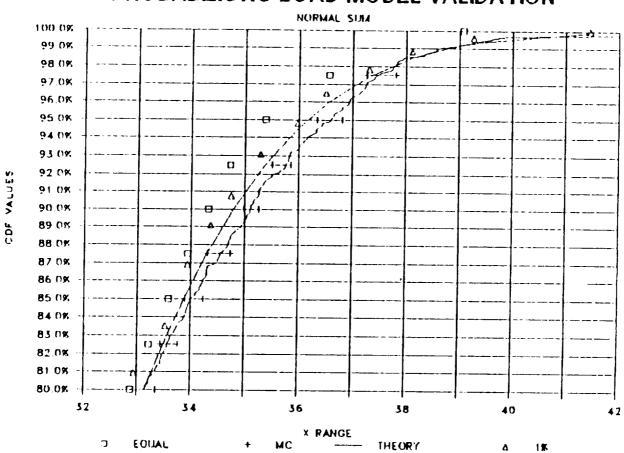


Figure 5.4. Case Study I: Sum of Three Normally Distributed Variables



PROBABILISTIC LOAD MODEL VALIDATION

Figure 5.5. Case Study I: Upper Tail Values For Normal Sum

# <u>Case Study II. Product Of Three Normal Distributions: Y = ABC</u>

In this study, RASCAL, Monte Carlo, and other theoretical results are compared for a product of three normally distributed random variables. In computing a product of three normal distributions the variance component increases as a function of both the mean squared value and the variance of inputs so that the spread in the dependent distribution is much larger than the case in which the sum is used. Figure 5.6 shows the results of the CDF calculation for RASCAL and normal distribution calculations. The expanded view of the upper tail region, which also includes the Monte Carlo result, is given in Figure 5.7. Again, the results are similar to Case I, however, the equal probability calculation appears to actually perform better than the equal space calculation. This is caused by the sampling procedure, i.e., this is an unlikely scenario that, on the average, we do not expect to see repeated. In either case, RASCAL methodology performs as well as, or better than, the Monte Carlo given the same number of sample points.

# <u>Case Study III.</u> Sum And Product Normal Distributions: Y = A + BC

The final case study looks at an algebra of normal distributions in which both a product and a sum are included. Results similar to Case I and II are shown in Figures 5.8 and 5.9. The conclusions to be drawn from these figures are the same as those previously stated. That is, the Monte Carlo and RASCAL methods perform well when compared to the theoretically correct results with the RASCAL results being as good as, or better than, the Monte Carlo calculation for the equivalent number of sample points.

#### SUMMARY

The validation of probabilistic methodologies has been performed. The comparison of simulation methods, RASCAL and Monte Carlo, to theoretically available methods has demonstrated good statistical agreement among results. The methods provide the user with parameters that can control the accuracy,

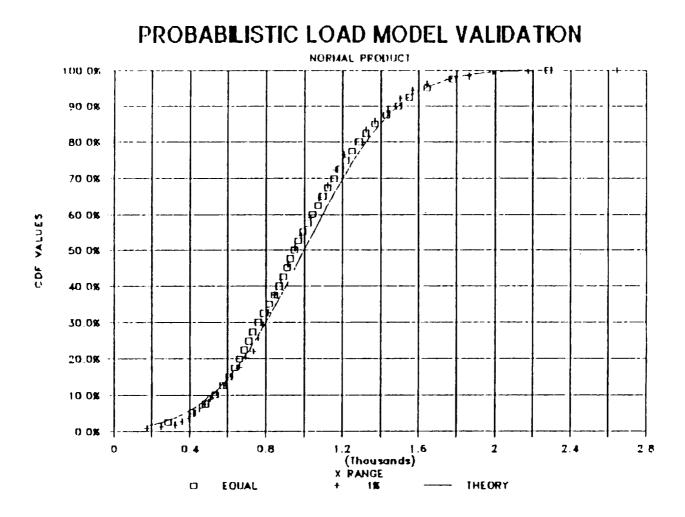
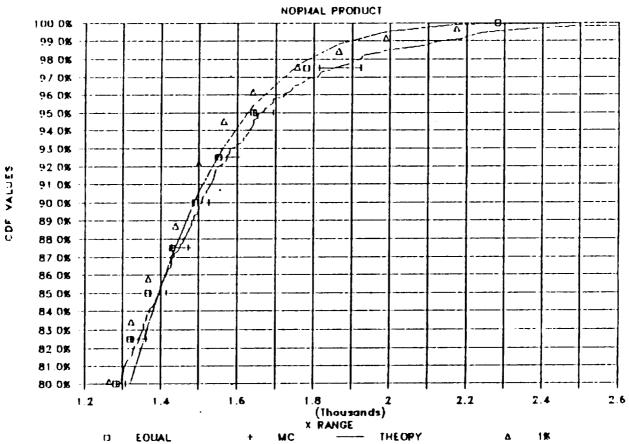


Figure 5.6. Case Study II: Product of Three Normally Distributed Variables



# PROBABILISTIC LOAD MODEL VALIDATION

Figure 5.7. Case Study I: Upper Tail Value For Normal Product

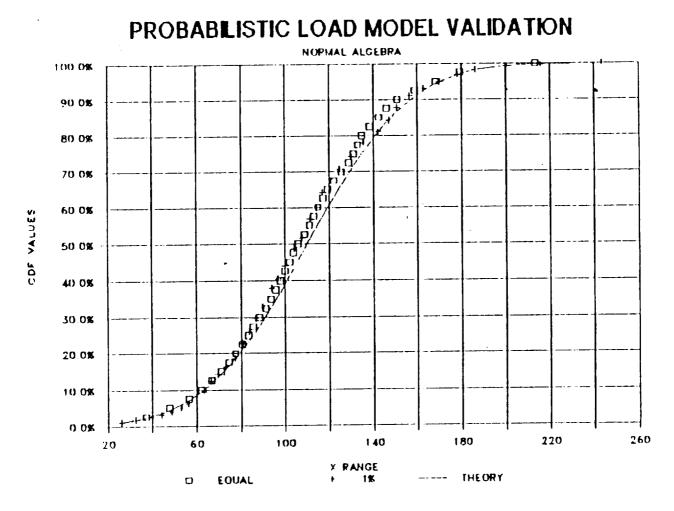
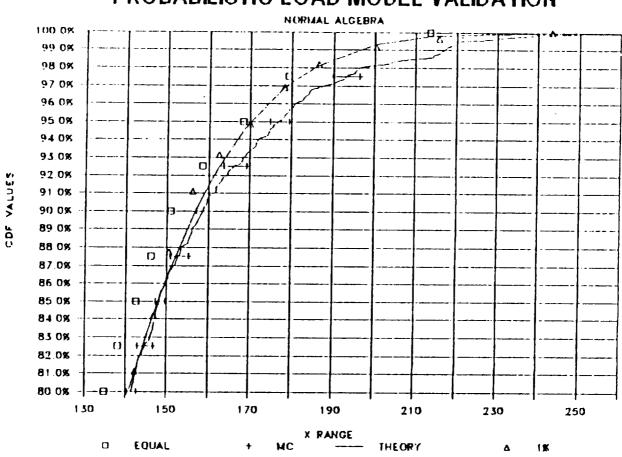


Figure 5.8. Case Study III: Algebra of Three Normally Distributed Variables



PROBABILISTIC LOAD MODEL VALIDATION

Figure 5.9 Case Study III: Upper Tail Value For Normal Algebra

as well as the confidence, of the predicted results. The next chapter investigates more fully the question of the accuracy of probabilistic methodologies.

#### 5.5 VERIFICATION STUDIES

#### INTRODUCTION

Ultimately, the probabilistic load model must be able to predict, within the limits of statistical accuracy, the behavior of loads in a space propulsion engine. While the initial phase of this study has no requirements for the physical process to be accurately modeled, it would be foolhardy to proceed without considering such processes. Therefore, the probabilistic model is driven by the influence function coefficient model and can be used to compare to the data received from flight and test stand data. The results of such comparisons are called verification studies. These analyses are used to calibrate the current status of the model, as well as indicating where additional effort was needed during the second phase of this program.

There are a variety of data sets available from the SSME test program and the subsequent flight data. There is limited data contained in the current expert system database for other engine types. Therefore, at this time, the validation studies are limited to SSME type engines. As the database is expanded, additional verification work will be performed.

For the available data sets and influence function data sets, there were five engine variables which were identified as being statistically valid for verification studies. The engine variables are listed in Table 5.2 and include the H2 mass flow rate, LOX mass flow rate, OPB discharge temperature, HPOT discharge temperature, and LPOT turbine shaft speed. These five variables were chosen for two reasons: (1) there was a match between the available data and the dependent variable list from the influence functions, and (2) there was a statistically significant number of data points available

# TABLE 5.2. ENGINE VARIABLES INCLUDED IN THE VALIDATION STUDIES H2 MASS FLOW RATE LOX MASS FLOW RATE OPB DISCHARGE TEMPERATURE HPOT DISCHARGE TEMPERATURE LPOT TURBINE SHAFT SPEED

for analysis. There is a significant difference in the type of loading associated with each of these engine variables.

The data that was obtained for use in the verification studies is the 10-sec averaged data set from both the test stand and flight databases. The test or flight data identifiers, together with the engine and component identifiers, are contained in Tables 5.3 and 5.4, respectively. These data are compared to results obtained from the ANLOAD program in the following sections.

### EXAMPLE SPACE SHUTTLE MAIN ENGINE ANALYSES

#### <u>Introduction</u>

The comparison of the ANLOAD and data requires that the influence function data set and the data set that is being examined be carefully scrutinized. As will be shown below, the slightest bias in the prediction from the influence coefficients can cause results of the probabilistic model to appear to be skewed. It is also important to note that the influence function model is based on an engine balance computer simulation model assuming in-flight conditions. This is in contrast to selected tests which are purposely set to limit state-type conditions that would be unacceptable sets of engine parameters for actual flight. Therefore, after examining this point in some detail below, the mean predictions will be shifted to match the data set so that the probabilistic results can be examined efficiently.

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# TABLE 5.3. TEST DATA USED IN VERIFICATION STUDIES

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Test No VE 901-391 901-413 901-414 901-427 901-438 901-438 901-438 901-438 901-438 901-438 901-438 901-438 901-447 902-307 902-311 902-311 9022-311 9022-313 9022-313 9022-313 9022-313 9022-313 9022-313 9022-313 9022-313 9022-313 9022-335 9022-335 9022-335 9022-335 9022-3446 9022-34467 9022-34467 9022-3455 9022-3455 9022-3455 9022-3455 9022-3455 9022-3555 9022-3555 9022-3555 9022-3555 9022-3555 9022-3555 9022-3555 9022-3555 9022-3665 9022-3665 9022-3665 9022-3665 9022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-3655 90022-36557 9002-3655757 90022-36557 9002-3655	SH I C-1 A - 1 A - 2 C C C C C C C C C C C C C C C C C C C	PCS EN	NGINE NO 2011 2012 2013 2017 2019 2019 2019 2019 2019 2019 2019 2019	DU00 51350 5555555555555555555555555555555	$\begin{array}{c} 104 \\$	PWE         HD           2016         2019           20107         2018           2020         2020           2010         2011           2011         2011           2011         2011           2011         2011           2011         2011           2011         2011           2011         2015           2025         2025           2025	BCC           20162           40002           2011           2012           2013           2014           2019           2019           2019           2019           2019           2018           2019           2019           2018           2019           2018           2019           2018           2019           2019           2018           2019           2018           2019           2018           2019           2018           2019           2018           2019           2018           2019           2018           2015           2015           2015           2015           2015           2015           2015           2015           2015           2015           2015           2015           2015           2015           2015	2011 2011 2011 2011 2011 2011 2011 2011	F-11775769986000 F-1277576998600 FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF	HPFTP 2214B1 0209 2314 5101B1 2415 9210 4002 5102E1 9011 2016B1 2017B1 9210 5105 5101 2018 2019 4001 2020B1 2020B1 2020B1 2020B1 2020B1 2020B1 2010 4001 2020B1 2018 2019 4001 2020B1 2018 2019 4001 2020B1 2018 2019 2010 5105 5101 2018 2019 2010 2010 2010 2010 2010 2010 2010	LFFTP 9106 400181 400181 2117 9206 2118 2022 910581 910582 910582 910583 2118 910583 2118 910581 910581 2118 2118 2118 2118 2118 2118 2118 2	HPOTP 9010 9211 0310 9010E1 2019 2022 2022 9505E2 2016 9010 2019 2029 2020 2020 2020 2020 2020	LPCTF \$005 2016 2017 2010 2010 2010 2022 2021
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# TABLE 5.4. FLIGHT DATA IN VERIFICATION STUDIES

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## Comparison Of Probabilistic Predictions And Data

Figure 5.10 shows the predicted fuel mass flow rate and the empirical CDF constructed, using all of the data from both test stands and flights. The ANLOAD prediction was obtained using the RASCAL method. In each of these RASCAL analyses, 40 discrete intervals were used and 25 samples per interval were obtained. Also, the RASCAL method was used by requiring that the input PDFs were calculated between the 1 and 99 percentile values.

The independent, or input, variables used in these analyses are the first five independent variables from the influence function list: the commanded mixture ratio, fuel inlet total pressure, oxidizer inlet total pressure, fuel inlet temperature, and the oxidizer inlet temperature. These independent parameters were chosen because they introduce the most variability in predicted results and previous analyses have characterized their PDF forms. The inputs used are contained in Table 5.5.

TABLE 5.5.	INDEPENDENT ENGINE	VARIABLE PDF PA	RAMETERS
Independent Variable	Distribution	Parameter 1*	Parameter 2**
Commanded Mixture Ratio	Uniform	5.97443	6.05108
Fuel Inlet Pressure	Normal	30.0	1.5
Oxidizer Inlet Pressure	Normal	64.3341 .	21.0374
Fuel Inlet Temperature	Lognormal	3.61308	0.0162595
Oxidizer Inlet Temperatu	re Lognormal	5.10174	7.19274E-03

\*Parameter 1 is the lower bound for a uniform distribution, the mean for a normal distribution, and the modal for the lognormal.

<sup>\*\*</sup>Parameter 2 is the upper bound for a uniform distribution, the standard deviation for a normal distribution, and the transformed standard deviation for the lognormal.

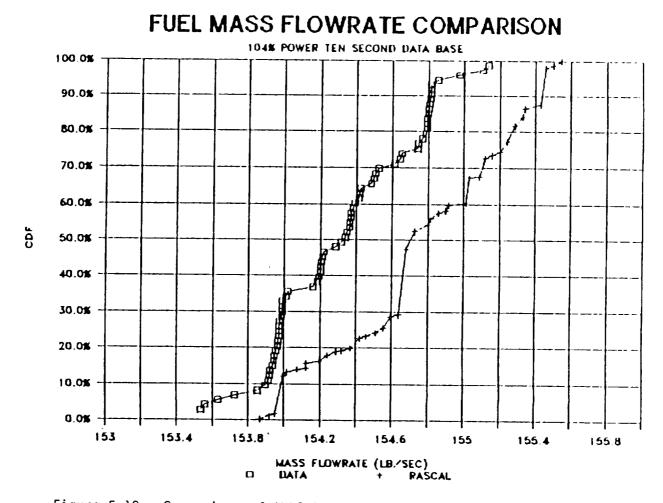
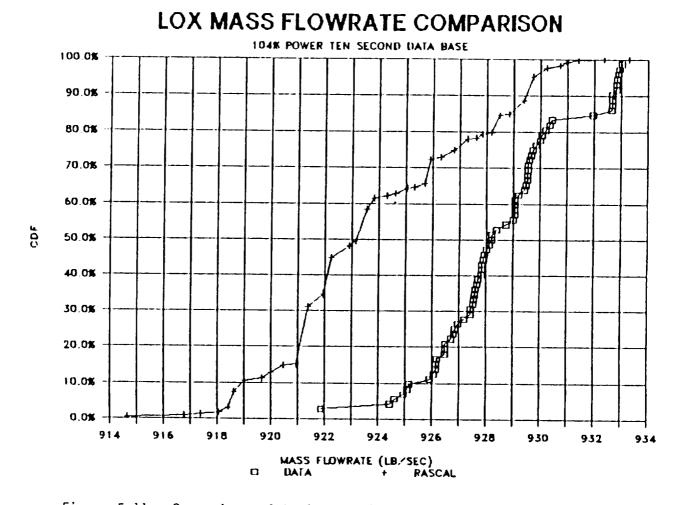


Figure 5.10. Comparison of ANLOAD Prediction and Data For Fuel Mass Flow

As Figure 5.10 indicates, the general shape of both CDFs are the same but the ANLOAD prediction is shifted to the right. Figure 5.11 shows a similar result for the LOX mass flowrate. Figures 5.12, 5.13, and 5.14 do not show the pronounced shift that the previous two figures indicated, but there is an obvious bias in the prediction for the OPB and HPOT discharge temperature. This bias does not appear as a skewness in the CDF but rather is a uniform shift of data.

There are two possible explanations for this shift.\* One explanation is that the influence coefficients are not sufficiently accurate in their prediction of engine variables. The other is that the data sets have a built-in bias. This bias can arise because the ANLOAD predictions are based on combining inputs from which distributions are calculated from a data set which is different from the data used to compare dependent variable results. The first explanation is believed to be the more plausible. There is some error associated with the use of the influence functions: by definition they are approximations to the detailed analysis. If the predicted average values and the averages calculated from the data are compared (ref. Table 5.6), it is quickly seen that these values are all within 1.0% of each other. This implies that the influence functions are predicting absolute values of five engine variables correctly, within the 1.0% error. To some extent, the shift seen in Figures 5.10 through 5.14, especially in the 20 to 80 percentile ranges, is also caused by the use of RASCAL in which the lower and upper tail regions are calculated more accurately. (Remember that 40 discrete intervals would lead to estimates between the 2.5 and 97.5 percentile values while the input required analyses between the first and 99 percentile values). Figures 5.15 and 5.16 show this increased accuracy in the upper tail regions for two of the five engine variables.

<sup>\*</sup>The possibility of an incorrect results from ANLOAD is discounted because of validation studies reported in the previous section.



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Figure 5.11. Comparison of ANLOAD Prediction and Data for LOX Mass Flow

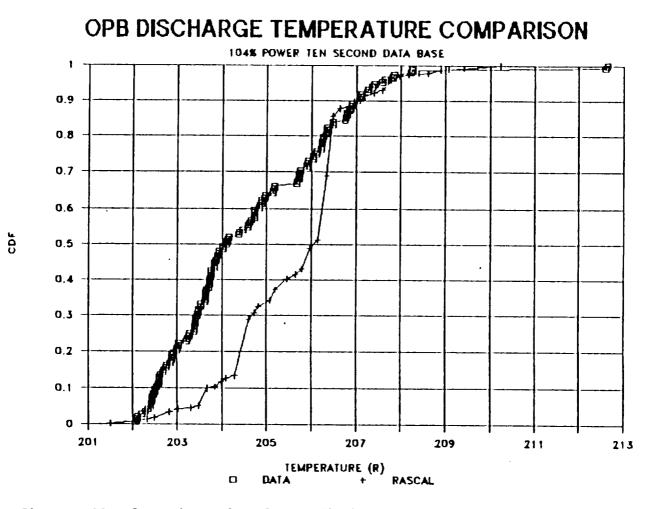


Figure 5.12. Comparison of ANLOAD Prediction and OPB Discharge Temperature

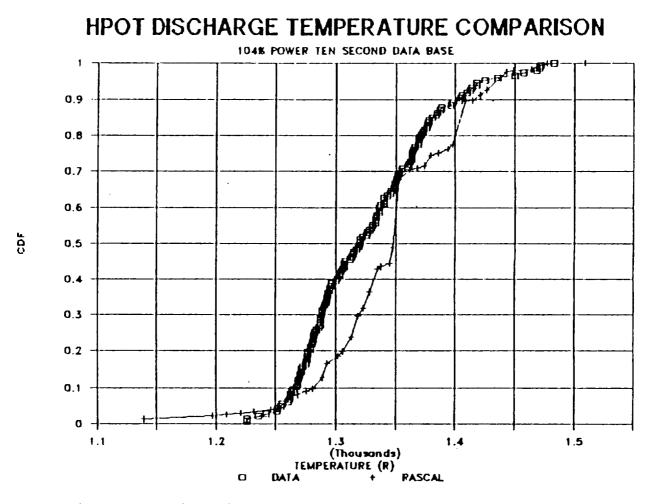
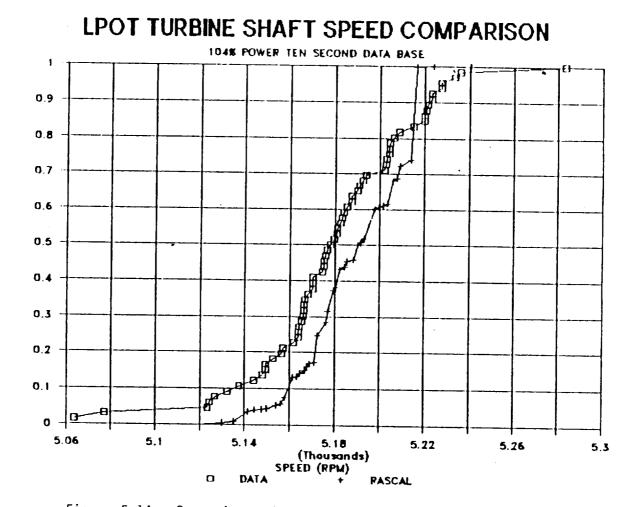


Figure 5.13. Comparison of ANLOAD And HPOT Discharge Temperature



CDF

Figure 5.14. Comparison of ANLOAD and LPOT Turbine Speed

TABLE 5.6.	CALCULATED	AND	PREDICATED	AVERAGE	VALUES	FOR	ENGINE	ANALYSES
				A CHARGE	MEDES	I UN	CHOTHE	MMALISES

	ANALYSIS METHOD						
	MONTE CARLO	RASCAL EQUAL	RASCAL EQUAL	DATA: FLIGHT	DATA: TESTS		
LOX Mass Flow Rate Mean Value Standard Deviation Coefficient of Variation Error in Mean (Flight)	930.745 1.359 0.15% -0.32%	930.740 1.438 0.15% -0.32%	924.018 3.641 0.39% 0.40%	927.721 1.492 0.16% NA	929.849 2.745 0.30% -0.23%		
<u>H<sub>2</sub> Mass Flow Rate</u> Mean Value Standard Deviation Coefficient of Variation Error in Mean (Flight)	154.711 0.499 0.32% -0.27%	154.671 0.500 0.32% -0.24%	154.704 0.475 0.31% -0.26%	154.294 0.300 0.19% NA	154.347 0.431 0.28% -0.03%		
<u>OPB Discharge Temperature</u> Mean Value Standard Deviation Coefficient of Variation Error in Mean (Flight)	205.925 1.642 0.80% -1.09%	205.967 1.567 0.76% -1.11%	206.001 1.540 0.75% -1.13%	203.676 1.436 0.71% NA	205.215 1.284 0.63% -0.75%		
LPOT Shaft Speed Mean Value Standard Deviation Coefficient of Variation Error in Mean (Flight)	5181.90 15.255 0.29% -1.00%	5180.24 15.785 0.30% -0.96%	5180.66 16.125 0.31% -0.97%	5130.26 2116.561 41.26% NA	5184.05 30.326 0.58% -1.04%		
HPOT Discharge Temperature Mean Value Standard Deviation Coefficient of Variation Error in Mean (Flight)	1349.79 20.551 1.52% -3.82%	1350.38 21.353 1.58% -3.87%	1298.18 75.929 5.85% -3.79%	1298.18 22.907 1.76% NA	1272.44 16.053 1.26% 2.07%		

To correctly remove the bias from the data and make direct comparisons of CDF values, it is necessary to rerun the analyses using equal probability intervals. Equal probability intervals are needed in order to subtract the bias in the results without changing the distribution shape. Thus, if the difference in the mean value calculated from the data and the predicted mean value from the ANLOAD calculation is subtracted from each of the dependent engine variable's DPD, then the predicted standard deviation will remain constant. This then allows the predicted CDF to be shifted left or right without affecting the shape of the distribution. If unequal probability intervals are used, then this simplified modification to the results is not possible and comparisons are difficult.

These analyses were performed, again using RASCAL, but with 25 discrete intervals used to describe each of the five input CDFs.

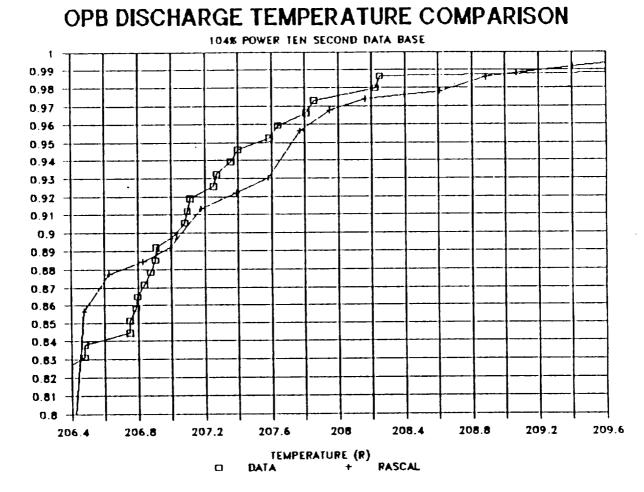
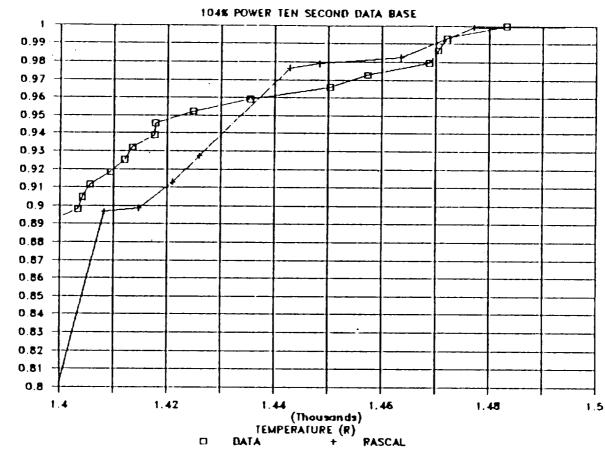


Figure 5.15. Upper Tail Comparison For OPB Discharge Temperature



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# HPOT DISCHARGE TEMPERATURE COMPARISON

Figure 5.16 Upper Tail Comparison For HPOT Discharge Temperature

The independent parameter otherwise remained the same as the previous analyses. In addition, a Monte Carlo analysis was performed for each of the five dependent variables so that confidence limits on the predictions could be obtained. This was also done to demonstrate the fact that the RASCAL methodology, with equal probability intervals, is not causing any shift (systematic or otherwise) in the predicted CDF values.

The results of the calculations when all of the data are plotted as a single CDF value is similar to the previous analyses and are not reproduced here. The form of the CDF is similar for both the predicted and calculated data values but there is still much more variability in the data than is being predicted by the ANLOAD results. To explain this inconsistency, the data was examined in many ways. What was determined is that the ANLOAD program agrees well with the flight data and exhibits less variability than the test data. This is shown graphically in Figures 5.17 through 5.26. For example, in Figure 5.19, the LOX mass flow rate from the flight has a standard deviation of approximately one-half of that from the test data. This is to be expected since flight conditions are much more tightly controlled than the possible range of conditions that the designers of an engine may want to retest to certify the engine performance. (This is not meant to imply that tests are not well controlled but that the range of conditions allowed during tests is larger than that allowed during flights). When the test data is removed from the plot (Figure 5.20), one can see how well the prediction actually matches the flight data. The LOX mass flow rate is one of the most accurate predictions, but all of the other predictions follow this same pattern. Each of the figures repeats this same pattern and indicate that the choices for input variables and influence function set reproduces the flight data in a statistically consistent fashion.

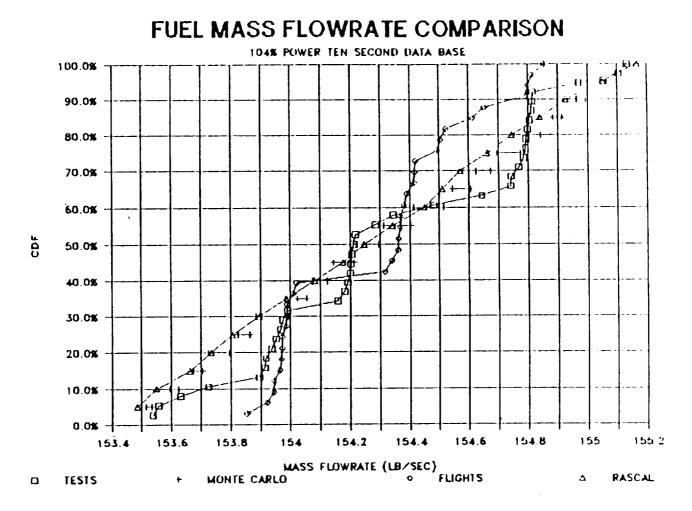


Figure 5.17 Test Data, Flight Data and ANLOAD Comparison for Fuel Flow

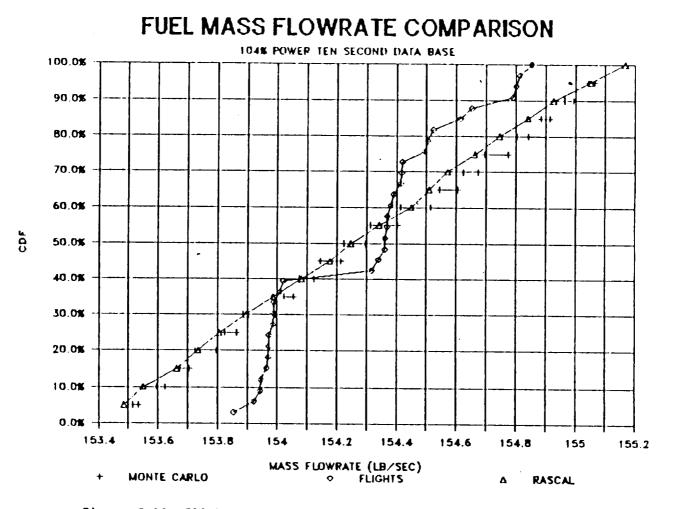


Figure 5.18 Flight Data and ANLOAD Comparison for Fuel Flow



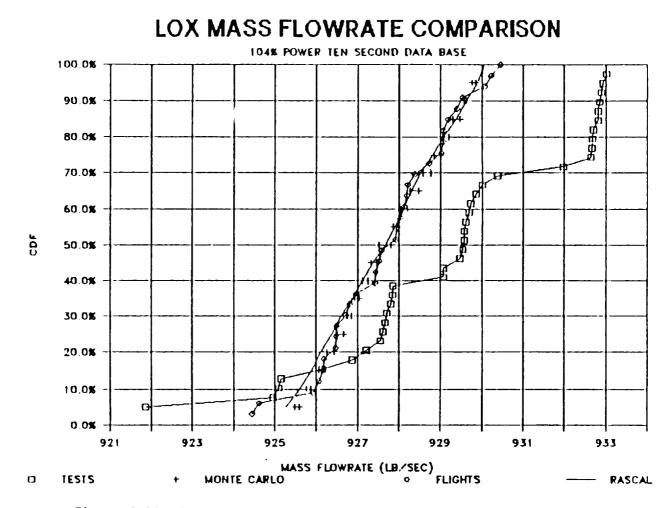


Figure 5.19 Test Data, Flight Data And ANLOAD Comparison For LOX Flow

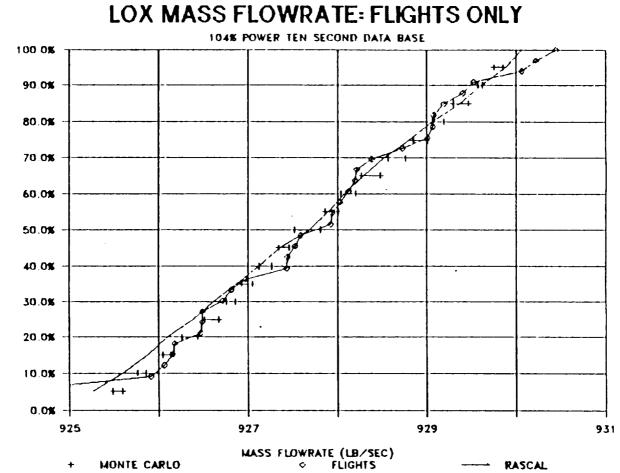
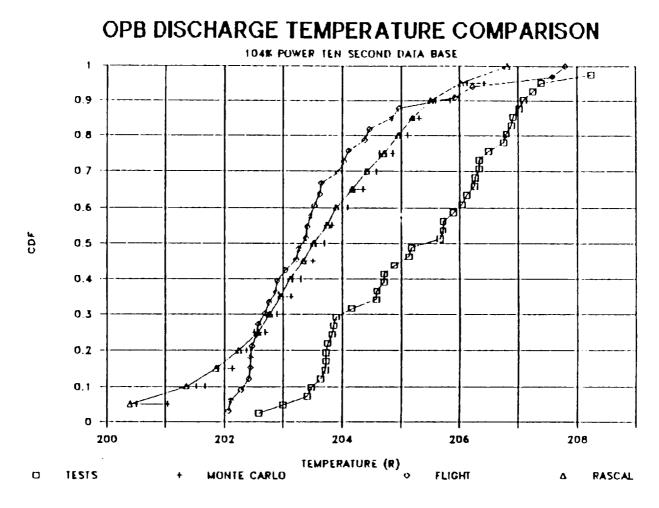


Figure 5.20 Flight Data And ANLOAD Comparison For LOX Flow





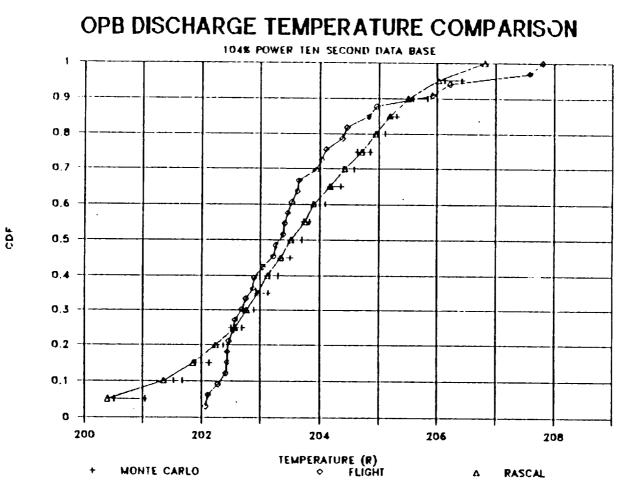


Figure 5.22 OPB Discharge Temperature Validation Using Flight Data

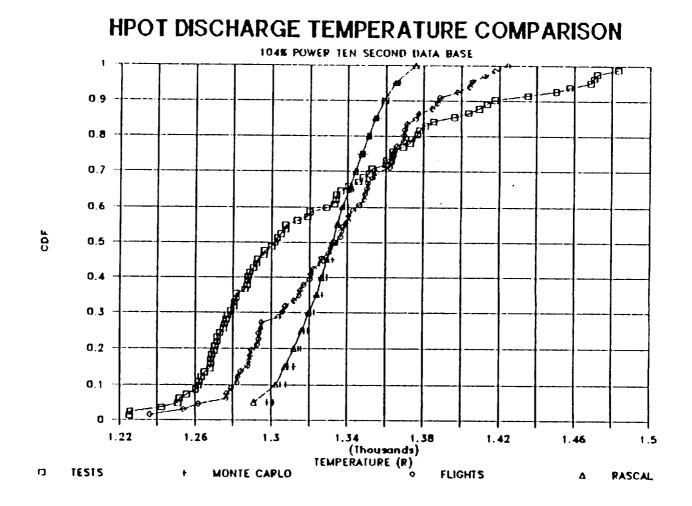
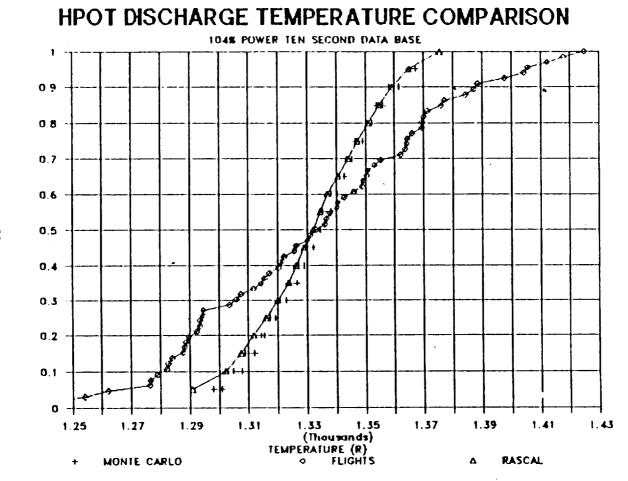
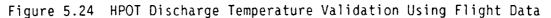


Figure 5.23 HPOT Discharge Temperature Validation Using Flight/Test Data





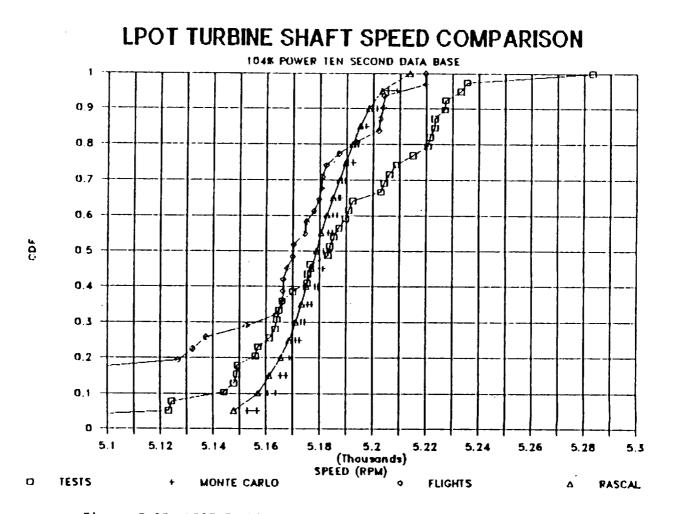


Figure 5.25 LPOT Turbine Speed Validation Using Flight/Test Data

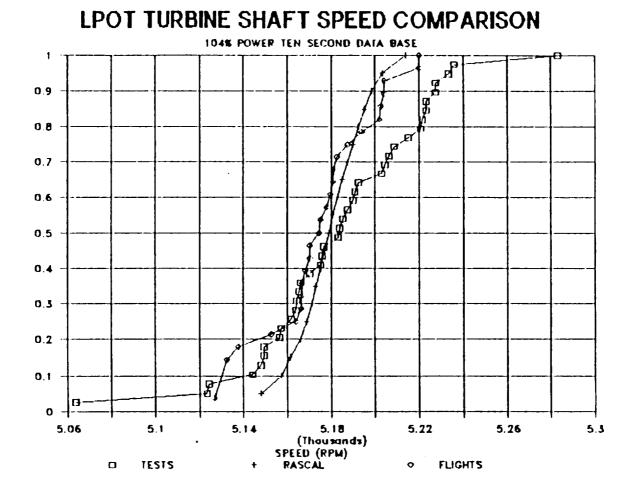


Figure 5.26 LPOT Turbine Speed Validation Using Flight Data

### Summary

The set of influence functions used to perform these calculations were derived from a nominal engine balance computer code. Since the code was assuming that the engine would not undergo severe transient behavior during flight, it was expected that the variability built into the coefficients would be minimized. This was exactly what was found. The probabilistic model contained in ANLOAD predicted the variability in flight data well, but did not predict as large a spread in the data as was seen in test data. This was also expected since the input distributional forms were derived primarily from flight data, although there was some mixing of results in the distributional fitting procedure. It is believed that the spread in the entire data set can be predicted if the input distributional forms are changed to reflect the larger variability contained in test conditions.

However, one must keep in mind the ultimate purpose of the program development: to derive an expert system model that can be employed by a relatively inexperienced engine designer. If the large variability contained in the entire data set is included in base coefficients, then unnecessarily stringent tolerances will result because the predicted variability in the load would be much larger than that which would credibly be encountered in flight conditions. Therefore, the set of coefficients and input distribution descriptions for independent loads are believed to be the best representation of the currently used space propulsion engine parameters and loads.

# 6.0 LDEXPT, The Load-Expert System

### 6.1 Objective and Approach

The objective of the CLS is to develop generic load models with multiple levels of progressive sophistication to simulate the CLS induced in space propulsion system components, representative of SSMEs. A computer code, incorporating the various individual and CLS models, is being developed to construct the specific load models desired. The approach is to develop incremental versions of the code. Each subsequent version will add sophistication to the component probabilistic load definition and decision rules. The probabilistic loads thus generated will be useful in space propulsion system design and probabilistic structural analyses.

The space propulsion system is a complex machinery. Tremendous amounts of load information and numerous engine data are being generated over the years. Probabilistic load synthesis not only demands sophisticated probabilistic methodology, but it requires knowledge of state-of-the-art space propulsion system load analyses and calculations. It encompases the knowledge of over 30 years of experience of rocket engine design, analysis and manufacturing at Rocketdyne, NASA, and other institutions. The approach for the CLS program is to develop a knowledge-based or expert system which can interface with the load calculation routines to synthesize the load spectra of a generic propulsion engine.

A knowledge-based system has the facility of building a domain knowledge base which, in a broad sense, includes decision rules, numerical data, and evaluation procedures. It has the capability to perform logical deduction and inferences and, as such, can help users make decisions and solve problems. A knowledge-base environment also allows incremental development and modularization of the knowledge. The knowledge implemented (load models, load data, or load calculation procedures) is readily available to other modules. The CLS program requires a knowledge-based system that has built-in sophisticated probabilistic modeling and statistical tools, and a large database of rocket engine information. This knowledge-based system will help engineers generate probabilistic loads for select space propulsion system components and will provide probabilistic information for structural analyses. The functions of this knowledge-based system are to manage the load information database, provide expert knowledge in load models and load synthesis, and generate user requested loads. In other words, the CLS program needs a coupled symbolic and numeric processing system. With these constraints, a knowledge-based system in FORTRAN was developed from scratch for the CLS program. The advantage of developing one's own knowledge-based system is that there is no licensing restriction. A knowledge system in FORTRAN facilitates the interface with FORTRAN probability evaluation and load calculation routines. In addition, FORTRAN programs are fairly portable and can be easily implemented into most any computer system. The disadvantage of building one's own system is that generally the user interface is primitive because of cost constraint.

# 6.2 Intelligence Database System Design

The CLS load-expert system is a hybrid knowledge-based system different from the conventional rule-based product system. The design of the CLS load-expert system follows the "knowledge is power" philosophy. That is the power of a knowledge-based system is its capability for having a vast amount of domain knowledge without the necessity of a complex inferencing scheme. A decision tree inference scheme is employed for simplicity. Each decision tree is implemented as a rule module. To facilitate the communication between rule modules, a simple working memory is implemented for passing information from one rule module to another. The load-expert system has a rule-based module and a knowledge-based module (ref. Figure 6.1). The rule-based module has many rule modules, each of which model a decision tree which performs certain tasks, such as the QLM. The QLM retrieves the load distribution data to do a Gaussian moment method calculation in order to obtain a system load distribution. A user interface module SESUIM takes care of user queries and answers. The knowledge-based module uses a database system to store and manage load

6-2

information and data, such as engine system load distribution data. The CLS knowledge-based module is similar to a simple frame-based system except that no inheritance mechanism is built into the system.

The knowledge representation in database format has proven to be the correct and viable choice. The database system manages the large volume of load information. It helps maintain data integrity and avoid data redundancy. It standardizes the data storage and retrieval procedures. It facilitates the communication between the expert system rule-based module and the knowledge base. The CLS approach is to couple the knowledge-based system to a genuine database system which can retrieve and update records, add and delete.records, etc. not just a data file, to become an intelligence database system. This approach has demonstrated in this project to be excellent for engineering applications.

The large volume of domain knowledge in data format almost dictates the use of a database system. Writing rules to manipulate the data intelligently, to select and utilize the relevant data in computations increases the power and flexibility of a database system tremendously. Such an intelligent database system is the system being built for the CLS program. Our experience on the system is that the system does well what it intended to do and we are satisfied with the design of the system.

6.3 Knowledge Engineering

Knowledge engineering is the most important task for building a knowledgebased system. Generally, one or more experts are available who know how to solve the problems at hand. In this case, the knowledge engineering task is to extract the knowledge from the expert(s) to transform into rules or other forms that can be implemented on a knowledge-based system. Things are a little more difficult for a research project such as the CLS program. Here, new methodology needs to be developed. First, probabilistic methods need to be implemented. The methodology is available, but the application of the methodology to mechanical loads requires research effort. Next, probabilistic load

models for space propulsion system and components need to be developed. There is a vast amount of knowledge on space propulsion system design and load evaluations accumulated at Rocketdyne. Most of the analyses, however, are using deterministic models and algorithms. The probabilistic load modeling is at the forefront of the research. Knowledge engineering for this task includes learning how Rocketdyne experts model and evaluate the loads. Knowledge engineering also includes transformation of deterministic models into probabilistic models, utilization of the deterministic results, and development of new probabilistic models.

As an example of knowledge engineering, transformation from a deterministic model to a probabilistic model is the rocket engine influence model described in section 4. The deterministic influence model performs engine load evaluation and engine performance prediction. Transformation of the model into a probabilistic one is not as straightforward. One of the reasons is that the purpose of the probabilistic engine model is to provide engine systemdependent loads (system interface operation conditions) to be used as boundary conditions for probabilistic component load models. The deterministic model uses tag values to normalize engines for engine performance prediction, whereas the probabilistic engine model treats all engine operating variables and Nevertheless, the CLS project has benefited loads as random variables. greatly from the availability of rocket engine deterministic influence model and the depth of the Rocketdyne experience in rocket engine design, modeling Without the Rocketdyne team providing their expertise in and evaluation. respected areas, the CLS effort would be futile.

There are situations wherein there are no appropriate models available for generating a certain load. In this case, an appropriate probabilistic model needs to be invented. Such are the cases for the generic probabilistic component thermal load model and the duct fluctuation pressure load model. For example, in developing the thermal load influence model, our aerothermal dynamics expert initially did iterative perturbation analyses using a deterministic thermal analysis code. He then massaged the results and developed the thermal load influence model. The process was a lot more difficult than

6-5

described here. It relies on the expert's knowledge of component structure, geometry, and thermal environment. Selection of the system operation condition loads (system-dependent loads) which are the most influential to the component thermal load, requires in-depth knowledge of the system interaction of the component with its environment. For example, in developing the thermal load for the turbine blade temperature, coolant leakage through the worn-off seal has significant effect on the temperature profile at the turbine blade shank region.

Once a probabilistic load model was developed, it was integrated into the load-expert system. Databases for the loads and geometry information were designed and added to the knowledge base file. A rule module for the load model was coded and added to the rule-based module. Queries were written and inserted into the problem text file (query file used by the user interface driver). It is here that the advantage of an incremental development environment for the knowledge-based system is apparent. New knowledge is being added to the system. New rule modules can be built with the new knowledge as well as the information that was already in the knowledge base.

Knowledge engineering is the most crucial step in developing a knowledge-based system. The success of this program depends largely on it. The fact that there is a Rocketdyne team with 30 years of expertise in rocket engine design and development to draw from ensures Rocketdyne the highest probability of success.

# 6.4 The Load-Expert System: LDEXPT Version 2.1

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The load-expert system, LDEXPT version 2.1, was implemented on the NASA Lewis Research Center's mainframe computer. It is in the VM/CMS operating system. At the writing of this report, the load-expert system is being updated to LDEXPT version 3.0. As mention earlier, an expanded loads and influence coefficient set will be implemented. The load-expert system is an interactive system. The structure of the system is shown in Figure 6.1. The load-expert

6-6

system has a rule-based module and a knowledge-based module. The rule-based module has the user interface system SESUIM taking care of user query and answer functions. The rule-based driver RBMS controls the overall process of running a user-selected rule module, performing a load calculation with the ANLOAD module, etc. The knowledge-based module has a database system, a duty-cycle-data processing module, and a file I/O module. The database system manages the knowledge base and takes care of database functions, such as database retrieval and update. The file I/O module performs file input and output to the operating system.

# <u>The Database</u>

The database system of the load-expert system is a genuine database system. It is a flat-file database system which has most of the database operations. An index sequential access method (ISAM) algorithm is employed for the retrieval of the database records. A key file is constructed for each database table. The keys are sorted in ascending order. Records are then retrieved through the indices stored in the key file. The system can be upgraded to a relational database system if the relational algebra, such as joining (union and intersection) the database tables, is implemented. If such need arises, the relational algebra will be implemented.

Available database functions include: database table creation, record selection, record deletion, updating database tables, building key files, and saving database. The database commands of the load-expert system as follows:

COMMAND	FUNCTION
?DBCR	Create a database table
?DBCF	Create fields for a database
?DBBK	Build key file
?DBSL	Select database record(s)
?DBDL	Delete database record(s)
?DBDF	Display field and key names
?DBUP	Update and/or add database record(s)
?DBRD	Open a database file

COMMAND	FUNCTION
?DBSV	Save an updated database
?DBLT	List all records of a database table
?DBLK	List all key variables of a database
?INLD	Special command for input SSME loads
?INFL	Special command for input infl. coeffs
?HELP	List available database commands
?RETN	Return to KBMS
?QUIT	Exit LDEXPT

# The Knowledge Base

The domain knowledge for the probabilistic engine load synthesis of a space propulsion system consists of two main areas: the probabilistic methodology and modeling, and the rocket engine structural load information and evaluation. The probabilistic methods and calculation are implemented on the loadexpert system with traditional algorithmic and procedural codes. These coding routines are included in the load calculation module ANLOAD as discussed in section 5. The load information and the load model information are implemented in the knowledge base. The information of the knowledge base is utilized and processed by the rule modules. The synergism of the two domain knowledge bases and the coupling of the symbolic and numeric processing have to be brought about to a successful knowledge-based system for the CLS project.

The knowledge base of the load-expert system is managed by the database system. The knowledge base includes the following database tables:

TABLE <u>GROUP_NAME</u>	NUMBER OF	INFORMATION DESCRIPTION
LIDP	ו	System independent loads
LDEP	1	System dependent loads
INFC	16	Influence coeff's set
DFAT	١	Duty-cycle-data file IDs
LTBC	1	Turbine blade static pressure loads

TABLE <u>GROUP_NAME</u>	NUMBER OF	INFORMATION DESCRIPTION
LCTH	1	Component loads
SCTH	1	Component load models
ICTH	1	Component load scaling coeffs
DUCT	1	Duct geometries
CLFP	1	Fluctuation pressure loads

The knowledge base has engine load information and their distribution parameters as delineated in Figure 6.2 and 6.3. The engine loads can be classified by four categories: (1) system-independent loads, (2) system-dependent loads, (3) component independent local loads, and (4) the component loads. The system-independent loads include engine inlet operating parameters and engine hardware parameters. Engine inlet operating parameters are the engine mixture ratio, the fuel inlet pressure and temperature, and the oxidizer inlet Engine hardware parameters relate to hardware pressure and temperature. turbopump efficiency, turbine efficiency, and valve performance, i.e., resistance, etc. The system-dependent loads are the engine performancerelated variables and the system interface loads. Engine performance variables are the engine thrust, fuel and oxidizer flowrates, etc. Engine system interface loads are the system operating boundary condition loads, such as turbine inlet and discharge pressures and temperatures, and the HGM (Hot Gas Manifold) fuel inlet pressure. These loads define the operating conditions for system components. The component independent local loads and component loads are loads local to the components. The component local independent loads are related to geometry and other effects local to the component under consideration. An example is the coolant seal leakage geometry factor for the turbine blade. The component loads are important in structural analysis and failure probability evaluation of the particular component. Examples of the component loads are the turbine blade pressure and temperature, transfer duct static and dynamic pressures, etc. The knowledge base has the mean values, coefficients of variation and distribution type for all these loads. The information is stored in database format. Examples of the databases LIDP and LDEP are shown in Figures 6.4 and 6.5. In these databases, the load

	Independent Loads	System Level Dependent Loads	Component Level Composite Loads
6-10	<ul> <li>Commanded power level</li> <li>Engine inlet operating parameters Mixture ratio</li> <li>Fuel inlet pressure &amp; temperature</li> <li>Oxidizer inlet pressure</li> <li>&amp; temperature</li> <li>&amp; temperature</li> <li>Bump efficiency</li> <li>Turbine effeciency</li> <li>Main oxidizer valve</li> <li>resistance</li> <li>Turbine flow coefficient</li> </ul>	<ul> <li>Engine performance parameters</li> <li>Engine fuel flowrate Engine oxidizer flowrate Engine thrust</li> <li>Engine operating parameters Pump speed Turbine inlet &amp; discharge pressures</li> <li>MGM fuel inlet pressure</li> </ul>	<ul> <li>Component loads HPFTP turbine blade pressure &amp; temperature Transfer duct static pressure Transfer duct dynamic pressure LOX post temperature</li> <li>LOX post temperature</li> <li>Local independent loads</li> <li>Local independent loads</li> <li>Conposite loads for Turbine blades</li> <li>Composite loads for Turbine blades</li> <li>Tansfer ducts</li> </ul>
	Figure 6.2.	6.2. Load-Expert System Load Model Knowledge Base	wiedge Base
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Engine System Model	tem	Component Load Models
<ul> <li>Load distributions Means Means Coefficients of val Distribution types Nominal value coe Influence coefficie</li> <li>Probabilistic influence Influence coefficie</li> </ul>	d distributions Means Coefficients of variation Distribution types Nominal value coefficients babilistic influence model Influence coefficients 1 o gain values	<ul> <li>Generic static pressure scaling model</li> <li>Generic probabilistic thermal load model</li> <li>Generic turbine blade pressure load model</li> <li>Tip, mean &amp; hub cross section pressures</li> <li>Turbine blade pressure interpolation scheme</li> <li>HPFTP 2nd stage turbine blade pressure &amp; temperature loads</li> <li>2519 nodes geometry model</li> <li>Reference nodal pressures &amp; temperatures</li> <li>Turbine blade dynamic pressure load model</li> <li>Turbine blade dynamic pressure load model</li> <li>Transfer ducts, LOX posts, HPOTP discharge duct</li> <li>Transient LOX post thermal load model</li> <li>Vibration model</li> </ul>
Rockwell International Rocketdyne Division		896 - 4 -

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Figure 6.3. Load-Expert System Load Knowledge Base

89c-4-339-31

NE-COEF1 NE-COEF2 NE-COEF3 NE-COEF4 0.60000E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.30000E+02 0.00000E+00 0.00000E+00 0.00000E+00 0.37000E+02 0.00000E+00 0.00000E+00 0.00000E+00 0.16400E+03 0.00000E+00 0.00000E+00 0.00000E+00 0.16400E+03 0.00000E+00 0.00000E+00 0.00000E+00 0.1015E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.10152E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.10152E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.112500E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.15500E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.15500E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.15500E+00 0.00000E+00 0.00000E+00 0.00000E+00	0.9500E+00 0.00000E+00 0.00000E+00 0.00000E+00 0.36665E+02-0.99669E+02 0.90168E+02-0.27112E+02 0.16767E+00 0.17642E+01-0.31119E+00 0.00000E+00 0.10000E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.10000E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.10000E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.10000E+01 0.00000E+00 0.00000E+00 0.00000E+00
<pre>HEAN COV P3 DIST 0.60000E+01 0.20000E-02 0.00000E+00UHIF0RH 0.30000E+02 0.25900E+00 0.00000E+00E0HIF0RH 0.30000E+02 0.25900E+00 0.00000E+00L0GH0RHAL 0.10000E+01 0.10000E-01 0.00000E+00L0GH0RHAL 0.1052E+01 0.10000E-01 0.00000E+00L0GH0RHAL 0.10152E+01 0.10000E-01 0.00000E+00L0GH0RHAL 0.10152E+01 0.10000E-01 0.00000E+00H0RHAL 0.10152E+01 0.10000E-01 0.00000E+00H0RHAL 0.10500E+01 0.10000E-01 0.00000E+00H0RHAL 0.10500E+01 0.10000E-01 0.00000E+00H0RHAL 0.10500E+01 0.10000E-01 0.00000E+00H0RHAL 0.10500E+01 0.10000E-01 0.00000E+00H0RHAL 0.10500E+00 0.10000E+01 0.00000E+00H0RHAL 0.10500E+00 0.10000E+01 0.00000E+00H0RHAL</pre>	0.71600E+00 0.110000E+01 0.00000E+00N0RMAL 0.55605E+01 0.15000E+01 0.00000E+00N0RMAL 0.16206E+01 0.15000E+01 0.00000E+00H0RMAL 0.10000E+01 0.10000E+02 0.00000E+00H0RMAL 0.10000E+01 0.10000E+02 0.00000E+00H0RMAL 0.10000E+01 0.10000E+02 0.00000E+00H0RMAL

Database
Loads
Independent
6.4.
Figure

6-12

LD-WAHE HR F-P1 F-71 F-71 F-71 F-71 HF-78-FM H0-78-FM H0-78-FM F-78-FM F-78-FN F-78-FN H0-785-F1 F-785-F1 F-785-F1 Hf-78-CC

LI0P-10

Database
Load
Dependent
LDEP:
6.5.
Figure

key to continue

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LD-NAME	MEAN COV P3 DIST	NE-COEF1 NE-COEF2 N
HO • 78 • SP	0.27098E+05 0.52000E-02 0.00000E+00NORMAL	0.55834E+04 0.20905E+05
HF-TB-SP	0.34625E+05 0.55000E-02 0.00000E+00NORMAL	0.15410E+05 0.16751E+05
Od-Hd-DH	0.41075E+04 0.89000E-02 0.00000E+00NORMAL	0.14544E+03 0.24759E+04
HF.PH.PO	0.61998E+04 0.90000E-02 0.00000E+00NORMAL	0.14515E+04 0.23857E+04
OP8-CH-P	0.50592E+04 0.12900E-01 0.00000E+00NORMAL	0.25803E+03 0.44060E+04
FPB-CH-P	0.49555E+04 0.13700E-01 0.00000E+00NORMAL	0.10327E+04 0.75249E+04-
ENG-O-FL	0.89435E+03 0.62000E+02 0.00000E+00NORMAL	0.10448E+01 0.89777E+03-
ENG-F-FL	0.14906E+03 0.69000E-02 0.00000E+00N0RHAL	0.54315E+00 0.14048E+03
ENG-THRU	0.47107E+06 0.50000E-02 0.00000E+00NORMAL	0.10474E+04 0.46729E+06
0-PRS-FL	0.16206E+01 0.15000E-01 0.00000E+00NORMAL	0.16767E+00 0.17642E+01-
F-PRS-FL	0.70031E+00 0.65000E-02 0.00000E+00NORMAL	0.34437E-01 0.63776E+00
97-0-890	0.65025E+00 0.14700E-01 0.00000E+00NORMAL	0.61621E+00-0.40203E+00
FP8-0-VP	0.78974E+00 0.13500E-01 0.00000E+00NORMAL	0.69291E+00-0.15036E+00
HCC-0-1P	0.35372E+04 0.86000E+02 0.00000E+00NORMAL	0.78808E+02 0.27181E+04
HCC-0-17	0.19024E+03 0.20000E-02 0.00000E+00NORMAL	0.16512E+03 0.12433E+02
HG-1P	0.32438E+04 0.64000E+02 0.00000E+00N0RMAL	0.13722E+03 0.36198E+04-
HCC-IEP	0.30060E+04 0.58000E-02 0.00000E+00NORMAL	0.16085E-03 0.30060E+04
Id-Hd-OH	0.37915E+03 0.22800E-01 0.00000E+00N0RMAL	0.11393E+03 0.33464E+03-
HF-PH-PI	0.20900E+03 0.26300E-01 0.00000E+00NORMAL	0.26705E+03-0.15416E+03
DG • Md • Bd	0.70920E+04 0.98000E-02 0.00000E+00N0RMAL	0.53504E+03 0.67636E+04
/ key to continue		Hit any key to continue
		•
LD-NAME	MEAN COV P3 DIST	NE-COEF1 NE-COEF2 N
11-M4-OH	0.16943E+03 0.6000E-03 0.00000E+00N0RMAL	0.1647BE+03 0.2824BE+01
HO-PH-TO	0.19024E+03 0.20000E-02 0.00000E+00NORMAL	0.16512E+03 0.12433E+02
HF-PH-TO	0.95571E+02 0.11400E-01 0.00000E+00N0RMAL	0.60135E+02 0.19283E+02

**S** NW4N92800101145928600 HIt

	LD-NAME	MEAN C	COV	P3 01ST	NE
21	IT-M4-OH	0.16943E+03	0.60000E-03	0.16943E+03 0.60000E.03 0.00000E+00NORMAL	0
22	HO-PH-TO	0.19024E+03	0.20000E-02	0.19024E+03 0.20000E-02 0.00000E+00NORMAL	0
23	HF-PH-TO	0.95571E+02	0.11400E-01	0.95571E+02 0.11400E-01 0.00000E+00N0RMAL	0
24	HFV-TO	0.96151E+02	0.11400E-01	0.96151E+02 0.11400E-01 0.00000E+00H0RHAL	0
25	P8-PN-T0	0.20306E+03	0.25000E-02	).20306E+03 0.25000E+02 0.00000E+00HORMAL	0
26	HF-PN-TI	0.42210E+02	0.19000E-02	3.42210E+02 0.19000E-02 0.00000E+00NORMAL	0
27	LO-TB-SP	0.50366E+04	0.80000E-02	0.503666+04 0.800006-02 0.000006+00H0RMAL	
28	LF-T8-SP	0.14921E+05	0.90000E-02	0.00000E+00N0RMAL	0
29	HO-TB-TO	0.12890E+04	0.27400E-01	<pre>0.12890E+04 0.27400E-01 0.00000E+00NORMAL</pre>	0
30	HF-T8-T0	0.17029E+04	0.19300E-01	0.19300E.01 0.00000E+00NORMAL	0
Ē	0PB-0-VR	0.13143E+03	0.98200E-01	0.98200E-01 0.00000E+00NORMAL	0
32	FPB-0-VR	0.92308E+01	0.15350E+00	0.15350E+00 0.00000E+00HORMAL	0
33	O-PRS-P	0.33703E+04	0.92000E-02	0.92000E-02 0.00000E+00NORMAL	0
34	F-PRS-P	0.33486E+04	0.79000E-02	0.00000E+00NORMAL	0
35	O-PRS-T	0.83918E+03 (	0.24500E-01	0.00000E+00NORMAL	0
36	F-PRS-T	0.47628E+03	0.12500E-01	0.00000E+00NORMAL	0
37	LO-PH-SP	0.80451E+04 (	0.10000E-01	0.00000E+00NORMAL	0
38	LF-PM-SP	0.10573E+05 (	0.10000E-01	0.00000E+00NORMAL	0
39	HO-PH-SP	0.11258E+05	0.10500E-01	0.11258E+05 0.10500E-01 0.00000E+00N0RMAL	0
40	HF-PM-SP	0.64475E+04 1	0.24000E-01	0.64475E+04 0.24000E+01 0.00000E+00N0RMAL	0

NE-COEF1 NE-COEF2 NE-CDEF3 NE-COEF4
0.55834E+04 0.20905E+05 0.61017E+03 0.00000E+00
0.1544E+03 0.24759E+04 0.18903E+04-0.40409E+03
0.14515E+04 0.23657E+04 0.18903E+04-0.40409E+03
0.14515E+04 0.23657E+04 0.18903E+04-0.40409E+03
0.14515E+04 0.23657E+04 0.35029E+04 0.00000E+00
0.25803E+03 0.44606E+04 0.484113E+03 0.42709E+04
0.10327E+04 0.75249E+04-0.35029E+04 0.19661E+04
0.10327E+00 0.148AE+03 0.37899E+04-0.11461E+04
0.10448E+01 0.897777E+03-0.4638E+01 0.0000E+00
0.54315E+00 0.148AE+03 0.37899E+04-0.11461E+04
0.10448E+01 0.89777759E+04-0.35029E+04 0.19661E+04
0.10448E+01 0.89777759E+04 0.388A8E+04-0.11461E+04
0.10448E+01 0.89777759E+04 0.388A8E+04-0.11461E+04
0.10448E+01 0.89777759E+04 0.00000E+00
0.14575E+00 0.17642E+03-0.24709E+00
0.16721E+00-0.15036E+00 0.28114E+01 0.00000E+00
0.34437E+01 0.03776E+00 0.28114E+01 0.00000E+00
0.54515E+00 0.15036E+00 0.24779E+02-0.21637E+03
0.18512E+03 0.32498E+04-0.50439E+04 0.00000E+00
0.69291E+00-0.15036E+00 0.26457E+02-0.21637E+03
0.18512E+03 0.32456E+04 0.095671E+03-0.21637E+03
0.18512E+03 0.32456E+04 0.095671E+03-0.21637E+03
0.55595E+03
0.26795E+03 0.33456E+04 0.095637E+03-0.21637E+03
0.15035E+03 0.32455E+03
0.26795E+03 0.32455E+04
0.95575E+03
0.15036E+04 0.095671E+03-0.21637E+03
0.18512E+03 0.32456E+04
0.95575E+03
0.26795E+03
0.15036E+04 0.095637E+03
0.26575E+03
0.219545E+03
0.26735E+03
0.26735E+03
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0.25355E+03
0.25355E+03
0.25458+03
0.26458+03
0.26458+03
0.26458+03
0.26458+03
0.26458+03
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0.26458+03
0.264585
0.253556+0
0.20000E+0
0
0.253565+0
0.253556+0
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LDEP - 10

Me-LUETI Mer-LUETA Mer-LUETA 0.1647BE+03 0.28248E+01 0.24169F+01-0.59064E+01 0.16515E+03 0.12435E+02 0.14775E+02-0.209066+01 0.16575E+02 0.19283E+02 0.14775E+02 0.00000E+00 0.16959E+03 0.15697E+02 0.161775E+02 0.00000E+00 0.15955E+02-0.46672E+01 0.29147E+01 0.00000E+00 0.43963E+02-0.46672E+01 0.28147E+01 0.00000E+00 0.17100E+04 0.36940E+04 0.33674E+03 0.00000E+00 0.13081E+05-0.45270E+04 0.336734E+03 0.00000E+00 0.13081E+05-0.45270E+04 0.336734E+03 0.00000E+00 0.13081E+05-0.45270E+04 0.336734E+03 0.00000E+00 0.33530E+04-0.16428E+03 0.38645E+03 0.00000E+00 0.14807E+04-0.16428E+03 0.38645E+03 0.00000E+00 0.33530E+04-0.59476E+04 0.17816E+04 0.00000E+00 0.19042E+03 0.23012E+03 0.49820E+03 0.00000E+00 0.19042E+03 0.23012E+03 0.49820E+03 0.00000E+00 0.33542E+03 0.23012E+04 0.93589E+03 0.00000E+00 0.33542E+03 0.53012E+04 0.93589E+03 0.00000E+00 0.33542E+03 0.58347E+04 0.93589E+03 0.00000E+00 0.33542E+03 0.58347E+04 0.93589E+03 0.00000E+00 0.33542E+03 0.58347E+04 0.935397E+04 0.00000E+00 0.33542E+03 0.58347E+04 0.935397E+04 0.00000E+00 0.14279E+04 0.11165E+05-0.335377E+04 0.00000E+00 0.14279E+04 0.11165E+05-0.335377E+04 0.00000E+00 0.14279E+04 0.11165E+05-0.333172E+04 0.00000E+00 0.14279E+04 0.11165E+05-0.333172E+04 0.00000E+00 NE-COEF4 NE-COEF3 continue 2 Hit any key

6 - 13

LDEP-

<pre>ME-CGEF1 NE-COEF2 NE-CGEF3 NE-CGEF4 0.96970E+03 0.23960E+04 0.15293E+04 0.00000E+00 0.34914E+03 0.23960E+04 0.15293E+03 0.00000E+00 0.35028E+03 0.231228E+04 0.23734E+03 0.00000E+00 0.35028E+03 0.23122E+04 0.23734E+04 0.34008E+03 0.234972E+02 0.17332E+03-0.38821E+02 0.00000E+00 0.34972E+02 0.17332E+03-0.38821E+02 0.00000E+00 0.34972E+02 0.17332E+03-0.38821E+02 0.00000E+00 0.14676E+03 0.23734E+01 0.12321E+04 0.39175E+04 0.116629E+01 0.49960E+02 0.11654E+02 0.00000E+00 0.14676E+03 0.23734E+04 0.18122E+04.0.39175E+04 0.116555E+03 0.23734E+04 0.18122E+04.0.39175E+04 0.116655E+03 0.24002E+04 0.18122E+04.0.39175E+04 0.116655E+03 0.23734E+04 0.18122E+04.0.39175E+04 0.116655E+03 0.23734E+04 0.18122E+04.0.39175E+04 0.116655E+03 0.23734E+04 0.1915E+04 0.00000E+00 0.14676E+03 0.23565E+04 0.18122E+04.0.39175E+04 0.19505E+03 0.23734E+04 0.19125E+04.0.39175E+04 0.19505E+03 0.23734E+04 0.19525E+04 0.19505E+03 0.23754E+03 0.19000E+00 0.146555E+03 0.23556E+04 0.19525E+04 0.19505E+03 0.23556E+04 0.19125E+04 0.19505E+03 0.23754E+03 0.19505E+04 0.19505E+03 0.23556E+04 0.19125E+04 0.19505E+03 0.23556E+04 0.19525E+04 0.19505E+03 0.23556E+03 0.164952E+04 0.19505E+03 0.23556E+03 0.19926E+03 0.195555E+03 0.23556E+03 0.19926E+03 0.195555E+03 0.23556E+03 0.19975E+04 0.19505E+03 0.23556E+03 0.19975E+04 0.19505E+03 0.23556E+03 0.19975E+04 0.19505E+03 0.23556E+03 0.19975E+04 0.19505E+03 0.23556E+03 0.19975E+04 0.19505E+03 0.23556E+03 0.50716E+03 0.00000E+00 0.1653756E+03 0.27154E+04 0.40252E+03 0.00000E+00 0.10909E+03 0.27154E+04 0.40252E+03 0.00000E+00</pre>	NE-COEF1 NE-COEF2 NE-COEF3 NE-COEF4 -0.14193E+03 0.36618E+04-0.46887E+03 0.27518E+03 -0.26861E+03 0.42106E+04-0.97850E+03 0.51460E+03
НЕМ СО РЗ 0.10800E-01 0.00000E-00000RMAL 0.48950E+04 0.10800E-01 0.00000E-00000RMAL 0.49091E+03 0.12200E-01 0.00000E-00000RMAL 0.97352E+04 0.15900E-01 0.00000E-00000RMAL 0.97352E+04 0.15900E-01 0.00000E-00000RMAL 0.95479E+04 0.14200E-01 0.00000E+0000RMAL 0.9547313E+02 0.17500E-01 0.00000E+00000RMAL 0.17602E+03 0.99000E-01 0.00000E+00000RMAL 0.17605E+03 0.17700E-01 0.00000E+00000RMAL 0.15605E+04 0.10700E-01 0.00000E+00000RMAL 0.15605E+04 0.10700E-01 0.00000E+00000RMAL 0.15052E+03 0.10700E-01 0.00000E+00000RMAL 0.19052E+04 0.10500E-01 0.00000E+00000RMAL 0.19024E+04 0.10500E-01 0.00000E+00000RMAL 0.19034E+04 0.10500E-01 0.00000E+00000RMAL 0.44928E+04 0.10500E-01 0.00000E+00000RMAL 0.19034E+04 0.10500E-01 0.00000E+00000RMAL 0.14073E+04 0.18000E-02 0.00000E+00000RMAL 0.49362E+04 0.10500E-01 0.00000E+00000RMAL 0.1335F+03 0.220000E-01 0.00000E+00000RMAL 0.1335F+03 0.25000E-01 0.00000E+00000RMAL 0.1335F+03 0.25000E-01 0.00000E+00000RMAL	МЕАИ COV P3 DIST 0.33262E+04 0.66000E-02 0.00000E+00И0RHAL 0.34781E+04 0.67000E-02 0.00000E+00И0RHAL
LDEP-1D LD-NAME 41 HCC-C-PO 42 HCC-C-PO 43 LO-TB-TQ 45 HC-TB-TQ 46 HF-TB-TQ 46 HF-TB-TQ 46 HF-TB-TQ 46 HF-TB-TQ 40 HF-TB-TQ 40 HF-TB-TI 51 LCO-TB-FL 53 HO-TB-PI 53 HO-TB-PI 54 HF-TB-FI 55 LF-TB-FI 56 LF-TB-FI 58 HF-TB-FI 58 HF-TB-FI 58 HF-TB-FI 59 LO-TB-FI 59 LO-TB-FI 59 LO-TB-FI 59 LO-TB-FI 59 LO-TB-FI 59 LO-TB-FI 59 LO-TB-FI 59 LO-TB-FI 50 HF-TB-FI 50 LF-TB-FI 51 HF-TB-FI 52 HF-TB-FI 53 HF-TB-FI 54 HF-TB-FI 55 HF-TB-FI 56 LF-TB-FI 56 LF-TB-FI 57 HC-TB-FI 56 LF-TB-FI 56 LF-TB-FI 57 HC-TB-FI 56 LF-TB-FI 57 HC-TB-FI 58 HF-TB-FI 59 LO-TB-FI 50 HF-TB-FI 51 HF-TB-FI 52 LF-TB-FI 53 HF-TB-FI 54 HF-TB-FI 55 HF-TB-FI 56 HF-TB-FI 57 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 57 HC-TB-FI 56 HC-TB-FI 5	LD-KAME HO-TB-PO HF-TB-PO
LDEP-10 421 424 424 424 424 424 424 424 424 424	LDEP - 10 61 62

# Figure 6.5. LDEP: Dependent Load Database (Continued)

ID parameters are the keys for retrieval and other database operations. The knowledge base also includes engine load model information. The influence coefficient set for the engine probabilistic influence model and the 1 sigma gain values are stored in the database INFC. An example of the database is shown in Figure 6.6. The values of the fields INFL-C1, INFL-C2, INFL-C3 and INFL-C4 in the database INFC are the four coefficients  $c_i$ 's in Equation (4.3). The values of the fields GAIN65, GAIN90, GAIN100, and GAIN104 are the 1 sigma gains of the dependent load at power levels of 65%, 90%, 100% and 104%. These are the gains corresponding to the 1 sigma (standard deviation) change in the respected independent load. The expert system uses these gains to select the most influential independent loads to a dependent load for users and thus shows a seemingly intelligent behavior.

The knowledge base includes also the load dependency and scaling information of the component load models, the duty-cycle-data information, etc. The complete information of the knowledge base will be documented in the load-expert system LDEXPT user's manual.

### The Rule Modules

The rule-based module has the expert system driver SESUIM (the user interface module), the load calculation module ANLOAD, the statistical tool box, and the Rule Modules. In LDEXPT version 2.1, the statistical tool box has only a few data-fitting routines: not much effort has gone into developing it. As discussed earlier, the decision tree inference scheme is used to process the rules. Each Rule Module is a decision tree for performing certain tasks and/or solving a particular problem. The advantage of this inference scheme is that it is efficient. System with this inference scheme can be easily coupled with external numerical routines. The disadvantage of the decision tree inferencing is the loss of flexibility of selecting alternative rules to solve problems.

0.16865-05 0.16865E-05 0.16865E-05 0.16865E-05 0.06570E-05 0.60570E-05 0.60570E-05 0.05771E-02-0.15771E-02-0.15746E-02-0.15808E-02 0.16955E-02-0.15771E-02-0.15746E-02-0.15722E-02 0.52009E-04 0.49643E-04 0.31078E-04 0.33118E-04 0.61999E-04 0.43575E-04 0.38545E-04 0.337548E-04 0.61999E-04 0.43575E-04 0.287717E-03-0.66216E-03 0.16215E-02 0.16215E-03 0.65717E-03-0.66216E-03 0.16215E-02 0.16215E-02 0.16215E-02 0.16215E-02 0.106215E-02 0.16215E-02 0.53229E-03-0.633305E-03-0.43596E-03 0.11472E-02-0.110916E-02-0.653305E-03-0.43596E-03 0.93350E-02 0.10682E-01 0.13162E-01 0.14465E-01 0.53299E-03 0.253226E-03 0.25163E-03 0.21947E-03 0.11472E-02-0.10016E-02-0.633305E-03-0.43596E-04 0.11898E-04-0.90808E-04-0.90808E-04-0.90808E-04 0.11723E-02 0.10682E-01 0.13162E-01 0.14465E-02 0.11723E-02 0.10582E-03 0.25163E-03 0.21947E-03 0.53299E-03 0.253202E-03 0.25163E-01 0.14465E-02 0.11725E-02 0.10016E-02 0.14786E-02 0.14786E-02 0.11725E-02 0.01016E-02 0.14786E-02 0.14786E-02 0.11898E-04-0.99808E-04-0.25881E+00-0.258842E-04 0.11898E-03 0.258840E+00-0.258841E+00-0.25882E+00 0.25269E-05-0.63530E-04-0.52841E+00-0.25842E-04 0.25269F-05-0.63530E-04-0.52841E+00-0.25842E-04 0.257877E-01-0.33077E-01-0.33077E-01-0.33077E-01 GAIN65 GAIN90 GAIN100 GAIN104 -0.22353F-03'0.22353F-03'0.22353F-03'0.22353F-03 0.16261E-03 0.83700E-04 0.52137F-04 0.39511E-04 -0.40496E-02:0.23041E-02-0.19184E-02-0.18141E-02 -0.17077E-03:0.17793F-03:0.16139F-03:0.15167F-03 0.31309E-03:0.46298E-03-0.46298E-03-0.46298E-03 0.46290E-03-0.46298E-03-0.46298E-03-0.46298E-03 0.46290E-03-0.46298E-03-0.26815E-03-0.26608E-03 0.19985E-02-0.15590E-03-0.46298E-03-0.26608E-03 0.19985E-02-0.15590E-03-0.26815E-03-0.26608E-03 0.24372E-03-0.26896E-03-0.26815E-03-0.26608E-03 0.24372E-03-0.26896E-03-0.26315E-03-0.26608E-03 0.25372E-05 0.25372E-05 0.25372E-05 0.25372E-05 0.44403E-02 0.28849E-04-0.357328E-05 0.253775E-05 0.44403E-02 0.28849E-02-0.34486E-02-0.36775E-05 0.44403E-02 0.28849E-02-0.35775E-05 0.253775E-05 0.44403E-02 0.18641E-02 0.12445E-02-0.56775E-05 0.44403E-02 0.18641E-02 0.12445E-02-0.56775E-05 0.44403E-02 0.18849E-02-0.56775E-05 0.55775E-05 0.14758E-02 0.18641E-02 0.95775E-05 0.14758E-02 0.588775E-05-0.56775E-05 0.14758E-02 0.58775E-05-0.56775E-05 0.14758E-03 0.09475E-03-0.956775E-05 0.178035E-01 0.06000E+00 0.00000E+00 0.71812E-01 0.61371E-01 0.58940E-01 0.50246E-01 0.71812E-01 0.61371E-01 0.58940E-01 0.50246E-01 GAIN104 GAIN100 continue continue **GA1N90** any key to 9 key βuλ SAIN65 0.00 0.71 Hit 0.233666-04 0.00006400 0.00006400 0.00006400 0.115816-01 0.965499-02-0.503016-02 0.00006400 0.335556-04 0.861196-03-0.678826-03 0.00006400 0.335556-04 0.861196-03-0.678826-03 0.00006400 0.335546-04 0.590946-03-0.564876-03 0.00006400 0.415806-02-0.875786-02 0.471076-02 0.00006400 0.335946-03-0.517346-02 0.230016-02 0.000066400 0.3556076-03 0.00006400 0.000006400 0.1562607 -01 0.141716-01-0.501186-02 0.000006400 0.147366-011 0.141716-010.501186-02 0.000006400 0.147546-02-0.311166400 0.214176400 0.000006400 0.147546-02-0.311166400 0.214176400 0.000006400 0.147546-02-0.311166400 0.214176400 0.000006400 0.477546-02-0.310386-02 0.000006400 0.000006400 0.47546-02-0.12046-02 0.000006400 0.000006400 0.47546-02-0.12046-02 0.000006400 0.000006400 0.47546-02-0.12046-02 0.000006400 0.000006400 0.47546-02-0.1204646-02 0.000006400 0.000006400 0.475546-02-0.1204646-02 0.000006400 0.000006400 0.475546-02-0.1204646-02 0.000006400 0.000006400 0.475546-02-0.1204646-02 0.000006400 0.000006400 0.475546-02-0.1204646-02 0.000006400 0.000006400 0.475546-02-0.1204646-02 0.000006400 0.000006400 0.475546-02-0.1204646-02 0.000006400 0.000006400 0.475546-02-0.1204646-02 0.000006400 0.000006400 0.127716400 0.000006400 0.000006400 0.000006400 0.286776-02-0.694216-02 0.000006400 0.000006400 0.00006+00 0.000006+00 10.000006+00 0.000006+00 0.000006+00 0.000006+00 0.000006+00 0.000006+00 0.000006+00 0.000006+00 0.000006+00 0,00000E+00 0,00000E+00 0.00000E+00 0.00000E+00 0.00000E+00 0.00000E+00 0.00000E+00 0.00000E+00 0.00000E+00 INFL-C4 - C4 -0.86304E-03 0.0000E+00 0.0000E+00 0. 0.14200E-02-0.12187E-02 0.00000E+00 0. 0.14200E-02-0.34281E-02 0.21403E-02 0. 0.66462E-03-0.34281E-02 0.21403E-02 0. 0.12088E-04 0.00000E+00 0.00000E+00 0. 0.17876E-02 0.00000E+00 0.00000E+00 0. 0.15800E-01 0.16728E-01-0.64132E-02 0. 0.16320E-04-0.225550E-02 0.20000E+00 0. 0.16371E-03 0.013034E-01 0.44132E-02 0. 0.17744E-01 0.16728E-01-0.64132E-02 0. 0.3771E-03 0.00000E+00 0.00000E+00 0. 0.3771E-03 0.00000E+00 0.00000E+00 0. 0.3771E-03 0.00000E+00 0.00000E+00 0. 0.75700E-02-0.17664E-01 0.79576E-02 0. 0.84480E-02-0.21763E-01 0.79576E-02 0. 0.84480E-02-0.21763E-01 0.32483E-01 0. 0.32042E-01 0.00000E+00 0.00000E+00 0.0 0.31221E-02-0.15427E-02 0.00000E+00 0.00000E+00 0.19247E+00 INFL-C3 INFL-C3 0.00000E+00 0.13176E-03 0.00000E+00 0.49467E+00-0.45957E+00 INFL-C2 INFL-C2 ł 0.65117E-05 -0.50150E-02 -0.50709E-03 0.00000E+00 NFL-C1 INFL-C1 continue any key to continue LIDP-10 LIDP-1D NNNNNNNNNNNNNNNNNNNN \$ key **Ang** LDEP-10 DEP-10 20180011022222260 يد ...

Figure 6.6. INFC: Influence Coefficient Database for LIDP-ID=2

6-16

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INFC: Influence Coefficient Database for LIDP-ID=2 (Continued) Figure 6.6.

GAIN65 GAIN90 GAIN100 GAIN104 -0.60482E-01-0.50323E-01-0.47390E-01 0.47478E-03 0.78276E-03 0.72772E-03 -0.44955E+00 0.45905E+00-0.19493E+00 0.00000E+00 -0.1067DE-01 0.29692E-01-0.16087E-01 0.00000E+00 JNFL-C4 INFL-C3 INFL-C2 INFL-C1 L10P-10 ~ ~ LDEP-1D 61 62

0.75552E-03-0.113055-02-0.10855E-02-0.10370E-02
0.36194E-02-0.19822E-02-0.16100E
0.29524E-03-0.130545-03-0.24381E-03-0.24092E-03
0.29524E-03-0.394755-03-0.24381E-03-0.24092E-03
0.294200E-03-0.894755-03-0.212755-03-0.212755-03
0.212756-03-0.212755-03-0.212755-03-0.212755-03
0.212756-03-0.21094E-03-0.212755-03-0.21094E-03
0.212756E-03-0.21756-03-0.212755-03-0.21094E-03
0.212756E-03-0.21094E-03-0.212755-03
0.212756E-03-0.217760E-02-0.11343E-02-0.112395-02
0.54209E-04-0.54209E-04-0.54209E-02
0.55551E-03-0.277205E-02-0.1373526E-02-0.244355E-02
0.75956E-02-0.487206E-02-0.378326E-02-0.24435E-02
0.75956E-01-0.94195E-02-0.13775E-03-0.024255E-01
0.75956E-01-0.94195E-02-0.13775E-03-0.17254E-01
0.17377E-03-0.17377E-03-0.17377E-03-0.17377E-03
0.17377E-03-0.17377E-03-0.17377E-03-0.17377E-03
0.17377E-03-0.17377E-03-0.17377E-03-0.17377E-03
0.17377E-03-0.17377E-03-0.17377E-03-0.17377E-03
0.17377E-03-0.17377E-03-0.17377E-03-0.771763E-03
0.17377E-03-0.17377E-03-0.17377E-03-0.17377E-03
0.16377E-01-0.81389E-02-0.79813E-02-0.79674E-03
0.10537E-010-0.213322E+00-0.213322E+00-0.212325E+00
0.21695E+00-0.21432E+00-0.213322E+00-0.212322E+00 GAIN104 GAIN100 Hit any key to continue GA1N90 GALN65

INFL-C1         INFL-C2         INFL-C3         INFL-C4           0.13048E-01-0.38323E-01         0.20000540           0.48649E-01         0.77611E-01-0.31178E-01         0.00000540           0.48649E-01         0.77611E-01-0.31178E-01         0.00000540           0.19901E-02         0.178955E-02         0.00000540           0.19901E-02         0.178955E-02         0.00000540           0.50150E-02         0.312215         0.2-0154275-02         0.00000540           0.821457E-03         0.000005400         0.000005400         0.000005400           0.821457E-03         0.000005400         0.000005400         0.000005400           0.821457E-03         0.000005400         0.000005400         0.000005400           0.256686F-01         0.4204156-02         0.000005400         0.000005400           0.2195556-02-0.949176-02         0.000005400         0.000005400         0.000005400           0.2195556-02-0.949176-02         0.1090056400         0.000005400         0.000005400           0.2255418-01-0.23179576-00         0.0000056400         0.0000056400         0.000005400           0.2255418-01-0.23179556-01         0.1090006400         0.000006400         0.000006400           0.2255418-010         0.4204566-02         0.0000006400	
LIDP-ID 2020222222222222222222222222222222222	
LDEP-10 41 42 42 42 43 44 45 55 55 55 55 55 55 55 55 55 55 55	

Rules are designed to represent the textual information needed for load synthesis. Rules also are written to control the computation process and to retrieve and manage the requested engineering data. The rule modules implemented in LDEXPT version 2.1 are:

<u>Rule-Modules</u>	Function
SLIDPL	Independent load info. retrieval
SLDEPL	Dependent load info. retrieval
SLICGN	Infl. coeff's & gain values retrieval
SLTBCL	Turbine blade pressure load info. retrieval
SLTHCL	Component load info. retrieval
SLSCTH	Component load model info. retrieval
SLICTH	Thermal load influence coeff's retrieval
SLCLFP	Fluctuation pressure load info. retrieval
SLDUCT	Duct geometry info. retrieval
SLDDYN	Duct dynamic load PSD info. retrieval
SLDCD	Duty-cycle-data file info. retrieval
QLM	Quick-Look model calculation
SICM	Deterministic influence model calc.
STBSM	Simple turbine blade scaling model calc.
TBPRLI	Turbine blade linear interpolation calc.
ANLDIN	Prepare ANLOAD input file for load calc.
EXIT	Return to RBMS, rule-based module control

The rule-module ANLDIN, preparing an ANLOAD input file for load calculation, is the module used most often. This module retrieves the user request load information and data from the knowledge base and prompts the user for required parameters such as: length of mission time, time step size, probabilistic

6-18

method chosen, etc. Details of each rule module will be discussed in the load-expert system user manual. As an example, the equivalent rules of the rule module SICM are listed below:

- a) If the dependent load ID is N and the independent load ID is M then the influence coefficient parameter set is cl, c2, c3 and c4.
- b) If the dependent load ID is N and the user requests that the expert system selects the M most influential independent loads on the dependent load and the selection is going to be based on gains for power level X

then the M independent loads are M1, M2, ... (after some numerical evaluations)

- c) If the dependent load ID is N and the user requests a simple deterministic influence model calculation
  - then the expert system will either request the user to select the independent loads manually or the expert system will select them if the user requests that, retrieve influence coefficient set and perform the deterministic influence model calculation.

It is obvious from the rules above that the SICM rule module will require the services of the following: (1) the rule-module SLDEPL which retrieves the dependent load information, (2) the rule-module SLIDPL which retrieves the independent load information, and (3) the rule-module SLICGN which retrieves the influence coefficient set. The required communication between these rule modules, or any other rule module, is carried out by a simple working memory model.

# The Working Memory Model

The working memory model was designed for passing information (short-term memory) between different rule modules. To keep the model simple, the information saved was limited to that needed to pass from one rule module to another module but not to multiple rule modules. The working memory consists of a stack used for storing database indices for record retrieval and a memory array used for storing information (e.g. subgoals, facts). The advantage of implementing a working memory model is that many inference processes can proceed without user intervention. For example, suppose one wants to do a deterministic influence model calculation for the HPFTP turbine speed using rule module SICM. First, one selects the dependent load ID number 3 for the HPFTP speed inside the SLDEPL rule module. This information is then passed to the SLIDPL rule module for selecting the most influential independent loads by the expert system if that is what the user chooses to do. Next, the dependent load ID and the independent load IDs are passed to the SLICGN rule module for retrieving the influence coefficient set. After all information and data are retrieved, an influence model calculation is then performed in the SICM rule module. Without the working memory, one has to manually pass the information between the rule modules in order to complete the process.

# <u>Operation</u>

The load-expert system, LDEXPT version 2.1, was installed on the NASA Lewis Research Center's VM/CMS system. To run the expert system, a user needs to have the library for the expert system, the LDEXPT EXEC file, the knowledge base file and duty-cycle-data file, the problem text file and rule file, and a few other data files. The procedure is as follows: (1) Request more virtual memory by executing a CP command:

CP DEFINE STORAGE 4096K

(2) Returns to CMS:

CP IPL CMS

(3) Loading the graphic-3d package (LeRC's graphic package):

# GRAPH3D

(4) Loading the load-expert system:

# LDEXPT

The load-expert system LDEXPT is a menu-driven program. To get to the expert system driver, one needs first to go to the rule-based module by entering the command:

### ?RBMS

then, the rule-based module menu is shown on screen. Select the expert system driver by entering the command:

## ?EXDR

A rule modules menu appears on screen and one can select and execute any one of the rule modules.

System operations such as implementing a new knowledge base or adding new database to the existing knowledge base will be discussed in the load-expert system users manual. Implementation of the available generic models, such as the generic static pressure load model, and the generic probabilistic thermal load model, etc. will also be discussed in the users manual.

For those readers who would like to see the load-expert system LDEXPT in action, a commented printout of an actual run of the rule module ANLDIN is attached as Appendix A. The example, an expert-system consultation session shows the dialogue between a user and the expert system for retrieving relevant load information and data to prepare a load calculation input file.

### 6.5 The Component Load Models

Four space propulsion system components were selected for development of the CLS synthesis: (1) the turbine blade, (2) the transfer ducts, (3) the LOX posts, and (4) HPOTP discharge duct. The loads of interest for these components are exhibited in Table 2.1. The component structures, the mechanics and operation, and the component loads are described in detail in the first CLS annual report (ref. 2.1). In this section, the actual implementation of component loads is summarized. The general approach taken in modeling the component load is to build generic models based on some simple and general principle. For example, one approach that was used in the turbine blade static pressure model is that the differential pressure on the turbine blade surface streamline is proportional to the turbine torgue. The techniques employed most often are the scaling technique and the influence coefficient technique. These two techniques were used in developing the static pressure load model and the probabilistic thermal load model. As the CLS technology advances, physical component load models (i.e., based on the physics of component structure and function) will be developed.

# The Generic Scaling Model

The component static pressure loads are directly scalable with a system-level dependent load or, in the case of a turbine blade, static pressures with two system-dependent loads. Since there are other component loads which are also scalable with one or two system-level loads, a generic scaling model was implemented on the load-expert system. With this model, the turbine blade centrifugal force, the HPOTP discharge duct static pressure load, the HGM fuel and LOX transfer ducts static pressures, and the LOX posts static pressures were implemented.

A simple scaling model is defined as a load directly scalable by one or two system-level dependent loads with a single scaling coefficient. That means in the case of two dependent loads, the scaling coefficient is the same for the two loads with possibly a sign difference. Some scaling models are scaled by two or more dependent loads with two or more coefficients. They are not that much different from the simple scaling model except that a data set for the scaling coefficients is required. The simple scalable component load can be evaluated as follows:

$$L_{c} = a * L_{s1}$$
 (6.1)

or,

$$L_c = a * (L_{s1} - L_{s2})$$
 (6.2)

where,  $L_r$  is the component load,

 $L_{s1}$  and  $L_{s2}$  are the relevant dependent loads,

a is the scaling coefficient.

Routines have been written to calculate the generic scaling model load using equation (6.1) or (6.2). Rule module has been written to supply the load information and data assuming they were implemented in the knowledge base in the conventional way of the load-expert system. To make the scheme work, the knowledge has to be implemented in a certain way. The following is an implementation procedure of the HPOTP discharge duct static pressure load using the generic scaling model. It will serve as an illustration of what is involved in building load models.

1. Add the load information to the component load database LCTH. This can be accomplished by going into the database system resided in the knowledge-based module KBMS with the following commands:

 After the expert system is loaded, enter ?KBMS. A menu of the KBMS module will then show up on the screen

- (2) Enter ?DBMS to enter the database system, a list of available database commands will show up on the screen
- (3) Enter ?DBRD to open the knowledge base file and bring in the database LCTH by following the system prompt
- (4) Enter ?DBUP to add the new load record to the load database LCTH. For example, enter the following for the HPOTP discharge duct static pressure load:

```
CMPN-ID : 10

C-LD-ID : 2

C-LD-NA : HODD-S-P

MEAN : 4107.0

COV : 0.1

P3 : 0.0

DIST : NORMAL

NE-COEF1:

NE-COEF2:

NE-COEF3:

NE-COEF4:
```

Notes: Component ID CMPN-ID = 10 identifies that the component is the HPOTP discharge duct Component load ID C-LD-ID = 2 identifies that the load is the static pressure load Leave blank for NE-COEF1 to NE-COEF4

If the component is a new one which is not in the existing list, select an ID number for the component.

2. Add the scaling load database to SCTH.

Repeat steps (3) and (4) of the previous procedure for database SCTH. The database for the HPOTP discharge duct is as follows:

.

```
CMPN-ID : 10

C-LD-ID : 2

C-LD-NA : HODD-S-P

LD-TYPE : ONE

C1-ID : 0

LDEP1-ID: 3

C2-ID : 0

LDEP2-ID: 0

C3-ID : 0

LDEP3-ID: 0

C4-ID : 0

LDEP4-ID: 0

C5-ID : 0

LDEP5-ID: 0

SC-COEF : 1.0
```

- Notes: LD-TYPE = ONE is for scaling model with one system dependent load = TWO for scaling with two system dependent loads Cn-ID is O for simple scaling model, it means that the dependent load is one of the system dependent loads on the engine influence model n = 1,2,...,5 LDEPn-id is the system level dependent load ID, n = 1,2,...,5 LDEP1-ID = 3 is the system load HO-PM-PO, the HPOTP discharge pressure, which is the static pressure load
  - SC-COEF is the scaling coefficient, in this case, which is 1.0

3. Go into the problem text file: "LOADKB PTF", add an entry for the HPOTP discharge duct static pressure load

4. Go into the rule file: "LOADKB RUL", add an entry for the HPOTP discharge duct static pressure load.

Once these four steps are completed, the load-expert system will be capable of evaluating the component static pressure load.

# The Probabilistic Thermal Load Model

The generic probabilistic thermal load model is much more complex as compared to the scaling model; nevertheless, the same implementation philosophy is followed. Routines and rule module have been written for generic probabilistic thermal load model, and the load-specific knowledge is required to be implemented in the knowledge base. With such a design, one model serves the needs of all components. The evaluation model stays the same, but the load information and data could change, depending on the engine type and the component design.

The probabilistic thermal load model is really a two-level hierarchical model. It is a coupling of a thermal load influence model and a scaling model. The thermal load influence model is a probabilistic influence model which correlates the system-dependent loads relevant to the component under consideration to a set of boundary condition loads for the component. The scaling model then uses the boundary loads to scale the reference temperature profile of the component to the new temperature profile.

The thermal load influence model implemented on the load-expert system has the following form:

$$\frac{\Delta L_{bc,i}}{L_{bc,io}} = \sum_{j} IC_{ij} - \frac{\Delta Y_{j}}{Y_{jo}}$$

where,  $L_{bc.io}$  is the mean of the ith boundary condition load,

 $\Delta L_{bc,i}$  is the change of the ith b.c. load,  $Y_{jo}$  is the mean of the jth system dependent load,  $\Delta Y_{j}$  is the change in  $Y_{j}$  $IC_{ii}$  is the influence coefficient

In this model, the influence coefficients are assumed to be constant. This influence model is the same as the engine system influence model except that the influence coefficients of the thermal load model are constant whereas the engine system influence coefficients are a polynomial function of the commanded power level.

With appropriate selection of system level dependent loads and boundary condition loads, the probabilistic thermal load model makes good prediction of the new temperatures. The boundary condition loads information and the load dependency of component thermal load models for four selected components have been implemented on the knowledge base. The component thermal boundary load information is implemented in database SCTH and the thermal load influence coefficients in ICTH.

The probabilistic thermal load evaluation routines have been implemented in the load calculation module ANLOAD. One could use the expert system consultation module ANLDIN to prepare an ANLOAD input file and run an ANLOAD calculation to obtain the thermal load result. With the model and tools available on the expert system, the probabilistic thermal model for any new component can be easily implemented. In the load-expert system LDEXPT version 2.1, the thermal load models for the turbine blade, the HPFTP and the HPOTP transfer ducts, the LOX post and the HPOTP discharge duct have been implemented (ref. 6.1). As an example, the probabilistic thermal load model for the turbine blade is presented in Appendix B.

6-27

The Duct Pressure Fluctuation Model

The dynamic pressure load on a duct is the pressure fluctuation exerted to the duct due to the turbulence flow condition inside the duct. The generic pressure fluctuation model was developed (ref. 6.2) to provide a fluctuation pressure load in the form of a pressure PSD and correlation lengths for flows through the ducts at different locations.

The fluctuation pressure PSD of the ducts under investigation (for the Composite Load Spectra project, it is the hot gas manifold transfer ducts, the LOX posts, and the HPOTP discharge duct) has the following general shape as shown in Figure 6.7:

> (f)  $k_0 \star f^{-s}$  for  $f_0 < f < f_1$ (f)  $k_1 \star f^{-5/3}$  for  $f_1 < f < f_1$

where s is the shape factor, it can be either 1.0 or 0.4, depending on the component and the geométry location,

 $f_0$  is the frequency lower bound cutoff,  $f_1$  is the frequency beyond which inertial subrange is in effect, it is chosen in general at 40% of the entire frequency band  $f_1$ , and  $f_1$  represents the range to which the spectra is of interest.

The PSD is normalized to the root-mean-square fluctuation pressure p' which is proportional to the 1-D flow dynamic head  $q_{1-D}$ . The  $p'/q_{1-D}$  ratio is an empirical parameter developed based on experimental data. It varies with the flow geometry and flow separation characteristics. The values used in the model will be based on existing experimental data and engineering estimates by our expert if data does not exist. Figures 6.8 and 6.9 show the PSD predictions of the above formulas for the HGM oxidizer upper transfer duct at the entrance top position and the fuel upper transfer duct at the entrance bottom position. In Figure 6.9, the shape factor s of 0.4 gives a better fit to the PSD.

6-28

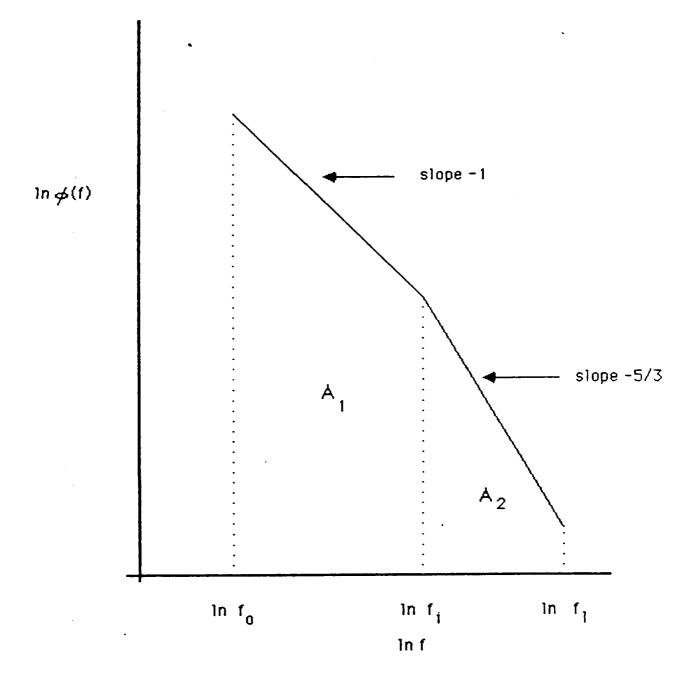
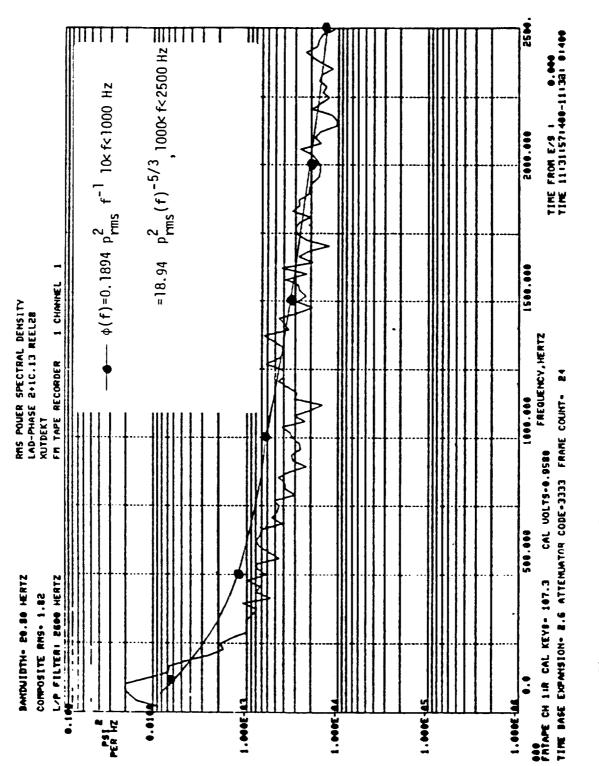
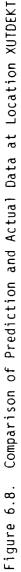


Figure 6.7. Schematic of PSD Curve From Which Various Constants Need to be Determined





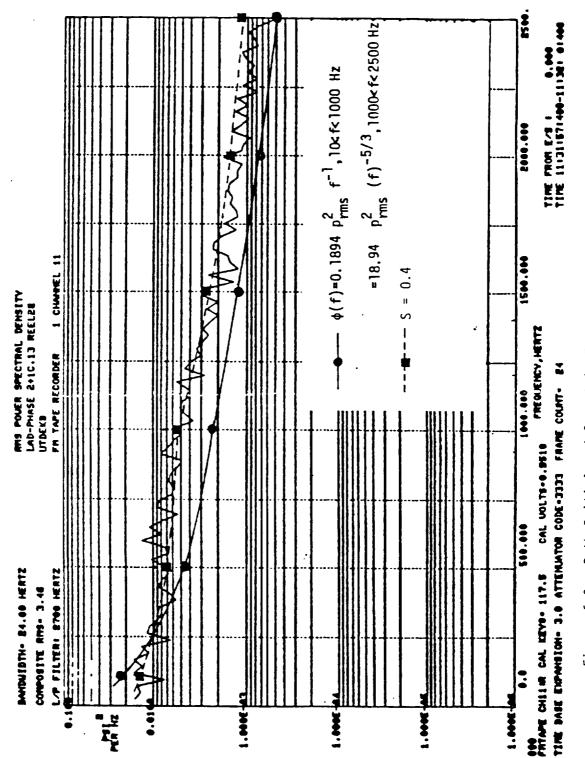


Figure 6.9. Both Initial and Geometric Factor Predictions are Shown

The correlation length  $L_{\chi}$ , over which the pressure fluctuation acts, can be evaluated as follows:

$$L_{X} = U_{C} * T_{X}$$
$$T_{X} = \int_{0}^{\infty} R(\tau) d\tau$$
$$R(\tau) = \int_{0}^{\infty} \phi(w) \cos w\tau dw$$

where,  $U_{c} = 0.6 * U_{1-D}$  for a boundary layer flow,

 $U_{\rm C}$  is the convection velocity of the large scale eddies,  $U_{\rm l-D}$  is the freestream velocity

The model implemented is generic to the components of interest. Three databases are required. The first database is the dependent load information on flow velocity and dynamic head for each component. The second database is the coarse geometry information related to the ratio of the 1-D (one dimension) root-mean-square pressure to the flow dynamic head. This ratio relates to the turbulent intensity factor of the flow and is geometry dependent. The third database is the pressure fluctuation parameter database. One of the parameters is the geometry-dependent ratio related to the turbulent intensity. Therefore, the parameter database has entries for each coarse geometry region. Examples of the second and third databases are listed below for the HPOTP discharge duct.

DUCT : The geometry database for ducts

COMP-ID : 10	/* HPOTP
C-L-ID : 33	<pre>/* Component Fluctuation Pressure Load</pre>
N-ZONES : 6	/* Number of coarse zones
LOC-1 : STRAIGHT	/* Straight portion of the duct
LOC-2 : TURNIALL	/* All area of the wall of the first turn

LOC-3 : TURN2TOP /\* Top wall of the turn #2 LOC-4 : TURN2BOT /\* Bottom wall of the turn #2 LOC-5 : TURN3TOP /\* Top wall of the turn #3 LOC-6 : TURN3BOT /\* Bottom wall of the turn #3 CLFP: The component fluctuation pressure load parameter database COMP-ID : 10 C-L-ID : 33 C-L-NA : HODD-F-P /\* HPOTP Discharge Duct Fluctuation Pr. LOCATION: TURNIALL /\* Location of the duct DIA-EOV : 0.333 /\* Equivalent diameter in ft FI-RATIO: 0.15 /\* Fluctuation intensity ratio, i.e. /\* the ratio of the 1-D root-mean-square /\* pressure to the flow dynamic head /\* Nominal fluctuation pressure CORLEN : 0.175 /\* correlation length SHAPE-F : 0.4 /\* Shape factor FREQ-0 : 10 /\* PSD frequency lower bound in Hz FREQ-I : 4000 /\* PSD intermediate frequency in Hz FREQ-L : 10000 /\* PSD cut-off frequency in Hz A-L-FREO: 0.81 /\* Percentage area under the low frequency /\* portion of the PSD

The fluctuation pressure load model is available in the load-expert system. However, the model requires the evaluation of the 1-D flow velocity and dynamic head which are not available in the present engine influence coefficient set but available in the expanded influence coefficient set which will be implemented in the next version of the load-expert system. A summary paper (ref. 6.3) written by the developer of the pressure fluctuation model is included as Appendix C to provide the theoretical support of this work.

# The Vibration Loads

A vibration load model, called periodic load model, was developed (ref. 6.4) which evaluates the variance of the composite vibration load which is a linear combination of a random vibration and synchronous vibration loads. Detail of the model is presented as Appendix D of this report. This model is interesting and is available as a rule module. However, further investigation is needed to develop applications of this model.

In practical applications of a vibration model, the power density spectrum of the vibration load is required. A simple model generating a piecewise linear PSD function is available in the load-expert system. The vibration model will be revisited when an application problem to the HPOTP discharge duct is developed.

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Appendix A

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Sample LDEXPT Load-Expert System Consultation Session

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# Appendix A. Sample LDEXPT Load-Expert System Consultation Session

/\* User input. Running LDEXPT EXEC proc /\* User input. Going to EXPERT SYSTEM Rules-Base Management System Knowledge-Base Management System List available COMMANDS Exit LDEXPT ?DFIT : Fit distribution ?DMLE : Estimate distribution parameters ?HELP : List available COMMANDS BUELCOME TO THE COMPOSITE LOAD SPECTRA EXPERT SYSTEM must be executed first before **TILDEXPT ===> COMPOSITE LOAD SPECTRA EXPERT SYSTEM** ?PLRW : Plot random walk time series ?PEEK : Peek data files ?PLOT : Plot the peeked data file ?ANLD : Run ANLOAD interactively ?RNDW : Perform random walk executing ?PEEK and ?PLOT # ?EXDR : Expert System driver \* . EXPUPLICATE IDENTIFIER 'GAMMA'. # \* \* \* # Available COMMANDS: # Available COMMANDS: ?KBMS ?HELP ?QUIT \* **?RBMS** ELDEXPT ===> #LDEXPT ===> ٠ \* ■.7RBMS # \* LDEXPT ŝ .....

**?REIN : Return to LDEXPT** 

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SELECT ONE OF THE ANLOAD CALCULATIONS DESIRED: (1) TURBINE BLADE LOAD CALCULATION /\*This option will be checked /\*User input. Calling expert system driver /\*This was the first time entering /\*RBMS module. The system was requesting /\*a knowledge base file DDNAME /\*User input. Calling rule module ANLDIN
 /\*for preparing ANLOAD input file (2) DEPENDENT LOAD CALCULATION
 (3) MONTE CARLO ANLOAD CALCULATION /\*This option is not
 /\*available at this time /\*User input. Selecting option 2 : Deterministic Influence Coefficient Model SLIGGN : Influence coefficients and Gain values SLIBCL : Turbine blade component load information SLDCD : Duty-Cycle-Data file information STBSM : Simple Turbine Blade Scaling Model ANLDIN : Preparing ANLOAD INput file EXIT : Return to RBMS SLIDPL : Independent load information SLDEPL : Dependent load information : Quick Look Model calculation ?QUIT : Exit from the program **MRBMS ===> RULES-BASE MANAGEMENT SYSTEM** \* # Available rule modules are : OPEN A DATABASE FILE &/or read a db table dictionary \* \* \* \* \* \* \* . OLM SICM STBSM ERBMS ===> #RBMS ===> **E.ANLDIN** EXDR. \* **8.**2 \* \* \* ŝ

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E.LUAUAB	_			ser input. u *of the load	/"USET TRPUL. USET ETLEFEU LHE VVMANE /#of the load broutedae bees
				*only LOADKB	/*only LOADKB is available this time
***** #	FROM OPNOFL ****	)fL *****	•		
# ANAME	= LOADKB	= n	14		
		GRP NAME	GRP #	# OF REC.	
				LAST GRP	
<b>EDBNREF</b>	TABLE	<b>111L</b>	-	-	/*This is a list of group
<b>#DBNREF</b>	TABLE	L 10P	-	45	/*data in the knowledge
	TABLE	LDEP	-	45	/*base. Each group is a
<b><i><b>BOBNREF</b></i></b>	TABLE	INFC	16	45	/*DATABASE except that the
	TABLE	DFAT	-	45	/*group TITL which contains
	TABLE	LTBC	-	45	/*file header information
				/*The knowled	knowledge base has six (6) DATABASE
				• TITL :	file header infor
				* LIDP :	independent load database
				LDEP :	dependent load database
				* INFC :	influence coefficient DB
				* DFAT :	duty-cycle-data database
				* LTBC :	turbine blade load database
*	*	* *	*		
	ET INDEX	GET INDEX (INDICES)	*		
•	*	* *	•		
# Please	Enter KE	Please Enter KEY Values for the desired Records Enter REANK for ALL Values of	the desi	red Records	/*Expert system requested /*user selection of IDFP-ID
			5		/#the decondent load 10
Enter	Enter .000000 fr	cnaracter type Enter -000000 for All Values of	s of		
E intege:	integer type		i		
KEY : I	: LDEP-1D	15			
EX	PERT SYSTE	EXPERT SYSTEM QUERY NEXT ***	***		
- Fl	ease selec	Please select a dependent load 10(LDEP·ID)	nt load 11	(LDEP-ID)	
En	Enter 10 number	mber			
AVI	Available LDEP-1D:	DEP-1D:			
-	HO-TB-SP	;2 HF-TB-SP;3	104-M4-0H E:	-P0;4 HF-PM-P0;5	
9	FPB-CH-P;7		8 ENG-F-FL;9		
-	F-PRS-FL;12				

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SP: SPeed; PO: discharge (Outlet) Pressure; CH: CHamber; /\*The dependent load abbreviations 16 HG-IP ;17 MCC-IEP ;18 HO-PM-PI;19 HF-PM-PI;20 PB-PM-PO; 21 HO-PM-TI;22 HO-PM-TO;23 HF-PM-TO;24 MFV-TO ;25 PB-PM-TO; 26 HF-PM-TI;27 LO-TB-SP;28 LF-TB-SP;29 HO-TB-TO;30 HF-TB-TO; 31 OPB-O-VK;32 FPB-O-VK;33 O-PRS-P ;34 F-PRS-P ;35 O-PRS-T ; 36 F-PRS-T ;37 LO-PM-SP;38 LF-PM-SP;39 HO-PR-SP;40 HF-PM-SP; 41 MCC-C-PO;42 MCC-C-TO;42 LC-TB-T0;44 LF-TB-T0;45 HO-TB-T0; 46 HF-TB-T0;47 LO-TB-T0;42 LF-TO-FL;49 HO-TB-T0;54 HF-TB-FL; 51 LO-TB-P1;52 LF-TB-P1;53 HO-TB-FL;59 LO-TB-T0;56 LF-TB-FL; 56 LF-TB-P1;57 HO-TB-T1;58 HF-TB-FL;59 LO-TB-P0;60 LF-TB-P0; 61 HO-TB-P0;62 HF-TB-P0; 61 HO-TB-P0;62 HF-TB-P0; HF: High pressure Fuel; PI: Inlet Pressure; II: Inlet Temperature; LF: Low pressure Fuel; IP: Injector Pressure; MFV: Main Fuel Valve; VP: Valve Position: I: Temperature; THRU: THRUst; ENG: Engine; HG: Hot Gas; C: Coolant; FL: FLOW: /\* MCC: Main Combustion Chamber; If /\* IT: Injector Temperature; HG /\* IEP: Injector End Pressure; HG /\* PB: PreBurner; /\* T0: discharge (Outlet) Temp; MF /\* L0: Low pressure Oxidizer; LF /\* VR: Valve Resistance; C: /\* T0: TorQue /\* HO: High pressure Oxidizer; /\* OPB: Oxidizer PreBurner; /\* P: Pressure; /\* FPB: fuel PreBurner; /\* PRS: PResSurant; /\* TB: TurBine; 0: Oxidizer; /\* PM: PUMp; /\* F: Fuel; \*

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# °.

/\*User input. Selecting the engine thrust

# OF RECORDS RETRIEVED IS -# \* \* #TOTAL \*

DISPLAY RECORD(S) OR FIELDS \* \*

# \* \* •

Enter display options

Display complete record(s)
 Display field values of the table

/*User input	/*User input	/*The database record for engine thrust	r /*User input	<pre>stions for INDEPENDENT LOADS : User selects the independent loads : Expert System selects the indep. loads based on info in BBOARD (working memory) /*User input. The user requested /*the expert system to select the</pre>
<ul> <li>(3) Display key values</li> <li>(4) No display</li> <li>7</li> <li>*?</li> <li>*.1</li> </ul>	<pre># Display format # (1) record by record # (2) in compact form # ? # ? # 1</pre>	MRECORD # 1 MLDEP-ID : 9 MLD-NAME : ENG-THRU MMEAN : 0.47107E+06 MCOV : 0.50000E-02 MP3 : 0.00000E+00 MP3 : 0.00000E+00 MNE-COEF1 : 0.10474E+04 MNE-COEF2 : 0.46729E+06 MNE-COEF3 : 0.38848E+04 MNE-COEF4 : -0.11461E+04	# # # Do you wish to select another # Dependent Load ? (Y/N) #.N	<ul> <li>Select Options for INDEPENDENT LOADS</li> <li>MANUAL : User selects the independ</li> <li>ESASIS : Expert System selects the based on info in BBDARD ("LEASIS</li> <li>L'ESASIS</li> </ul>

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/\*independent loads based on GAINS

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/*User input. The user asked the expert
    /*system to select the 10 most influen-
    /*tial independent loads
                                                                          many independent loads need to be selected
for each dependent load by the expert system ?
                                                                                                                                                                                                                                                                         /*User input.
         /*User input
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        # Please Enter the NUMBER of FIELDS or KEYS

(1) Display complete record(s)
(2) Display field values of the table
(3) Display key values
(4) No display

                                                                                                                                                                 B Selection based on which power level

C (1) 65% POWER LEVEL

C (2) 90% POWER LEVEL

C (3) 100% POWER LEVEL

C (4) 109% POWER LEVEL
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m Enter a LARGE number for Displaying
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# all FIELDS and KEYS
# Enter 0(zero) to quit displaying
#?

**N.15** 

/\*User input. 15 is larger than the
 /\*number of fields which is 10 in
 /\*this case

# .

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/\* LOX inlet pressure and temperature /\* the power level, the mixture ratio # 0.24347E-03 0.30498E-03 0.32959E-03 0.33943E-03 # 9 19 -0.74478E-02-0.31953E-01 0.00000E+00 0.00000E+00 #-0.18341E-03-0.23534E-03-0.25611E-03-0.26441E-03 # 9 6 -0.32588E-01 0.10112E+00-0.57827E-01 0.00000E+00 # 0.87097E-04 0.11582E-03 0.10708E-03 0.10034E-03 /\*duty-cycle-data profile curves for /\*User input. Selecting the test data /\*Each group except CONS includes CONS : Constant input by user STS61-A : SSME flight profile data with ID=STS61-A 902-384 : SSME AZ TEST DATA with ID=902-384 902-387 : SSME AZ TEST DATA with ID=902-387 750-262 : SSME AZ TEST DATA with ID=902-387 901-495 : SSME AT TEST DATA with ID=750-262 901-491 : SSME AT TEST DATA with ID=901-495 /\*User input /\*User input E Do you wish to change the defaults 2(Y/N)**E** Do you wish to change the defaults 2(Y/N)/\*set Available Duty-Cycle-Data files # Default values for load HFTBFM E Default values for load MOVR 0.10000E-01 0.00000E+00 P2 = 0.64000E-01 P3 = 0.00000E+00 P1 = 0.10700E-01 0.10125E+01 **1**160 = 2 .902-387 P3 = 0 н В 160 = 2. M N.M

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Appendix B

Turbine Blade Thermal Load Model

### TURBINE BLADE THERMAL LOAD MODEL

An algorithm has been developed for determining the steady-state temperature distribution in the HPFTP second stage turbine blade over the engine operating range from MPL to FPL. Geometric influences (tolerance stackup and seal wear) are included in the algorithm.

### <u>Thermal Model</u>

A three-dimensional steady-state ANSYS thermal analysis of the SSME HPFTP second stage turbine blade has previously been made on the SSME contract effort. The thermal model is shown in Figure 1. The model includes the blade, platform, and shank. The damper is not included and firtree region is accounted for with an added coarse model. A small portion of the aft region of the shank including the aft face of the shank has a nicraly/zirconium oxide thermal barrier coating to reduce the thermal gradients in this region. This coating is accounted for by adjusting the coolant side heat transfer coefficient. The airfoil itself is also coated. The model does not include this coating since, at steady-state, the airfoil operates at the turbine gas temperature with or without a coating. For a transient analysis, the coating should be considered so that the transient thermal gradients within the airfoil would be properly taken into account. The model was run for FPL conditions.

### Method of Determining Thermal Distribution

The same basic procedure used for the HGM transfer tube is also used for the turbine blade. One change for the blade analysis is that, in addition to using the maximum and minimum temperatures of the part (max.  $T_{wg}$  and min.  $T_{Wc}$ ) to scale the reference internal temperatures to other conditions, two intermediate temperatures are also used  $T_{m1}$  and  $T_{m2}$ ). These two intermediate temperatures correspond to the intermediate gas temperatures that are used in the thermal model. This has the effect of dividing the blade into three regions (the region between max.  $T_{wa}$  and the  $T_{m1}$  isotherm, the

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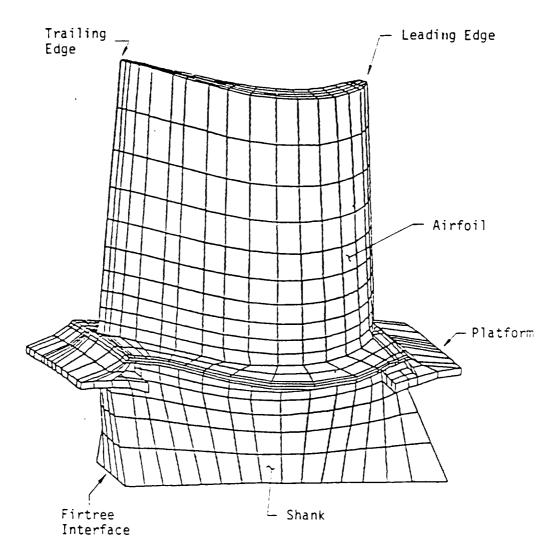


Figure B.1 Thermal Model for the SSME HPFTP Second Stage Turbine Blade

region between the  $T_{m1}$  and  $T_{m2}$  isotherms, and the region between the  $T_{m2}$  isotherm and min.  $T_{WC}$ ). These three regions correspond approximately to the airfoil and platform, the major portion of the shank, and the aft portion of the shank, respectively. These three regions will be discussed further in the section on the blade temperature distribution.

<u>Independent Parameters</u>. Because the flowrates are so high and the disk rotates so rapidly, the heat transfer coefficients are high enough that change in the heat transfer coefficients have a negligible influence on the blade thermal distribution. The thermal distribution is controlled by the fluid temperatures surrounding the blade. The following independent parameters control the fluid temperatures which surround the blade.

- Turbine inlet temperature (T<sub>in</sub>)
- Turbine discharge temperature (T<sub>out</sub>)
- Pump discharge temperature (T<sub>n</sub>)
- Geometric influence on the coolant flowrate  $(G_c)$ . This parameter is primarily determined by the tolerance stackup and seal wear. It determines the amount of coolant going to the aft face of the second stage disk. Increases in  $G_c$  correspond to increases in coolant flow (greater seal leakage).
- Geometric influence on the hot gas leakage into the coolant circuit  $(G_h)$ . This parameter is also primarily determined by the tolerance stackup and seal wear. Increases in  $G_h$  correspond to increases in hot gas leakage. There is not, as yet, enough data to determine whether the tolerance stackup or the seal wear is the predominant factor. Also, the rate at which seal wear occurs is not known (whether it occurs primarily early in testing or continues gradually from test to test).

<u>Blade Boundary Conditions</u>. The four temperatures (max.  $T_{wg}$ ,  $T_{ml}$ ,  $T_{m2}$ , and min.  $T_{Wc}$ ) used to define the thermal distribution in the blade are functions of the above five independent parameters described in the previous section. Equations for the four temperatures in terms of the five independent parameters are derived below.

The turbine hot gas  $(T_g)$  at the location of the second stage blade is a function of the turbine inlet and discharge temperatures  $(T_{in} \text{ and } T_{out})$ .

Based on hydrodynamic calculations (Fig. 2) it can be reasonably approximated by the following equation

$$T_{g} = 0.84*T_{out} + 0.16*T_{in}$$
(1)

The maximum temperature of the blade (max.  $T_{wg}$ ) is the same as the temperature of the turbine hot gas. Therefore, Equation (1) also represents the maximum temperature of the blade.

Max. 
$$T_{wg} = 0.84 T_{out} + 0.16 T_{in}$$
 (2)

The coolant temperature for the aft part of the disk  $(T_c)$  is determined by the pump discharge temperature  $(T_p)$  and the geometric influence  $(G_c)$  on the coolant flow. For baseline geometry conditions the coolant temperature is assumed to be 250°R greater than the pump temperature and to vary directly with the pump temperature.

$$T_{c} = 250 + T_{p}$$
 (3)

Experience has shown that the coolant temperature has an approximate range from 250°R to 450°R, depending primarily on the magnitude of the coolant flowrate. For a geometry influence parameter ( $G_c$ ) value of 1.0 at the reference conditions and a reference coolant temperature of 350°R the maximum range for the coolant geometry influence parameter is from 0.71 to 1.29. The 0.71 value will give a coolant temperature change of +100°R (450-350) and the 1.29 value will give a coolant temperature change of -100°R (250-350). In equation form the change in the coolant temperature due to geometric influence is

$$\Delta T_{c} = 344.8 \ (1-G_{c}) = 344.8 - 344.8G_{c} \tag{4}$$

Equations (3) and (4) can be added to give the equation for the coolant temperature.

$$T_c = 594.8 + T_p - 344.8G_c$$
 (5)

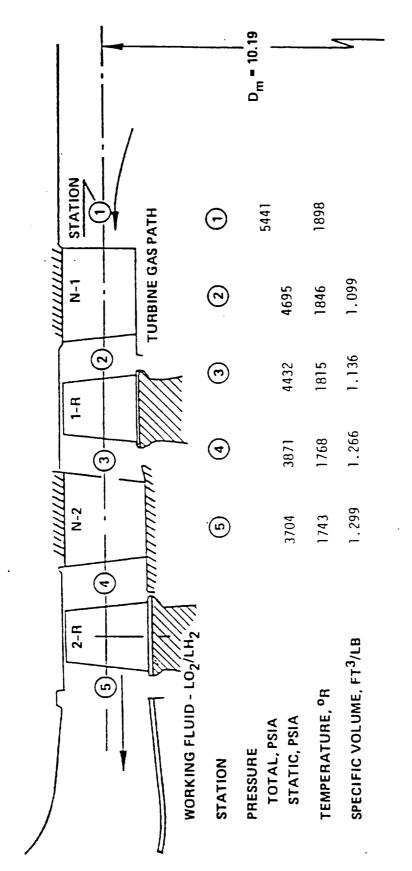


Figure B.2 SSME HPFTP Phase II Turbine Gas Data

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The minimum temperature of the blade (min.  $T_{WC}$ ) is assumed to vary identically with the change in the coolant temperature ( $T_C$ ) and to be 88°R higher than it. Using equation (5) the equation for the minimum temperature of the blade becomes

Min. 
$$T_{WC} = 682.8 + T_n - 344.8G_c$$
 (6)

The first mixed gas temperature  $(T_{ml})$  is determined from the turbine gas temperature  $(T_g)$ , the coolant temperature  $(T_c)$ , and the geometric influence  $(G_h)$  on the hot gas leakage into the coolant circuit. From the reference case data (nominal geometric conditions), the equation for  $T_{ml}$  can be given as

$$T_{ml} = 0.1325T_{c} + 0.8675T_{a}$$
(7)

There is also a geometry influence on this mixed temperature. This parameter  $(G_h)$  is set to a value of 1.0 for the reference case. Experience has shown that the mixed temperature can vary from 1350°R to 1860°R. For a reference mixed gas temperature of 1660°R, the maximum range for the hot gas geometry influence parameter becomes 0.813 to 1.12. The 0.813 value will give a change in the mixed gas temperature of -310°R (1350-1660) and the 1.12 factor will give a change in the mixed gas temperature of +120°R (1860-1660). The equation for the change in the first mixed gas temperature as a function of the geometric influence parameter can be given as

$$\Delta T_{m1} = 1660 (G_{h} - 1) = 1660G_{h} - 1660$$
(8)

Adding equations (7) and (8) and substituting equations (1) and (5) for  $T_g$  and  $T_c$ , respectively gives the equation for the first mixed gas temperature.

$$T_{m1} = -1581.2 + 0.1325T_{p} - 45.69G_{c} + 0.7287T_{out} + 0.1388T_{in} + 1660G_{h}$$
(9)

The second mixed gas temperature  $(T_{m2})$  is just the average of the first mixed gas temperature  $(T_m)$  and the coolant temperature  $(T_c)$ . By taking the average of the sum of Equations (5) and (9), the influence coefficient equation for  $T_{m2}$  is obtained.

$$T_{m2} = -493.2 + 0.566 T_p - 195.2 G_c + 0.3644 T_{out} + 0.0694 T_{in} + 830 G_h$$
 (10)

Equations (2), (6), (9), and (10) define, in terms of the five independent parameters, the four temperatures used in determining the temperature distribution.

<u>Influence Coefficients</u>. Equations (2), (6), (9), and (10) can be rewritten in influence coefficient form. The values of the coefficients are determined by multiplying the coefficient for each independent parameter in equations (2), (6), (9), and (10) by the ratio for the reference value of the independent parameter to reference value of the dependent parameter. For equation (2), this procedure is shown below.

$$\frac{\Delta \max. T_{wg}}{\text{Ref. max. }T_{wg}} = 0.84 \frac{\text{Ref. }T_{out}}{\text{Ref. max. }T_{wg}} \frac{\Delta T_{out}}{\text{Ref. }T_{out}} + 0.16 \frac{\text{Ref. }T_{in}}{\text{Ref. max. }T_{wg}} \frac{\Delta T_{in}}{\text{Ref. }T_{in}} (11)$$

The four influence coefficient equations are

$$\frac{\Delta \max. T_{wg}}{\text{Ref. max. } T_{wg}} = 0.8269 \frac{\Delta T_{out}}{\text{Ref. } T_{out}} + 0.1731 \frac{\Delta T_{in}}{\text{Ref. } T_{in}}$$
(12)

$$\frac{\Delta \min. T_{wc}}{\text{Ref. min. } T_{wc}} = 0.2283 \frac{\Delta T_g}{\text{Ref. } T_g} - 0.7872 \frac{\Delta G_c}{\text{Ref. } G_c}$$
(13)

$$\frac{\Delta T_{m1}}{Ref. T_{m1}} = 0.00798 \frac{\Delta T_{g}}{Ref. T_{g}} - 0.0275 \frac{\Delta G_{c}}{Ref. G_{c}} + 0.8038 \frac{\Delta T_{out}}{Ref. T_{out}}$$

$$+ 0.1682 \frac{\Delta T_{in}}{Ref. T_{in}} + 1.0 \frac{\Delta T_{h}}{Ref. G_{h}}$$
(14)
$$\frac{\Delta T_{m2}}{Ref. T_{m2}} = 0.0563 \frac{\Delta T_{p}}{Ref. T_{p}} - 0.1942 \frac{\Delta G_{c}}{Ref. G_{c}} + 0.6639 \frac{\Delta T_{out}}{Ref. T_{out}}$$

$$+ 0.1389 \frac{\Delta T_{in}}{Ref. T_{in}} + 0.8259 \frac{\Delta T_{h}}{Ref. G_{h}}$$
(15)

<u>Blade Temperature Distribution</u>. As mentioned previously, the blade is effectively divided into three sections. The reference isotherms for  $T_{ml}$  and  $T_{m2}$  form the internal boundaries. The physical locations of these internal boundaries (isotherms) do not change for different operating conditions. Only the temperatures associated with these two isotherms will change, being the adjusted values for  $T_{ml}$  and  $T_{m2}$ . The temperature distribution equation for each of the three sections is given below, based on the four temperatures determined from equations (2), (6), (9), and (10) and the reference conditions. Ref. T refers to the reference temperature at a specific location within the thermal model of the blade.

For Ref. T > Ref.  $T_{m1}$ :

$$T = T_{m1} + (Ref. T - Ref. T_{m1}) \frac{max. T_{wg} - T_{m1}}{Ref. max. T_{wg} - Ref. T_{m1}}$$
(16)

For Ref.  $T_{m2} \leq \text{Ref. } T < \text{Ref. } T_{m1}$ :

$$T = T_{m2} + (Ref. T - Ref. T_{m2}) \frac{T_{m1} - T_{m2}}{Ref. T_{m1} - Ref. T_{m2}}$$
 (17)

For Ref. T < Ref. T<sub>m2</sub>:

$$T = mix. T_{wc} + (Ref. T - Ref. min. T_{wc}) \frac{T_{m2} - min. T_{wc}}{Ref. T_{m2} - Ref. min. T_{wc}}$$
(18)

<u>Reference Parameters</u>. The temperature distribution from the previously constructed thermal model (ref. 2) of the HPFTP second stage turbine blade is used as the reference case. This reference case is at the FPL operating point. The values for the reference parameters are

Ref. 
$$T_{in} = 2011^{\circ}R$$
  
Ref.  $T_{out} = 1831^{\circ}R$   
Ref.  $T_p = 100^{\circ}R$   
Ref.  $G_c = 1.0$   
Ref.  $G_h = 1.0$   
Ref. Max.  $T_{wg} = 1860^{\circ}R$   
Ref.  $T_{m1} = 1660^{\circ}R$   
Ref. Min.  $T_{Wc} = 438^{\circ}R$ 

In addition, the reference temperature distribution will need to be used. This temperature distribution is saved on a file. The coordinate locations for the temperatures are also on this file.

A three-dimensional model of the second stage blade, including the firtree and the disk, has recently been run. A case has been run with this model using the same reference conditions as for the model. The thermal distribution for the blade, platform, and shank from this case could be substituted for the reference temperature distribution described in the previous paragraph. Conclusions. For purposes of this study the procedure developed for determining the thermal distribution is adequate. As this study progresses the following further work should be addressed.

- A more sophisticated approach to the influence of geometric variations should be considered.
- The geometric influence parameters (G<sub>h</sub> and G<sub>c</sub>) need to be correlated with actual engine dimensions and dimensional changes due to wear.
- A more refined second stage turbine blade model which includes the firtree and disk is now available. Eventually it should be used.
- Parameters which have a secondary influence on the temperature distribution have been ignored. Ultimately, these should be included in determining the thermal load.

# Appendix C

# Pressure Fluctuations and Correlation Lengths Summary and Critique

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Pressure Fluctuations and Correlation Lengths: Summary and Critique

Three previous I.L.s (refs. C1-C3) have documented the work that was carried out to predict the pressure fluctuations PSD and the correlation lengths for the transfer duct, high pressure oxidizer pump discharge duct (HPOPDD) and the main injector regions of the SSME for the CLS program. Figures C1-C3 summarize, in a flowchart format, the techniques established. Extensive use was made of the cold-flow experimental data and hot-fire engine data, where available, to yield these results. For example, a survey of the scaled-up transfer duct data showed that 81% percent of the energy was contained in the 10-1000 Hz range. A similar survey yielded the same energy in the 10-4000 Hz range for the HPOPDD data. These observations were used to determine the frequency domain in which the various scaling laws were valid.

Since the CLS program is generic in nature, it would be worthwhile to understand the rationale for these frequency values as a function of the flow geometry. A list of issues that need discussion are:

- i) Upper frequency bound which contains a major percentage of the energy,
- ii) Extent of correlated pressure zones,
- iii) Decay of wall pressure fluctuations, and
- iv) Separated region prediction.

### i) UPPER FREQUENCY DETERMINATION

Past research on nondimensionalizing wall pressure fluctuation data on flat plates and cylinders has shown that the displacement thickness,  $\delta^*$ , and the free stream velocity,  $U_{\infty}$ , are parameters that cause the data at differ- ent Reynolds numbers to collapse. Since this detailed information is not available for the complex flow geometries studied in this program, the best one can do is to survey the data that is available to determine the cross-over frequency at which the PSD data changes slope. In ref. Cl, an estimate

this frequency was made, based on the convection velocity and the duct radius, and a value within +20% of 1000 Hz was determined for the fuel and LOX side transfer ducts. However, the same technique yielded too low a value for the HPOPDD, since the flow geometry involves bends which lead to the wallbounded shear layers to be of different thicknesses on opposite walls. In any case, the geometries are far too complex for any simple technique to work adequately for all cases. From a review of the techniques developed in refs. C1-C3, it is observed that for "skimming" type flows, i.e., flows parallel to surfaces, the frequency at which the data shifts from a -1 or -0.4 slope (on a log-log scale) to a -5/3 slope occurs at 40% of the wideband frequency. For instance, the transfer duct data PSD frequency limits were 0-2500 Hz, and 1000 Hz was determined as the frequency below which 81% of the energy exists.

Similarly for the HPOPDD, 4000 Hz was determined as the point below which the same energy content exists, and the wideband frequency was 10,000 Hz. Similarly, a skimming-type flow exists for the main injector in the region of posts 70-71 and again, 40% of the wideband frequency limit was determined as the cross-over frequency point. In ref. C3, 75% of the energy was determined to exist in this frequency limit. For this summary report, this percentage was raised to 81% and no significant difference was observed in the PSD values. Hence, a 40% of the wideband frequency which contains 81% of the energy appears to hold true for the data studied.

As a check, a data set for measurements taken on the LOX-side transfer duct, which was analyzed in the frequency ranges of 0-2500 Hz and 0-10,000 Hz was used to check this hypothesis. Figures C4 and C5 show the result of this exercise. The results show that the fit to the data is rather good. This means that either there is proportionately the same amount of energy in the 10-1000 Hz range or that the addition to the energy from 1000-4000 Hz is not significant. Since the composite rms values (3.51 psi and 3.56 psi) are almost the same, the latter observation is true.

Consequently, one has to make sure that the data has been analyzed using an adequate frequency range so that a large fraction of the energy has not been omitted for this technique to work. Of course, by the same token, one cannot increase the upper frequency limit at random and expect the technique to work. A realistic bandwidth should be chosen based on either observing the highest frequencies seen in the data or basing it on past experience.

For the main injector, at posts O1-O2, a stagnation-type flow is envisioned. This is especially true for the top, i.e. towards the LOX dome, location. Revisiting the data in ref. C3, it is observed that a 40% split does hold true (ref. Fig. C6) provided one uses a geometric shape factor, S = 0.99 for the computer program or S = 1.0, if one determines the coefficients  $K_0$  and  $K_1$  explicitly, as was done for the initial analysis in ref. C1.

Hence, as a rule of thumb, a 40% value of the wideband frequency can be used as a guideline for the frequency at which the PSD changes slope. Also, in general, a shape factor value of S = 0.4 is advisable for flows which are separated or with adverse pressure gradient, since these conditions lead to more energy at the lower frequencies. Otherwise, S = 1 will generally prove to be adequate to predict the PSD decay.

With regards to predicting P<sub>rms</sub> values, significant differences are observed, depending upon the region under consideration. For geometries that do not have separated regions, it is observed that P<sub>rms</sub> values of 0.15  $q_{1-D}$  or 0.30  $q_{1-D}$  can be used, depending upon accelerating or decelerating regions, respectively. This is observed to be true for both the two-duct transfer duct and the HPOPDD data, where  $0.15q_{1-D}$  was used. Large departures from these values are observed when one uses estimates of  $q_{1-D}$  which do not hold true over a major portion of the flow. This is observed in the three-duct hot gas manifold where it is known that a large area of the center transfer contains separated flow. Consequently, the effective flow area is reduced, leading to a higher  $\gamma$  value. Yet, since this study is generic in nature, detailed information regarding the flowfield is not known. Consethe  $p_{rms}/q_{1-D}$  ratio result quently, large estimates of based on

one-dimensional estimates. Furthermore, because of the complex nature of the flow in the main injector region, the local value of q could be almost an order of magnitude different from  $q_{1-D}$  depending upon the location. Again, from a generic viewpoint, the values shown in Figure C3 essentially bracket the  $P_{\rm rms}$  based on one-dimensional estimates of q in the transfer duct, and should be used. It should be mentioned that a similar analysis should be done for the two-duct hot gas manifold to determine the  $P_{\rm rms}/q_{1-D}$  variation.

### ii) CORRELATION ZONE DETERMINATION

An estimate of the correlation length is obtained by determining the integral time scale and multiplying it by the convection velocity. The procedure is outlined in ref. Cl. The upper limit for the integration is typically set equal to a characteristic dimension divided by the convection velocity (equal to 0.6 times the  $U_{1-D}$ ). Since this study limits itself to wall pressure fluctuations, the extent of the correlated zone is of importance. Two surfaces that describe any surface are: flat and curved. For flat surfaces, Willmarth and Wooldridge (ref. C4) have shown that both the transverse and longitudinal scale are on the order of the boundary-layer displacement thickness. The transverse and longitudinal scales of both large and small-scale wall pressure fluctuations were also found to be approximately the same. For this study, curved surface geometries are more applicable. Past research on determining the ratio of longitudinal to transverse length scales (ref. C5 and C6) have shown that the transverse scale is typically smaller than the longitudinal scale. For flowthrough straight pipes, ref. C5 quantifies this ratio to be approximately 0.5. Qualitatively, this can be explained visualizing a large eddy adjacent to a curved wall. For a convex surface, it is apparent that in the transverse direction, at either side of the periphery of the large eddy, the mean velocity would be higher than it would be at the sides of the same eddy in a plane boundary layer. Thus, there is a streamwise shearing motion along the sides of large eddies in a boundary layer with transverse curvature that is not present in a plane boundary layer. This shearing motion also acts to reduce the transverse scale of the large eddies. A similar scenario can be envisioned for a concave surface, e.g. flow inside a

pipe. In this case, the edges of the large eddy are experiencing a lower mean velocity than the center. Again a streamwise shearing action ensues, thereby reducing the extent of the transverse scale. It should be noted that if  $\delta^*$ , the displacement thickness, is taken as a measure of the scale of turbulence, and if indeed the data does scale in the -5/3 slope regime, then one can use this technique to determine another estimate of the length scale, as follows.

If, for instance, for the LOX side transfer duct one determines, at f = 1000 Hz,:

$$\omega \delta^* / U_c = \frac{(2^* \pi^* 1000)^* (2.50/12)}{(0.6^* 386)}$$

= 5.65.

Then equating this value of  $\omega \delta^*/U_c$  to the HPOPDD case yields:

 $\delta^*_{HPOPDD} = 0.24$  inches,

which is almost an order of magnitude smaller than that predicted in ref. C2. This difference signifies the complexity of the flow and danger of putting too much faith in a single point measurement. From a worst-case point of view, obviously, the larger value for the correlation length scale should be used. Similarly, for the main injector, one obtains:

$$\delta^*_{MI} = 1.84$$
 inches,

which compares well with values obtained in ref. C3.

iii) DECAY OF WALL PRESSURE FLUCTUATIONS

In order to obtain a more realistic estimate of the extent of the correlation zone, it is best to determine the decay of the wall pressure fluctuations. It

should be noted that the correlation length discussed earlier is the average size of the large scale, energy-containing eddy over which the eddy retains its characteristics. Thus, by using this to be the length over which the pressure-producing eddy is fully correlated is, in a sense, assuming worst-case conditions. In reality, due to viscous interaction and dissipation, both large- and small-scale pressure producing eddies decay after travelling a distance proportional to their scale (ref. C4). More precisely, a pressure-producing eddy of large or small wavelength  $\lambda$  decays and vanishes after travelling a distance of approximately  $6\lambda$ .

In order to relate the PSD at one point to another point requires an in-depth knowledge of the flowfield. This has been done in ref. C4 for measurements over a flat plate turbulent boundary layer and analyzed in ref. C7 to yield the expression shown below:

$$PDS (\xi,\eta,\omega) = PSD (0,0,\omega)A(\omega\xi/U_c)B(\omega\eta/U_c)exp(-i\omega\xi/U_c)$$
(1)

with the corresponding space-time correlation given by:

$$R(\xi, o, \tau) = \int PSD(o, o, \omega) A(\omega\xi/U_{r}) exp[i(\omega\tau - \omega\xi/U_{r})] d\omega$$
(2)

and

$$R(o,\eta,\tau) = \int^{\infty} PSD(o,o,\omega) B(\omega\eta/U_{c}) exp[i\omega\tau] d\omega$$
(3)

In eq.(1), functions A and B are determined experimentally, see Figs. C7 and C8, and can also be fit by the following two expressions:

$$A(\lambda) = \exp(-0.1145|\lambda|) + 0.1145|\lambda| \exp(-2.5|\lambda|)$$
(4)

$$B(B) = 0.155 \exp(-0.92|B|) +0.70 \exp(-0.789|B|) +0.145 \exp(-2.916|B|) +0.99 \exp(-4.0|B|)$$
(5)

where  $\lambda = \omega \xi / U_c$  and  $\beta = \omega \eta / U_c$ . The variation of  $U_c$  with the frequency is shown in Figure C9. Thus, using these relationships it is feasible to predict the PSD as a function of distance from a reference location where the PSD is known. A similar database, developed by Willmarth and Yang, flows over cylinders aligned with the flow.

In order to develop this capability for the CLS program, an experimental program needs to be carried out to develop this database for geometries relevant to the program. Since data for such geometries is scant, the best one can do is to use the PSD prediction technique in conjunction with the correlation lengths described earlier.

## iv) SEPARATION REGION PREDICTION

Separated regions are of interest because they lead to irrecoverable total pressure loss which can lead to degraded engine performance. In addition, large values of the PSD at low frequencies are observed, which, if they are coincident with the resonance frequency of the local structure, could lead to structural problems or failures.

Furthermore, the streamwise extent of the separated region is usually larger than the normally computed correlation length. This, therefore, leads to larger, correlated pressure zones which also aid to amplify the problem.

Typically, the prediction of separated regions requires a detailed knowledge of the flowfield. As a minimum, for instance, a wall static pressure distribution is needed to determine if adverse pressure gradients exist which could lead to flow separation. Ideally, this information should be coupled with velocity measurements that are capable of resolving flow reversals.

However, this is unrealistic for the time being since no program currently exists to measure, in a nonintrusive manner, the flowfield in a hot-fire engine test. Thus, for the current wall, static pressure distribution coupled with high frequency pressure fluctuation measurements are more realistic. It

C-8

is anticipated that the current database will be substantially increased with the advent of the technology test bed program.

For the present, however, one is left to make intuitive judgments with regard to separated regions based purely on geometric considerations and past experience. For instance, the axisymmetric turnaround duct program (ref. C8) showed that a separated region exists starting at the 154 deg location on the inner wall of the duct. Similarly, the solid wall hot gas manifold test program (ref. C9) showed that the center transfer duct of the three-duct configuration contained flow which was essentially all separated.

Past work on flow through pipes with bends could also be researched in the literature to determine the relationship between Reynolds number, bend geometry and incoming turbulence intensity.

The bottom line is that quantitative separation zone prediction for the complex geometries being studied is difficult at best. One has to revert to past experience or intuitive judgment. Of course, with the continued development of computational fluid dynamics models, these predictions could also be used to aid in this process. However, current CFD capability is not at the point where it can be used routinely and cost-effectively for complex threedimensional geometries that are of interest in the rocket engine environment.

## CONCLUSIONS

A technique has been determined which can be used to predict the PSDs and the correlation lengths for the transfer duct, HPOPDD, and the main injector region of the SSME. The technique has been based on existing cold-flow or hot-fire engine data. It is observed that generally good agreement is achieved with other existing PSD data. However, the level of the PSD or the  $P_{\rm rms}$  level is a strong factor for the turbulence intensity assumed. Based on one-dimensional estimates, large variations in the  $p_{\rm rms}/q_{\rm 1-D}$  ratio are observed when different regions are compared. This issue can be only resolved

C-9

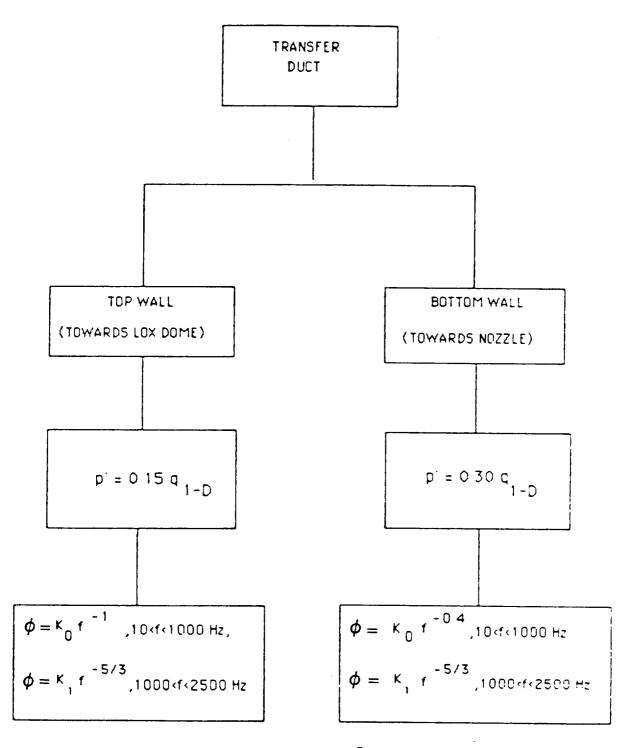
by acquiring more experimental data, thus widening the database. Similarly, due to the lack of a detailed database, no assumptions can be made regarding the decay of the wall pressure fluctuations. This knowledge would ultimately resolve the question of how the entire structure is loaded. This currently is a weak point since it is not known whether the locations at which past measurements have been made are those at which the turbulence is greatest. Such detailed information would give clues to the existence of separated regions since velocity profile measurements are not forthcoming in the near term.

Summarizing, the technique developed in the current study is a step in the right direction since it is anchored to actual data rather than intuitive guesses regarding the turbulence levels. Also, the PSD prediction is compared with actual data rather than data obtained from geometries which have little or no resemblance to those in a rocket engine. Future verification of the technique developed herein will be based by comparing it with more data as it becomes available.

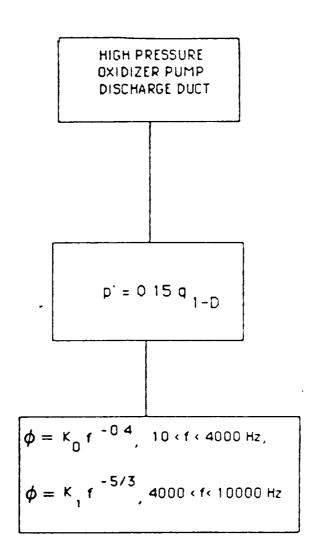
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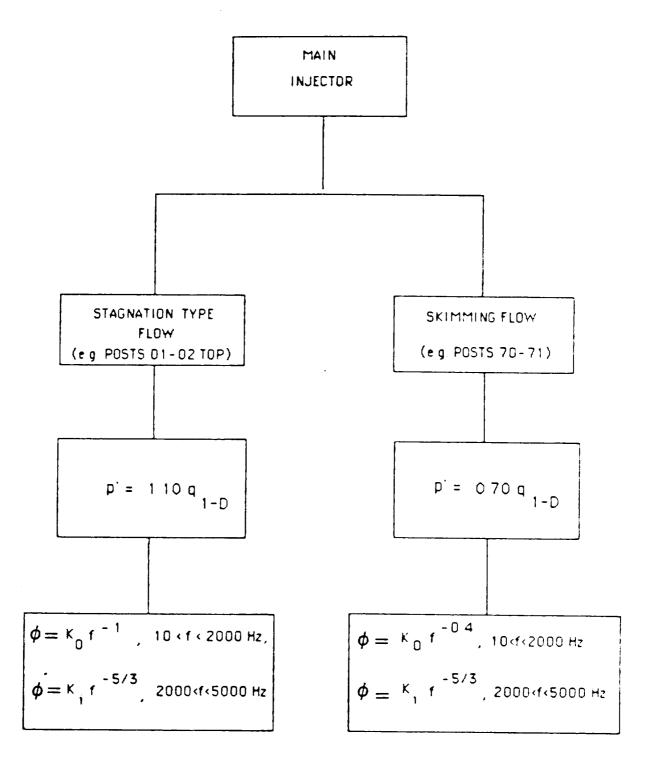


To evaluate K<sub>0</sub> and K<sub>1</sub> need to assume  $0.81 \text{ p}_{rms}^2$  in the frequency range 10 < f < 1000 HzFigure C1. Flow Chart to Determine Transfer Duct PSDs

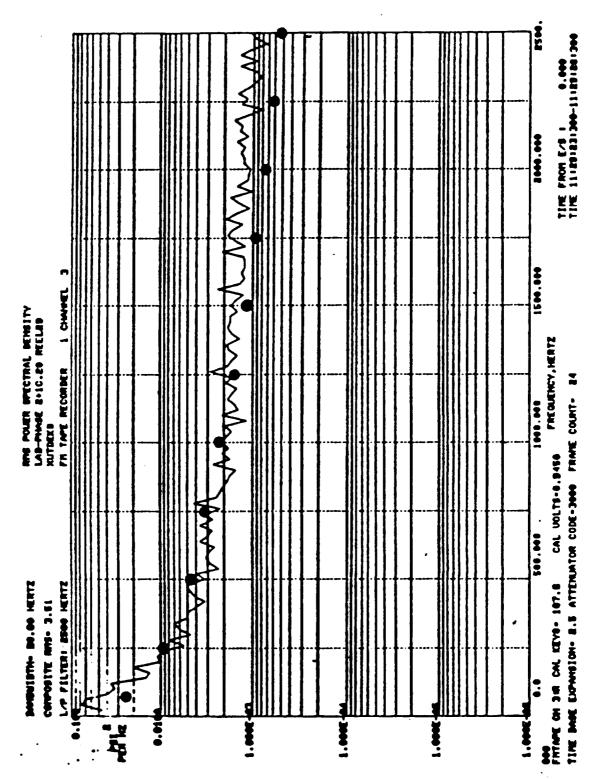


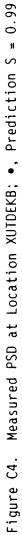
To evaluate K and K need to assume 0.81 p  $\frac{2}{rms}$  in the frequency range 10 < f < 4 000 Hz

Figure C2. Flow Chart to Determine HPOP Discharge Duct PSDs



To evaluate  $K_0$  and  $K_1$  need to assume 0.81 p $\frac{2}{rms}$  in the frequency range 10 < f < 2000 Hz Figure C3. Flow Chart to Determine Main Injector PSDs





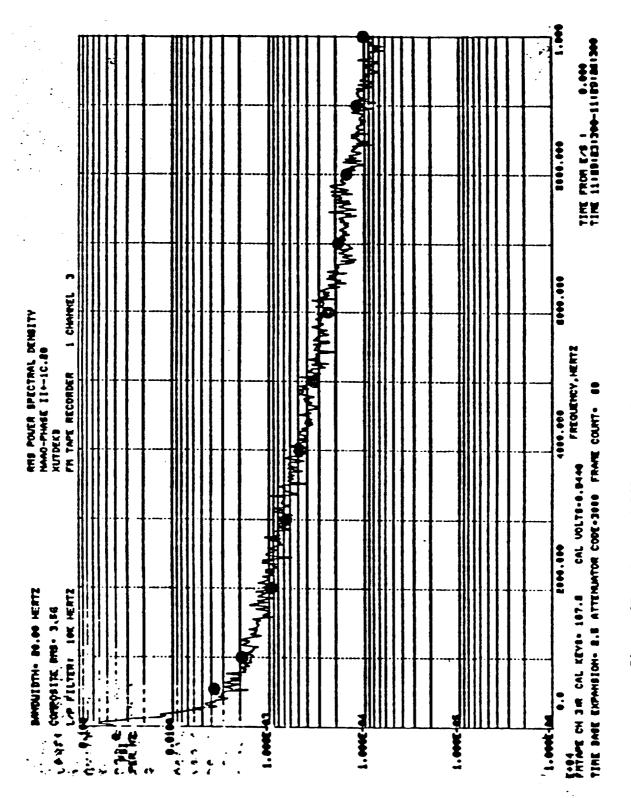
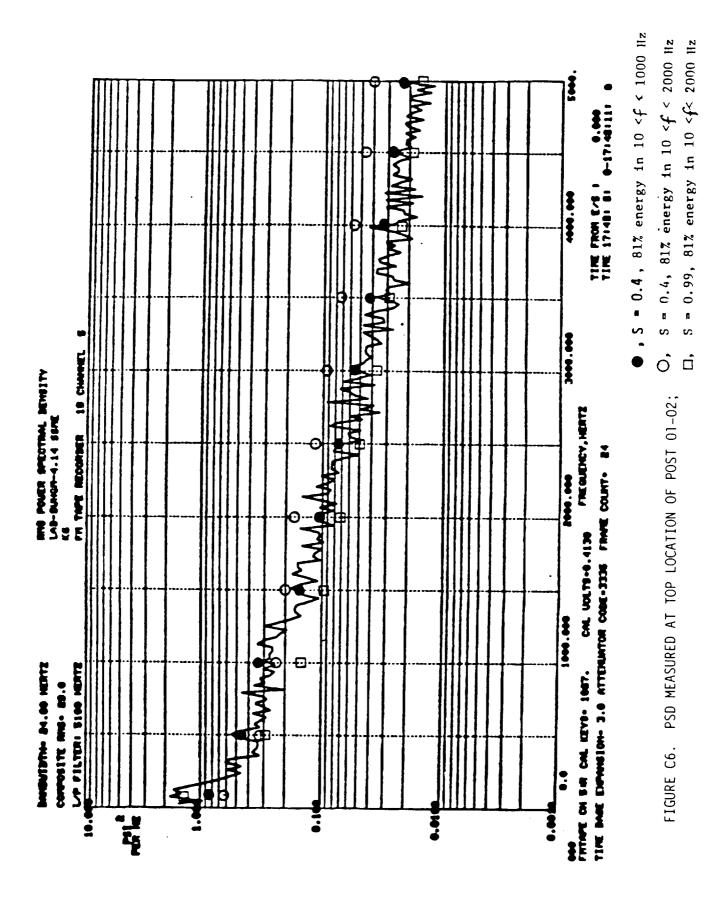


Figure C5. Measured PSD at Location XUIDEKB; •, Prediction S = 0.99



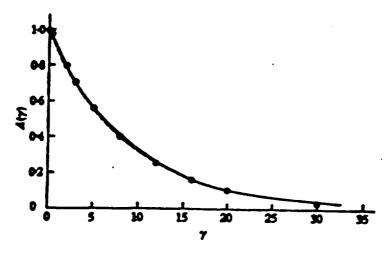


Figure C7. The Function A( $\gamma$ ),  $\gamma = \omega E/U_{c}$ \*

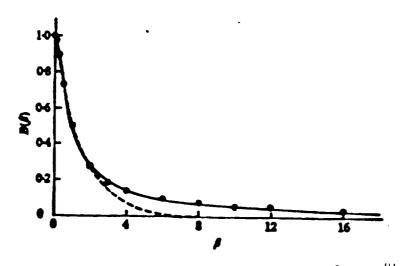


Figure C8. The Function B(B),  $\beta = \omega q/U_{c^*}$ 

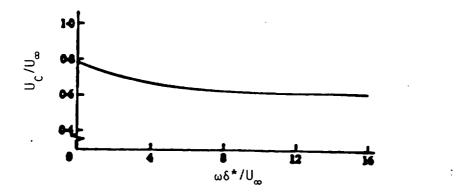


Figure C9. The Dependence of Convection Velocity on Frequency

Appendix D

Periodic Load Model

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#### PERIODIC LOAD MODEL

## <u>Introduction</u>

The modeling of vibration or, more generally, periodic loads, requires that a more rigorous treatment of dependent load models be developed. This is because the forced vibration loads, especially at multiples of pump speed (in the frequency domain) show a strong dependency. The variability in the predicted load will also be incorrect if the dependence effect is not accounted for in the model. In fact, when the correlation is in position, the variability will always be underpredicted. Therefore, a more thorough treatment of these types of loads has been developed.

### Model Development

The basic model requires some estimates of the correlation between various types of vibration loads. These correlations are then used to predict the spread in the variable of interest. As an example, assume that one is interested in the composite vibration load, where the composite load is composed of all of the synchronous and random levels for all frequencies. The composite load, denoted C, is given as a function of a constant term and the synchronous vibration magnitudes:

$$C = a_0 + a_1 L_1 + \dots + a_m L_m$$
<sup>(2)</sup>

where  $L_i$  is the magnitude of the i<sup>th</sup> synchronous level and the coefficients,  $a_i$  are to be determined. It is worth noting that this can just as easily be written as the first synchronous load,  $L_1$ , as a function of the composite level, C, but this is the example chosen for discussion.

For the model shown in Equation (1), how does one predict the composite levels? To do this we will need to compute the covariance matrix of the individual inputs,  $L_i$ , of the model. But first it is wise to adopt some additional notation and normalize some terms.

First we denote the normalized load levels as  $N_{i}$  and

calculate N; as:

$$N_{i} = (L_{i} - m_{i})/s_{i}$$
 (2)

where  $m_i$  is the mean of  $L_i$  and  $s_i$  is the standard deviation. The actual equation which will fit is then given by:

$$C = c_{0} + b_{1}N_{1} + \dots + b_{m}N_{m}$$
(3)

If we denote the variance of C by Var(C), then

$$Var(C) = b^{\mathsf{T}} R b \tag{4}$$

where b is the vector composed of the coefficients in Equation (3) and R is the matrix of the correlation coefficients,  $r_{ij}$ , between variable  $L_i$  and  $L_j$ .

At this point we take advantage of some useful properties of the covariance matrix, R. We know that the matrix Q, whose columns consist of the eigenvectors of R can be used to reduce Equation (4) to the form:

$$Var(C) = \Sigma q_{i} p_{j}^{2}$$
(5)

where  $q_i$  are the eigenvalues and  $p_i$  are the components of the vector obtained by multiplying b times  $Q^T$ .

To perform calculations using these equations, it becomes necessary to examine the available data to obtain estimates for  $m_i$  and  $s_i$ , i.e. the mean and standard deviations for the i<sup>th</sup> synchronous load level.

Most of the available data deals with maximum PSD values over the test or mission. These values are used to monitor the wear and health of various engine components, but they do leave out some of the statistical information that is needed. Therefore, the probabilistic information is obtained from the database, assuming that the peak values represent a three-standard deviation spread from the mean value. A visual examination of tracking filter data indicates that a COV value is approximately 20%. This implies that the mean and standard deviation values can be found from the following set of equations:

Of course, it is assumed that the PSD values are distributed normally about their mean values. The peak amplitudes are obtained from data analyses. Figure D1 shows the distribution of peak values for both pump and turbine data for 104% and 109% power levels. This data represents the HPFTP peak PSD data where an ll-point moving average has been used. It is interesting to note that the 109% power level curve is to the left of the 104% power level curve.

The other factor to examine is the variability in the vibration type load with location. Figures D2 through D5 show this variation for composite and synchronous pump data at both 104% and 109% power level. The turbine data has also been examined but the plots do not provide any new information; therefore, they are not included.

This information is useful for obtaining peak amplitudes for vibration loads either for pumps or turbines and adjusting for location. However, the peak amplitudes cannot be obtained as independent random variables, as has been done previously, since there is a high degree of correlation between some of the synchronous modes. The correlation of the peak composite data with the peak synchronous data is shown in Figures D6, D7, and D8. The correlation of the composite and synchronous data has a correlation coefficient of 0.818 when all of the power level data is included: 0.797 for the 104% power level data, and 0.987 for the 109% data for the pump radial position (0). The other

D-4

correlation coefficients for the remaining locations is shown in Table 1. The plots of these remaining data sets do not show any new information, they just more or less scatter about the trend lines and therefore are not included.

New information is obtained when higher multiples of the pump or turbine speeds are examined. For the 2N, 3N, and 4N multiples, there is little correlation among the peak amplitudes. This is shown in Figures D9 and D10. In Figure D9 we see the same plot as in Figure D7 but now the 2N data is superimposed on top of that plot. As this figure indicates, there is a clear relationship between the composite and synchronous data, but a very weak one between the composite and the 2N data. The relationships between higher multiples is even weaker, as indicated in Figure D9.

At this point it is noted that after this analysis was performed, it was discovered that the data for the PSDs found in Table 1 were taken only through 850 Hz. This implies that a significant portion of the energy imparted to the engine, due to the 2N, 3N, and 4N forced vibration levels, is not represented in the PSD values. While this is a problem for calculating the coefficients that will ultimately be contained in the expert system, it is not a problem for the purposes of this sample calculation. What will be changed when the complete frequency range is changed is the coefficients in the matrix R. However, a change in the numerical values will not affect the methodology.

To provide additional clarification of the steps taken so far, a sample calculation is performed. The data for this calculation is shown in Table 1 where the composite, synchronous, and pump multiple forced vibration loads, through four times the pump speed (4N), are shown. These data were analyzed to produce the correlation coefficients shown in Table 2. The data in Table 1 depicts the peak amplitudes measured during 63 separate tests. There are additional tests available for the composite and synchronous levels, but the data were missing for higher multiples. Since we are concerned with developing correlations, only these 63 tests were used. Ultimately, the actual PSD levels used in the vibration model will be transformed by Equation (6) where it is assumed that these peaks are at the 3-sigma level.

D-5

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Composite	Synchronous	2N	3N	4N
2.3	0.5	1.4	1.1	0.9
2.4	0.8	0.8	1.2	1.9
2.5	1.7	0.7	1.3	0.7
2.6	1.8	0.7	0.8	1.0
2.9	2.2	1.6	0.9	0.9
3.0	2.0	1.8	0.9	0.9
3.1	2.3	0.9	1.2	1.2
3.1	2.0	1.0	1.5	1.0
3.2	2.2	1.6	0.9	1.1
3.2	2.4	0.6	1.7	0.9
3.2	2.0	0.8	0.8	2.3
3.3	2.2	0.8	1.0	0.9
3.4	2.5	0.5	1.1	1.0
3.4	2.6	0.5	1.4	1.3
3.5	2.7	0.5	0.6	1.0
3.5	3.0	1.8	0.9	1.4
3.5	2.2	0.9	1.3	1.9
3.6	2.8	1.0	0.7	0.8
3.6	2.9	0.9	0.9	0.6
3.6	2.9	0.6	1.0	0.8
3.6	2.5	1.0	1.1	1.9
3.7	2.9	0.7	1.4	0.8
3.7	2.7	0.9	1.4	0.8
3.8	2.6	2.4	1.3	1.0
3.8	2.0	0.9	1.0	0.7
3.9	2.9	0.6	1.2	1.6
3.9	3.2	0.8	0.5	0.7
3.9	3.0	0.9	1.8	1.1
4.0	3.1	2.4	2.0	1.4
4.1	2.0	2.2	1.4	1.7
4.1	3.4	0.5	1.4	1.2
4.2	3.3	2.2	1.6	0.9

# TABLE 1. VIBRATION LOAD DATA USED FOR SAMPLE CALCULATION

Synchronous Composite 2N 3N 4N 4.2 3.2 0.9 1.0 1.2 4.2 3.4 0.6 1.2 1.5 4.2 3.3 0.8 1.0 1.4 4.2 3.4 0.9 1.8 0.8 4.2 3.5 0.6 1.0 1.0 4.5 2.7 1.1 1.0 1.0 4.7 4.1 1.4 1.0 3.3 4.9 3.2 1.2 1.2 1.4 4.9 4.5 1.8 1.3 2.1 4.9 4.2 0.6 1.0 1.0 4.9 4.1 1.9 1.0 1.3 1.4 5.0 4.2 2.1 1.2 5.4 4.7 1.1 1.1 0.9 5.4 4.6 1.5 0.8 0.9 5.5 4.8 1.0 1.0 1.2 5.8 5.1 1.1 1.1 1.0 5.0 5.9 1.0 0.9 0.8 5.9 5.2 1.3 0.9 · 1.0 5.9 5.4 0.9 1.9 1.0 6.1 5.4 1.6 1.0 1.5 6.1 5.4 0.9 1.1 1.1 6.2 5.4 0.8 1.9 1.4 6.5 5.2 1.1 1.1 0.9 6.8 6.2 1.0 1.0 0.6 6.9 6.4 1.9 1.4 1.0 6.7 0.9 7.5 1.6 1.6 7.8 6.2 1.2 1.8 0.9 9.3 9.0 2.0 1.0 1.3 9.4 9.0 1.7 1.2 0.9 9.7 8.8 2.2 2.3 1.6 4.2 10.8 2.0 1.7 1.7

TABLE 1. (Concluded)

During the first phase of this program, there are no physical model requirements for the vibration model. Therefore, the probabilistic synthesis of the individual components into an overall composite, random vibration load is being accomplished by a simple linear fit:

Composite = 
$$a_0 + a_1 L_1 + a_2 L_2 + ... + a_n L_n$$
 (7)

where L<sub>j</sub> is the individual synchronous loads and a<sub>j</sub> are the coefficients obtained from regression analysis. The variability in the composite load can then be obtained, using the variance as a measure of the variability from the covariance matrix:

$$Var(C) = b^{T} R b$$
(8)

where b is the vector of normalized coefficients  $(b_1, \ldots, b_n)$ , and R is the covariance matrix. The covariance matrix is made up of elements given by:

$$R_{ij} = r_{ij} \cdot s_i \cdot s_j \tag{9}$$

where  $r_{ij}$  is the correlation coefficients between variables i and j,  $s_i$  is the standard deviation of variable i, and  $s_j$  is the standard deviation for variable j. This provides a first approximation model for the composite, periodic load spectrum.

Before proceeding with additional calculations, it is necessary to first describe the numerical procedure used and how the eigenvalues and eigenvectors are determined.

D-8

## 

With:	С	L,	L,	L,	L,
С	1	0.903062	0.405069	0.343665	0.030434
L	0.903062	1	0.329034	0.273249	0.038454
L <sub>2</sub>	0.405069	0.329034	1	0.274478	0.147398
L <sub>3</sub>	0.343665	0.273249	0.274478	1	0.087954
L <sub>4</sub>	0.030434	0.038454	0.147398	0.087954	١
	///////////////////////////////////////		///////////////////////////////////////	///////////////////////////////////////	///////////////////////////////////////

## The Calculation Of Eigenvalues And Eigenvectors

The eigenvalue and eigenvector calculation is performed numerically using the Leverrier method as modified by Faddeeva (ref. D1). This method was selected because it simultaneously calculates the eigenvalues, eigenvectors and inverse matrix. It is somewhat of a brute force technique but is robust; just the type of method that is needed for generic applications.

For the R matrix (shown in Table 2 in rows 2 through 5 and columns 2 through 5), the eigenvalues and eigenvectors which were calculated are shown in Table 3. Because the covariance matrix is real and symmetric, a simple check of the accuracy of the calculation can be made. This check is performed by multiplying the eigenvector matrix, Q (ref. Table 3) by its transpose. This should produce the identity matrix. The calculation demonstrated four significant figures after the decimal point which was judged to provide the needed accuracy for these calculations.

At this point we can begin the calculation for the variance of the composite load, Var(C). If we use the correlation coefficients of C with the forced vibration levels, then these correlation coefficients represent the  $b_i$  in Equation (3). If we compare Equations (1) and (3), it is clear that in the calculation of the variance vector b in Equation (4) must be changed to

TABLE 3. EIGENVALUES AND EIGENVECTORS FOR SAMPLE CALCULATION Eigenvalues: 1.62570E+00 9.78083E-01 7.43709E-01 6.52502E-01 Eigenvectors:  $Q_3$ Q<sub>2</sub> Q  $Q_4$ 5.56692E-01 -3.12676E-01 3.92960E-01 -6.61853E-01 5.85605E-01 2.03978E-02 3.86287E-01 7.12258E-01 5.34772E-01 -1.31845E-01 -8.34468E-01 1.68408E-02 2.47343E-01 9.40444E-01 5.24853E-03 -2.33145E-01 

$$b' = (b_1 . s_1, ..., b_m . s_m)$$

Therefore:

$$Var(C) = \Sigma b_{i}^{2} \cdot s_{i}^{2} \cdot q_{i}$$
 (10)

The mean values and the standard deviations calculated from the data are shown in Table 4. Using these values for the standard deviation  $s_i$ , the correlation coefficients from Table 2 for the composite with four synchronous levels for  $b_i$ , and eigenvalues from Table 3 for  $q_i$ , the variance of the composite level is found to be:

## Var(C) = 3.08682

Taking the square root yields an estimate of the standard deviation for the composite load of 1.745 which compares very well with the value of 1.826 found from the data analysis. Generally, we do not expect agreement that is this close because the entire frequency range has not been included. To check, the entire analysis was repeated for the pump radial position (90). For this analysis, the calculated standard deviation for the composite vibration PSD is 1.435 while the data analysis gave a result of 1.852. While these are of the

same order, we would expect the agreement to improve as more of the frequency range is included. This expectation arises because the covariance matrix did not include all of the cross-correlations and, thus, the estimated variance should be low (for positive correlation). However, standard deviations should not match exactly because there is still one other source of variability that

# TABLE 4. MEAN AND STANDARD DEVIATIONS FOR VIBRATION DATA

 Composite
 Synchronous
 2N
 3N
 4N

 Mean:
 4.719047
 3.711111
 1.171428
 1.215873
 1.180952

 Standard
 Deviation:
 1.825903
 1.795772
 0.528678
 0.356440
 0.463546

has not been accounted for in analysis. This source of variability is the random component of the periodic load.

To account for the random portion of the composite PSD, we modify Equation (3) to include this component:

$$C = c_{0} + b_{1}N_{1} + \dots + b_{m}N_{m} + b_{m+1}Z$$
(11)

where Z is the random component. Because the random component must, by definition, be uncorrelated with all of the other modes, the covariance matrix will have another row and column added that contains all zeroes except the (m+1,m+1) component which will be equal to 1. That is, the new covariance matrix, denoted R', is given by:

It is a well known fact from linear algebra that this modification to the covariance matrix will leave the original eigenvalues and eigenvectors unchanged. It will introduce a new eigenvalue equal to 1 and an eigenvector equal to the identity matrix column. Therefore  $b_{m+1}$  will be equal to 1 and the variance of the random component can now be calculated from:

$$Var(Z) = Var(C) - \Sigma b_i^2 s_i^2 q_i$$
(12)

TABLE 5: CORRELATION COEFFICIENTS BETWEEN COMPOSITE AND SYNCHRONOUS DATA

Location	Corre	lation Coe	efficient
	A11	104%	109%
	Data	Power	Power
Pump Radial (O)	0.818	0.797	0.987
Pump Radial (90)	0.740	0.761	0.657
Pump Radial (174)	0.719	0.693	0.845
Pump Radial (186)	0.729	0.735	0.819
Turbine Radial (90)	0.554	0.594	0.491
Turbine Axial	0.874	0.873	1.000*
Turbine Radial (180)	0.642	0.702	0.661

\*Only two data points were in this data set, the remaining sets had as few as 21 and as many as 89.

Table 5 presents the results of these calculations for a variety of pump and turbine positions. In some cases, the variance of the composite PSD is less than the predicted value from the correlated data analysis. This is believed to be due to the restricted range of frequencies that are used for the data collection and is not indicative of the results which would be obtained from a more complete frequency spectrum. There is one interesting trend in the data that shows that the 90-deg positions for both pump and turbine loads has a larger correlation contribution to the variance than the (approximately) 180-deg position. This may warrant further investigation when the frequency range is increased.

## Changing The Peak Values to Nominal Values

All of the calculations performed to this point have been for the peak value data. As was previously discussed, the mean and standard deviation for the nominal PSD levels are calculated using the previous set of equations. Now, we can simply estimate the variance of the composite load for the nominal conditions using this equation. Therefore, the standard deviation is changed by dividing by 8 and the new variance of 0.38585 is obtained.

This model has been used to compare its prediction with the available data. A typical plot is shown in Figure Dll. In this figure, the actual data is compared to the prediction obtained from RASCAL. The mean predictions remain accurate but the standard deviation, or spread in the data, is underpredicted. This is primarily due to the limited number of samples available from these runs. The cases are being reanalyzed to determine if the smaller predicted variability is due to the method or to the need to increase the sample space selected for the analyses.

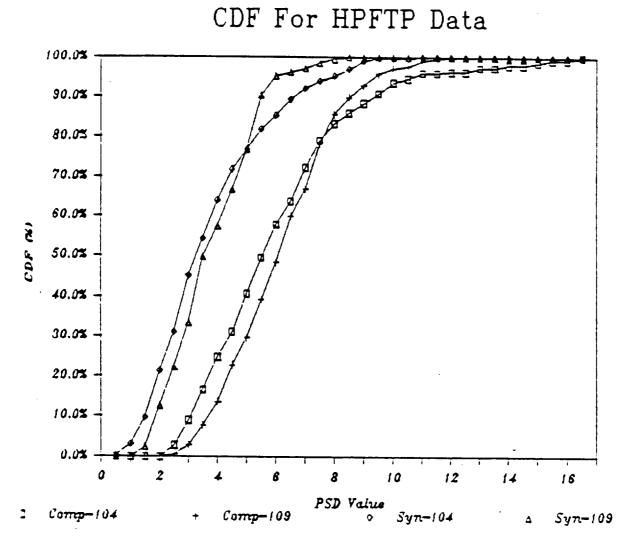


Figure D1. Cumulative Distribution Functions for Peak PSD Values

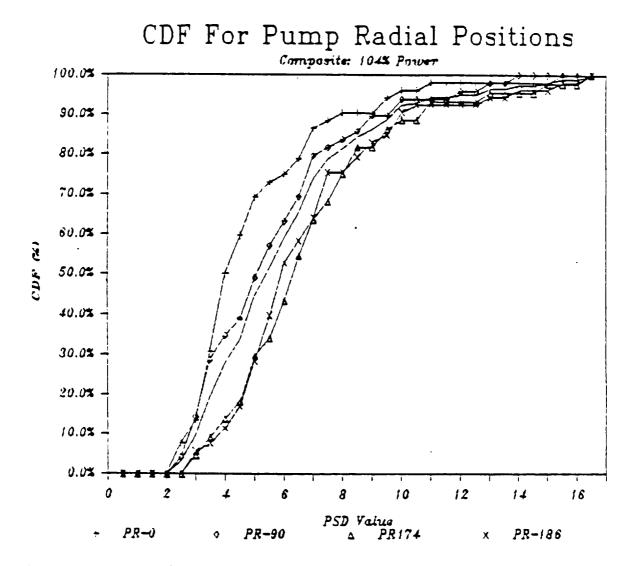


Figure D2. Cumulative Distribution Functions For Differing Pump Locations

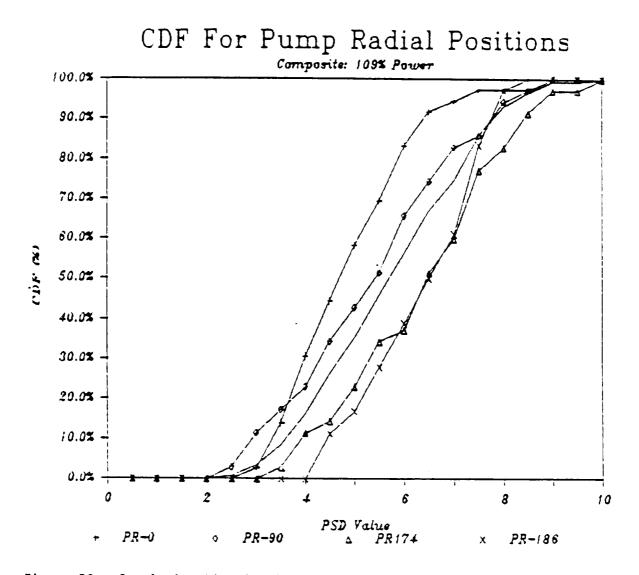


Figure D3. Cumulative Distribution Functions For Differing Pump Locations

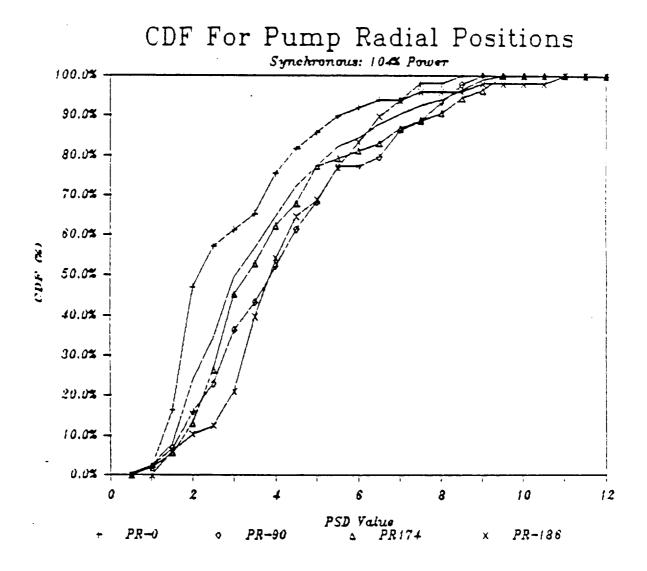


Figure D4. Cumulative Distribution Functions For Differing Pump Locations

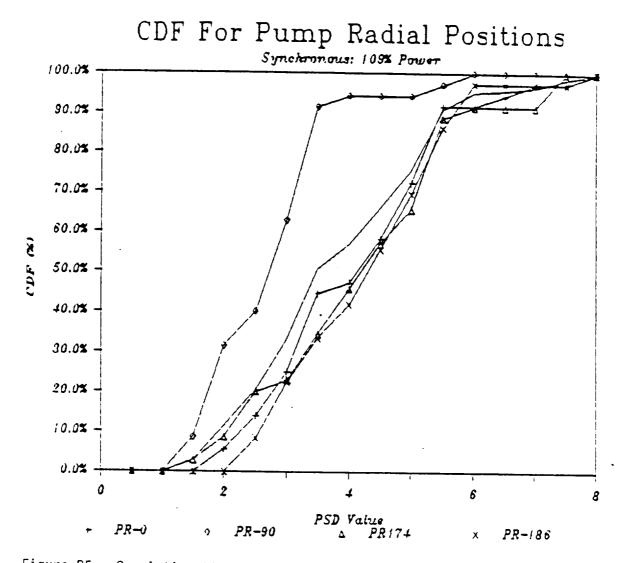


Figure D5. Cumulative Distribution Functions For Differing Pump Locations

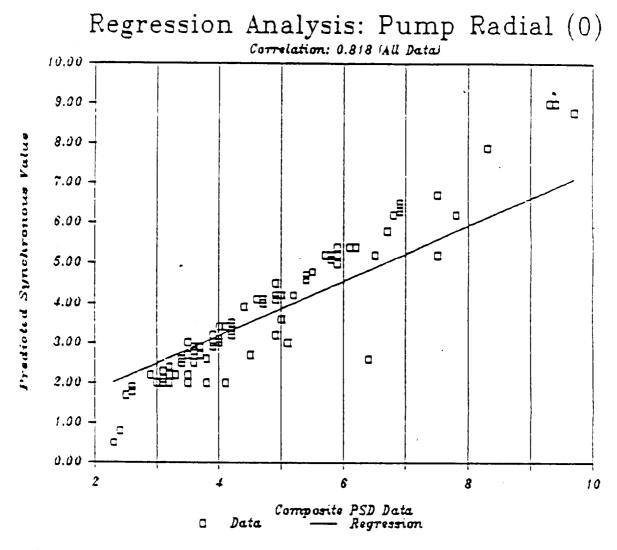


Figure D6. Composite And Synchronous Correlation For All Power Levels

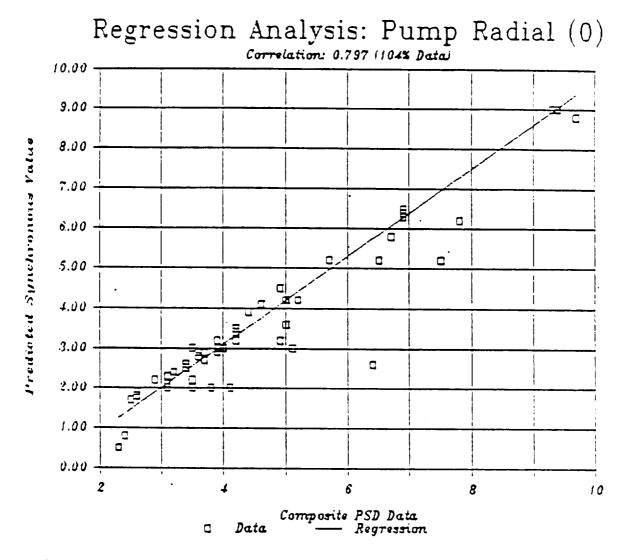


Figure D7. Composite And Synchronous Correlation For 104% Power Levels

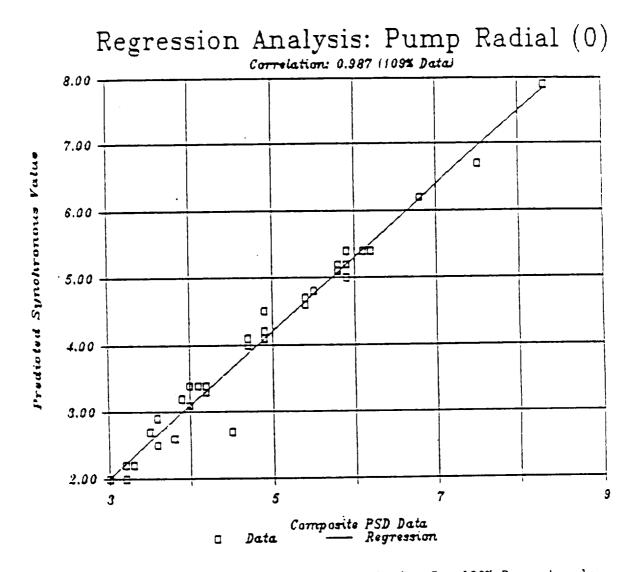


Figure D8. Composite And Synchronous Correlation For 109% Power Levels

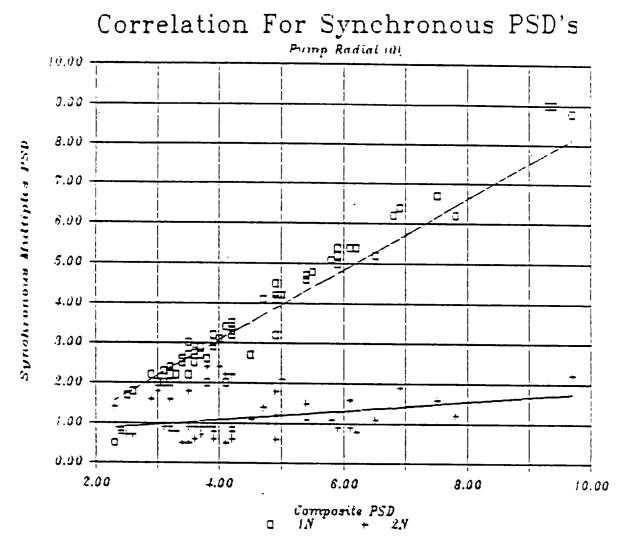


Figure D9. Correlation Of Higher Multiple Synchronous Data

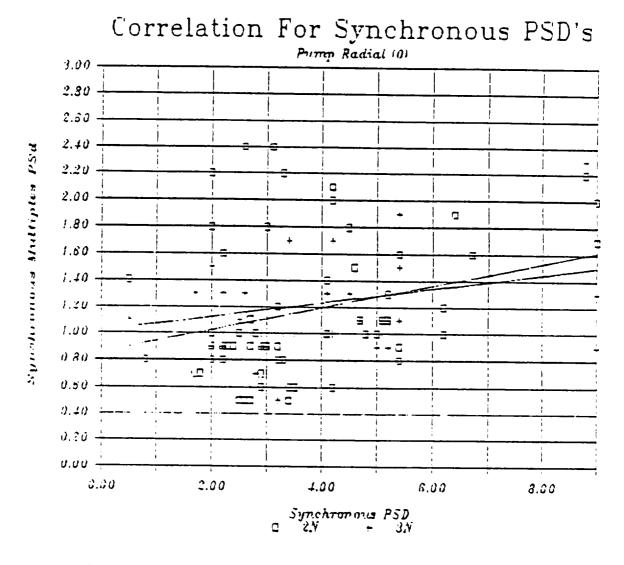
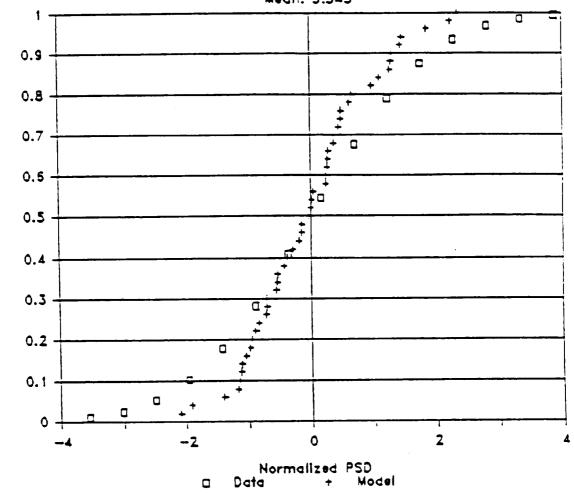


Figure D10. Correlation Of Higher Multiple Synchronous Data

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CDF

Comparison Of Periodic Model And Data

Figure Dll. Comparison of MSFC Pump Rad (O) Data and Model Prediction

## REFERENCES

D.1 Faddeeva, V. N., "Computational Methods of Linear Algebra," Dover Publications, 1959.

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